

Astronomy 13 Equations (Spring 2010)

A.U. = $1.5 \times 10^{11} \text{m}$ **pc** = 206,000 A.U. = $3 \times 10^{16} \text{m}$ **Solar mass** = $2 \times 10^{30} \text{kg}$
Solar Radius = $7 \times 10^8 \text{m}$ **Solar Luminosity** = $4 \times 10^{26} \text{W}$ **Proton mass** = $1.67 \times 10^{-27} \text{kg}$
Year: $3 \times 10^7 \text{s}$ **Earth mass** = $6 \times 10^{24} \text{kg}$ **Earth radius** = $6.4 \times 10^6 \text{m}$ $\text{W} = \text{J/s} = 10^7 \text{ergs/s}$
Angles: $360 \text{ deg} = 2\pi \text{ radians}$ $1 \text{ deg} = 60 \text{ arcmin}$ $1 \text{ arcmin} = 60 \text{ arcsec}$
 1 arcsec : $\text{transverse size} = \text{distance}/206,000$

Waves & Photons: $\text{Wavelength}(\lambda) \times \text{Frequency}(\nu) = c(\text{speed of light})$
 $\text{Energy} = h\nu = hc/\lambda$ where Planck's constant $h = 6.6 \times 10^{-34} \text{J}\cdot\text{s}$ and $c = 3 \times 10^8 \text{m/s}$

Wien's Law: $\text{Peak Wavelength}(\text{m}) = 0.0029/T$ $T = \text{temperature in K} = \text{Kelvin}$

Stefan-Boltzman Law: $\text{Flux}(\text{W/m}^2) = \sigma T^4$ where $\sigma = 5.67 \times 10^{-8} \text{W/m}^2 \text{K}^4$ $T(\text{K})$
 For surface of sphere, $\text{Luminosity}(\text{W}) = 4\pi R^2 \sigma T^4$ $R = \text{radius}(\text{m})$ of sphere

Redshift z: $z = \frac{\lambda(\text{obs}) - \lambda(\text{rest})}{\lambda(\text{rest})} \sim \text{velocity}/c$ (at low velocities)

Matter density (z) = matter density(at z=0) * $(1+z)^3$

Radiation density (z) = radiation density(at z=0) * $(1+z)^4$

Hubble Law: $\text{velocity} = H_0 * \text{Distance}$ $\text{velocity}(\text{km/s}), H_0(\frac{\text{km}}{\text{s} * \text{Mpc}}), \text{Distance}(\text{Mpc})$

Brightness: $b(\text{W/m}^2) = \frac{\text{Luminosity}}{4\pi \text{Distance}^2}$ where for Sun at Earth $b = 1370 \text{W/m}^2$

Magnitudes: $\text{apparent mag } m = -2.5 \log(\text{brightness}) + \text{Constant}$

$\text{Absolute mag } M = -2.5 \log(\text{brightness at } 10\text{pc}) + \text{Constant}$ $M(\text{sun}) = +5$

$\text{Absolute mag } M = -2.5 \log(L/L_{\text{sun}}) + 5$

$\text{Distance Modulus} = m - M = 5 \log(\text{distance in pc}) - 5$

$\text{Log } a = b \rightarrow 10^b = a$ $= 5 \log(\text{distance in Mpc}) + 25$

Proper Motion: $\mu(\text{arcsec/yr}) = \frac{T}{4.74D}$ $T = \text{transverse motion}(\text{km/s})$ $D = \text{Distance}(\text{pc})$

Luminosity of Stars: $L \propto \text{Mass}^4$

Radiation Blackbody Energy Density: $U = aT^4$ $a = 7.6 \times 10^{-16} \frac{\text{W}}{\text{m}^3 \text{K}^4}$

Radiation Mass Density: $U/c^2 = 4.6 \times 10^{-31} \text{kg/m}^3$ (from analogy of $E = mc^2$)

Law of Gravitation: $\text{Force} = \frac{GmM}{D^2}$ $G = 6.7 * 10^{-11} \frac{\text{m}^3}{\text{s}^2 \text{kg}}$ m, M are masses(kg)
 $D = \text{distance}(\text{m})$

Escape Velocity or Bending Angle: $v \propto \sqrt{\frac{\text{mass}}{\text{distance}}}$

EQUATIONS (continued)

Special Relativity Relations: $t(obs) = t(rest) / \sqrt{1 - \frac{v^2}{c^2}}$ Energy = mass c^2

$length(moving) = length(rest) \sqrt{1 - \frac{v^2}{c^2}}$ $mass(moving) = mass(rest) / \sqrt{1 - \frac{v^2}{c^2}}$

Schwarzschild Radius: $R (m) = 2 G \text{ Mass} / c^2 = 3\text{km} * \text{Mass}(\text{units of Sun})$

Heisenberg Uncertainty Principle: $\Delta t * \Delta E > h/2\pi$

Where ΔE is the uncertainty in its measurement of energy when measurement is over an interval of time Δt .

$$\Delta d * \Delta p > h/2\pi$$

where Δd is the distance interval and Δp is the uncertainty in the momentum

Compton wavelength: $\lambda(\text{compton}) = h/mc$

Where $h = \text{Planck's constant} = 6.63 * 10^{-34} \text{ J s} = 4.1 * 10^{-15} \text{ eV s}$
 $1\text{eV} = 1.6 * 10^{-19} \text{ J}$

Planck Mass: $= \sqrt{\frac{hc}{G}} = 5.5 * 10^{-8} \text{ kg}$

Planck Length: $= \sqrt{\frac{Gh}{c^3}} = 4.1 * 10^{-35} \text{ m}$

Planck Time: $= (\text{Planck length})/c = 1.4 * 10^{-43} \text{ s}$

Energy Conservation: $\frac{v^2}{2} - \frac{Gm}{r} = \text{constant}$

Einstein's Eq. For U: $\frac{H^2}{2} - \frac{4\pi G}{3} D = -\frac{kC}{r^2} + \frac{\Lambda}{3}$

Critical Density: $Density(\text{critical}) = 3H_0^2 / (8\pi G) \sim 1 * 10^{-26} \text{ kg/m}^3$

Density Parameter: $\Omega_0 = \text{mass density} / \text{critical density}$

Deceleration Parameter: $q_0 = \frac{\Omega_0}{2} - \frac{\Lambda c^2}{3H_0^2} = \Omega_0/2$ if cosmological constant $\Lambda=0$

Mass: mass = density x volume For spherical case = density * $4\pi R^3/3$
 $\propto rv^2$ $r=\text{size}$ $v=\text{velocity}$

Temperature (K) of Universe $= \frac{10^{10} K}{\sqrt{t}}$ where $t=\text{age of Universe in seconds}$

Typical Energy of Photons $= \frac{2\text{Mev}}{\sqrt{t}}$ where $t=\text{age of Universe in seconds}$