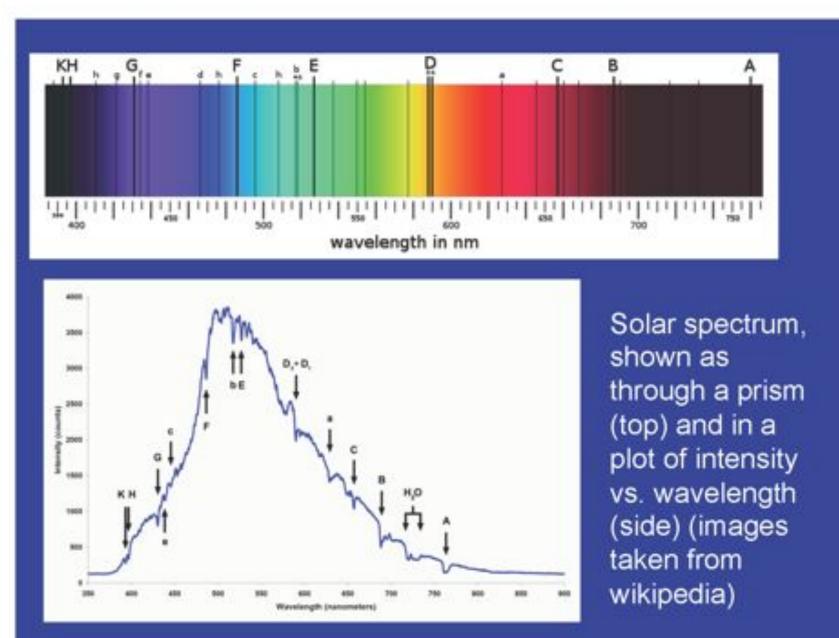
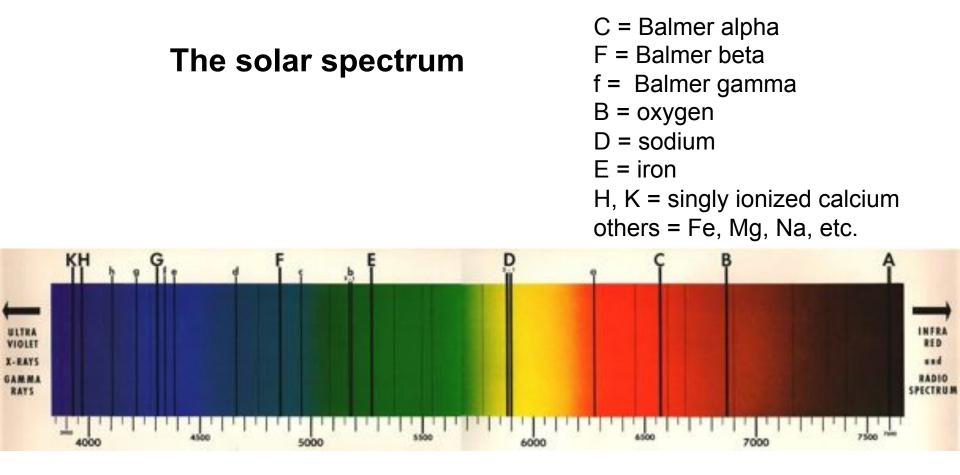
Lecture 3

Atomic Spectroscopy and Abundances

Glatzmaier and Krumholz 1 Pols 3.5.1





Wollaton (1802) discovered dark lines in the solar spectrum. Fraunhaufer rediscovered them (1817) and studied the systematics.

Note D, H, K stronger tha C, F, f but the sun is not made of Na and Ca,

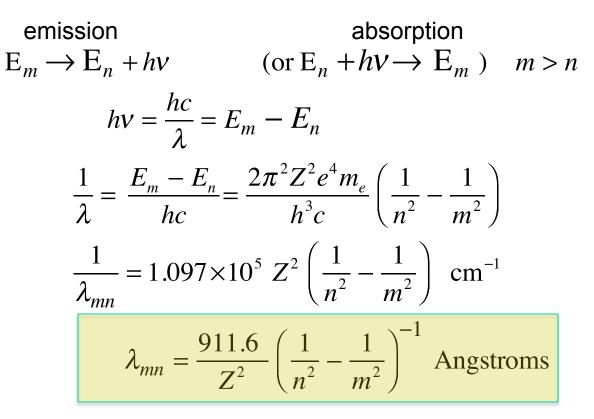
	Die	wichtigsten Fraunho	oferlinien	Im Ubert	blick
Symbol	Element	Wellenlänge in nm	Symbol	Element	Wellenlänge in nm
у	02	898,765	с	Fe	495,761
z	O ₂	822,696	F	Нβ	486,134
A	O ₂	759,370	d	Fe	466,814
в	O ₂	686,719	е	Fe	438,355
с	Ηa	656,281	G'	Hγ	434,047
a	O ₂	627,661	G	Fe	430,790
D ₁	Na	589,594	G	Ca	430,774
D ₂	Na	588,997	h	Нδ	410,175
D ₃ oder d	He	discovery of He 587,562 in the sun	н	Ca ⁺	396,847
е	Hg	Lockyer 1868	к	Ca*	393,368
E ₂	Fe	527,039	L	Fe	382,044
b ₁	Mg	518,362	N	Fe	358,121
b ₂	Mg	517,270	Р	Ti+	336,112
b ₃	Fe	516,891	т	Fe	302,108
b ₄	Fe	516,751	t	Ni	299,444
b ₄	Mg	516,733			

Fraunhofer's Notation

Quantum mechanics tells us:

Radiation in the form of a single quantum (photon) is emitted (or absorbed) when an electron makes a transition from one energy state to another in an atom. The energy of the photon is the difference between the energies of the two states.

E.g., for hydrogen-like atoms



(for atoms with only one electron)

E.g.,

$$m = 2, \quad n = 1, \quad Z = 1$$

$$\lambda = 911.6 \quad \stackrel{\circ}{A} \left(\frac{1}{1^2} - \frac{1}{2^2}\right)^{-1} = 911.6 \left(\frac{3}{4}\right)^{-1}$$

$$= 911.6 \left(\frac{4}{3}\right) = 1216 \stackrel{\circ}{A}$$

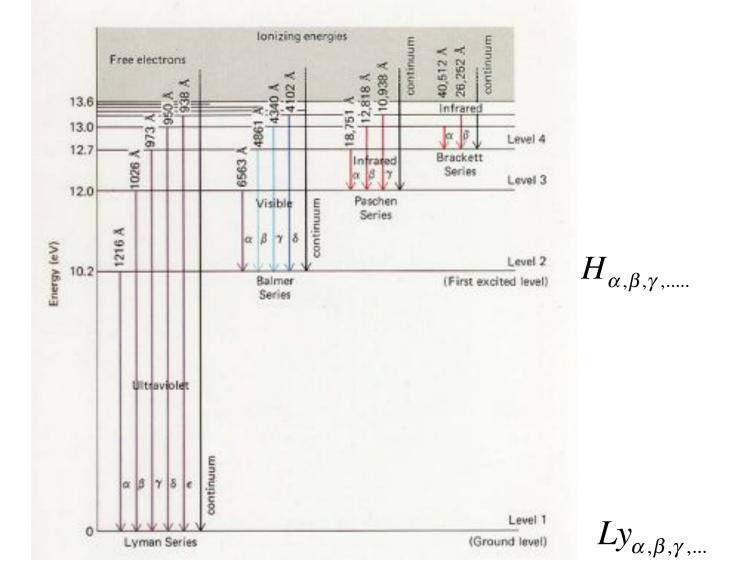
m=3, n=1, Z=1

$$\lambda = 911.6 \left(\frac{1}{1^2} - \frac{1}{3^2}\right)^{-1} = 911.6 \left(\frac{8}{9}\right)^{-1}$$
$$= 911.6 \left(\frac{9}{8}\right) = 1026 \text{ Å}^{\circ}$$

m = 3, n = 2, Z = 1 $\lambda = 911.6 \left(\frac{1}{2^2} - \frac{1}{3^2}\right)^{-1} = 911.6 \left(\frac{1}{4} - \frac{1}{9}\right)^{-1}$ $= 911.6 \left(\frac{5}{36}\right)^{-1} = 911.6 \left(\frac{36}{5}\right) = 6563 \text{ Å}$ Lines that start or end on n=1 are called the "Lyman" series. All are between 911.6 and 1216 A.

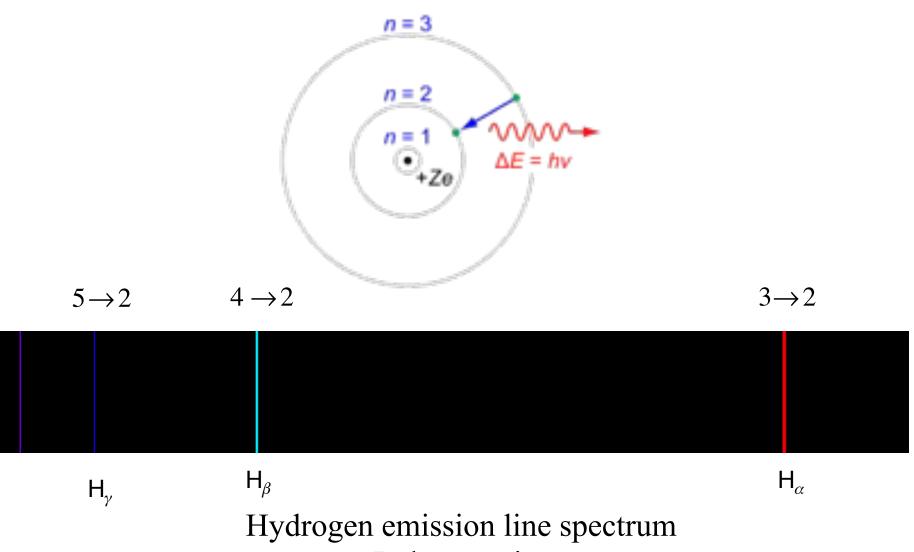
 $\lambda_{mn} = \frac{911.6 \text{ A}}{Z^2} \left(\frac{1}{n^2} - \frac{1}{m^2}\right)^{-1}$

Lines that start or end on n=2 are called the "Balmer" series. All are between 3646 (i.e. 4*911.6) and 6564 A.



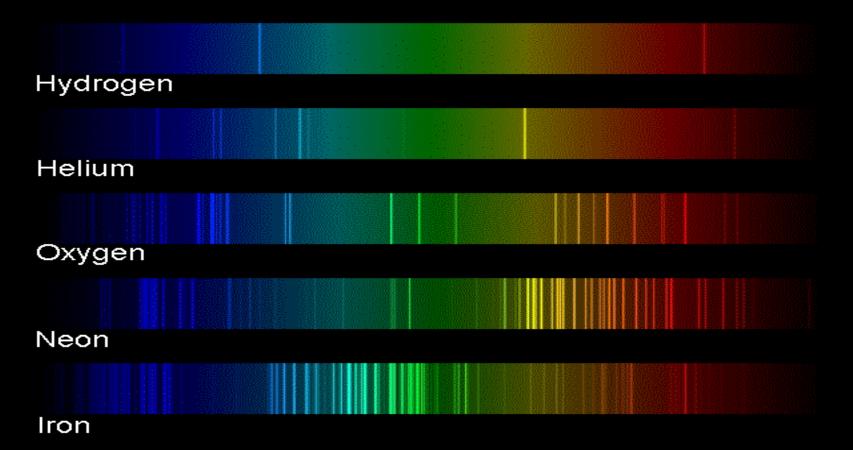
Adjusting the energy of each state in hydrogen by adding 13.6 eV (so that the ground state becomes zero), one gets a diagram where the energies of the transitions can be read off easily.

BALMER SERIES

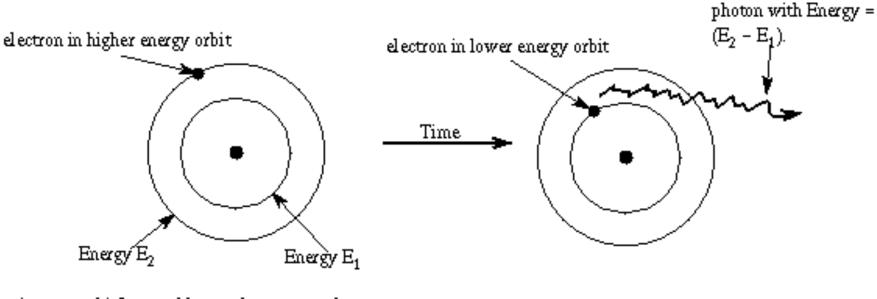


Balmer series

Heavier atoms have more energy levels and more complex spectra



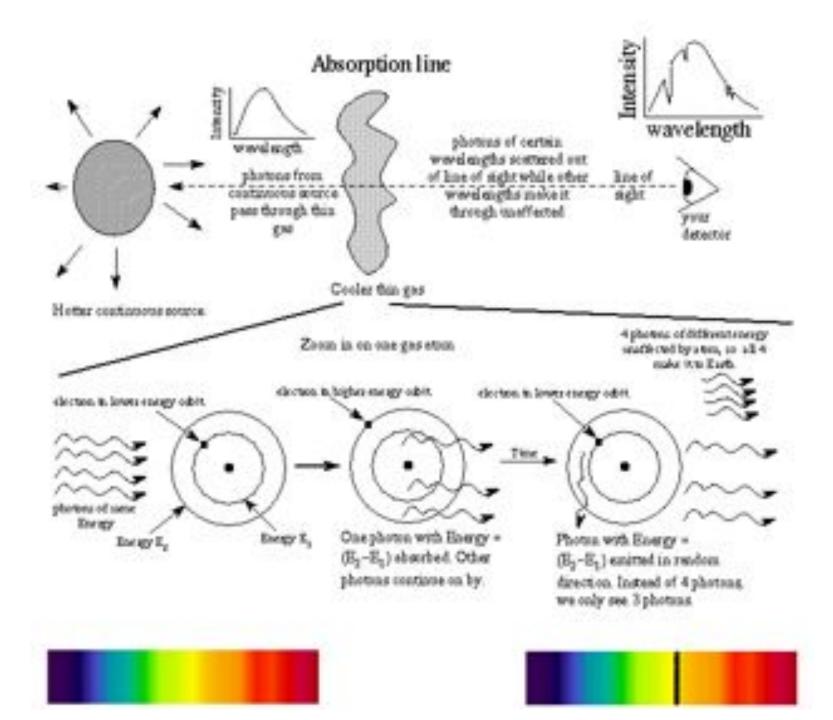
Emission line

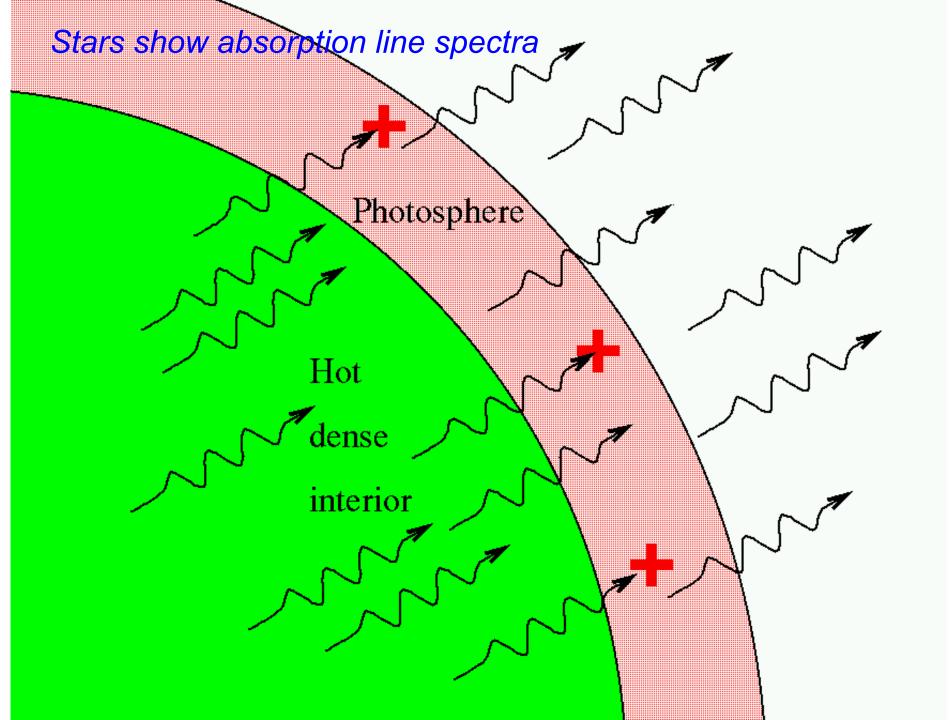


Emission line produced!

Atom was hit/bumped by another atom and gained some energy = $(E_2 - E_1)$. Electron in higher energy orbit (E_2) .



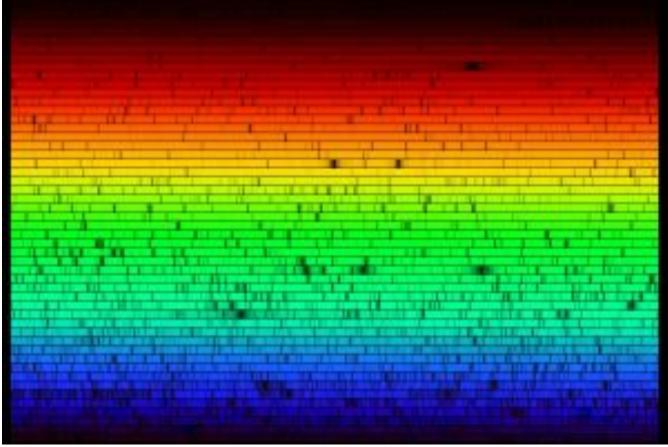




Absorption Spectra:

provide majority of data for elemental abundances because:

- by far the largest number of elements can be observed
- low fractionation due to convection zone still well mixed
- well understood good models available



solar spectrum (Nigel Sharp, NOAO)

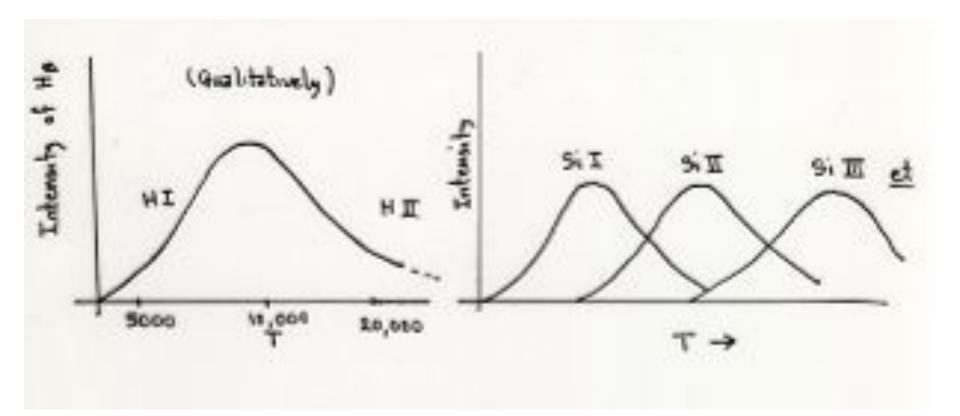
Ionization state of the absorbing gas

As the temperature in a gas is raised, electrons will be removed from atoms by collisions and interactions with light. The gas becomes *ionized*.

The degree of ionization depends on the atom considered and the density and temperature. High density favors recombination and high temperature favors ionization.

Notation: Ionization stages

ΗI	neutral hydrogen	1 p	1 e
ΗII	ionized hydrogen	1 p	0 e
He I	neutral helium	2 p	2 e
He II	singly ionized helium	2 p	1 e
He III	doubly ionized helium	2 p	0 e
CI	neutral carbon	6 p	6 e
C II	C^+	6 p	5 e
C III	C^{++}	6 p	4 e
etc.			

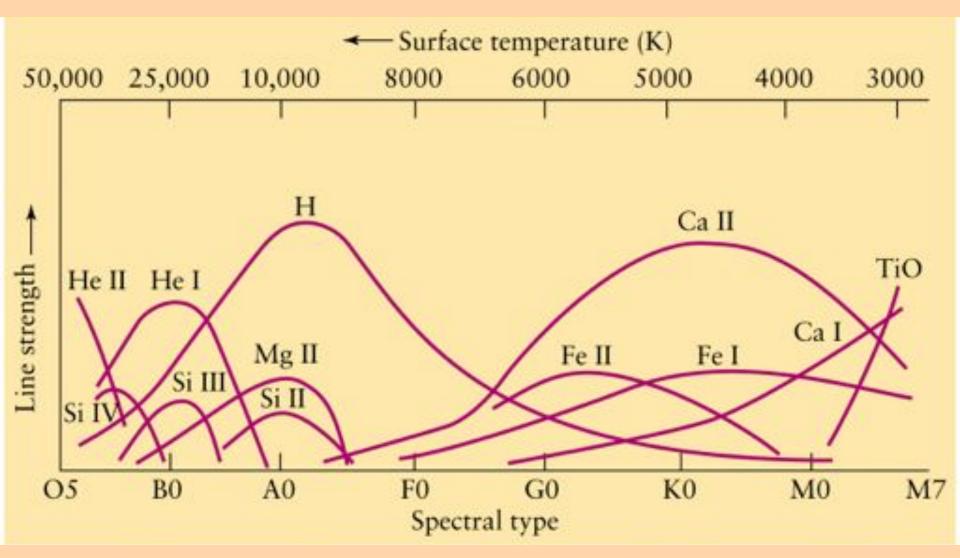


The ionization energy is the energy required to remove a single electron from a given ion. The excitation energy is the energy required to excite an electron from the ground state to the first excited state.

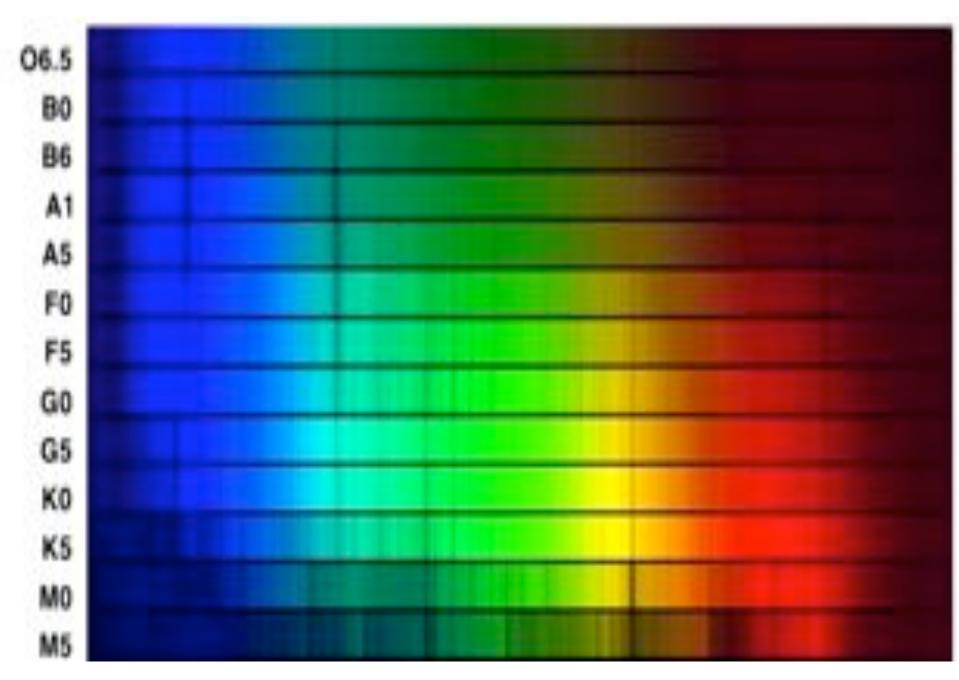
Ion	Excitation energy (eV)	Ionization energy (eV)	
ΗI	10.2	13.6	
He I	20.9	24.5	
He II	40.8	54.4	
rare _{Li I}	1.8	5.4	
Ne I	16.6	21.5	
Na I	2.1	5.1	
Mg I	2.7	7.6	
Ca I	1.9	6.1	

Li is He plus one proton, Na is Ne plus 1 proton, Ca is Ar plus 2 protons. The noble gases have closed electron shells and are very stable.

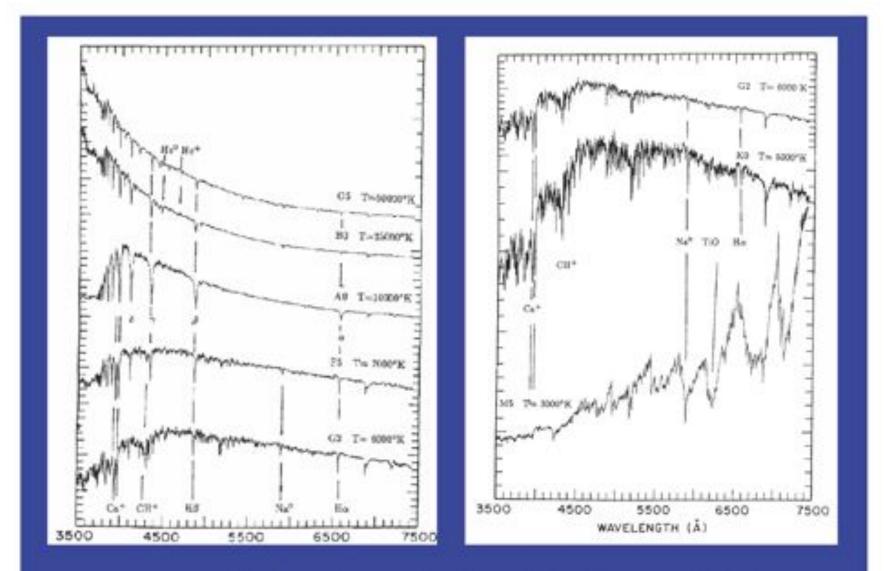
Some of the stronger lines in stars



The composition is not varying, just the temperature, and to a lesser extent, the density



and now L, T, and Y but these are mostly brown dwarfs



Spectra for O - G stars (left) and G - M stars (right)

Spectral Classes

table 19-2	The Spectral Sequence				
Spectral class	Color	Temperature (K)	Spectral lines	Examples	
0	Blue-violet	30,000-50,000	Ionized atoms, especially helium	Naos (ζ Puppis), Mintaka (δ Orionis)	
В	Blue-white	11,000-30,000	Neutral helium, some hydrogen	Spica (α Virginis), Rigel (β Orionis)	
A	White	7500-11,000	Strong hydrogen, some ionized metals	Sirius (α Canis Majoris), Vega (α Lyrae)	
F	Yellow-white	5900-7500	Hydrogen and ionized metals such as calcium and iron	Canopus (α Carinae), Procyon (α Canis Minoris)	
G	Yellow	5200-5900	Both neutral and ionized metals, especially ionized calcium	Sun, Capella (α Aurigae)	
K	Orange	3900-5200	Neutral metals	Arcturus (α Boötis), Aldebaran (α Tauri)	
М	Red-orange	2500-3900	Strong titanium oxide and some neutral calcium	Antares (α Scorpii), Betelgeuse (α Orionis)	
L	Red	1300-2500	Neutral potassium, rubidium, and cesium, and metal hydrides	Brown dwarf Teide 1	
т	Red	below 1300	Strong neutral potassium and some water (H ₂ O)	Brown dwarf Gliese 229B	

Main Sequence Luminosities and Lifetimes

table 21-1	Main-Sequence Lifetimes				
Mass (M _o)	Surface temperature (K)	Spectral class	Luminosity (L _©)	Main-sequence lifetime (10 ⁶ years)	
25	35,000	0	80,000	3	
15	30,000	В	10,000	15	
3	11,000	Α	60	500	
1.5	7000	F	5	3000	
1.0	6000	G	1	10,000	
0.75	5000	К	0.5	15,000	
0.50	4000	М	0.03	200,000	

DISTINGUISHING MAIN SEQUENCE STARS FROM RED GIANTS OF THE SAME COLOR

The surface gravity

$$g = \frac{GM}{R^2}$$

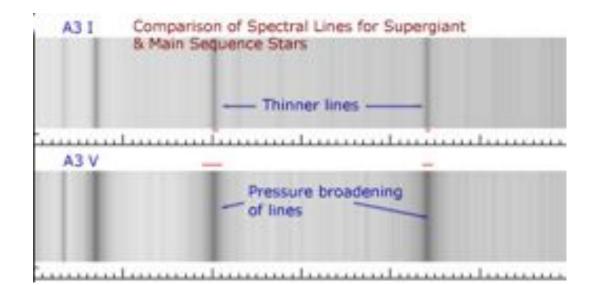
of a star is clearly larger for a smaller radius (if M is constant)

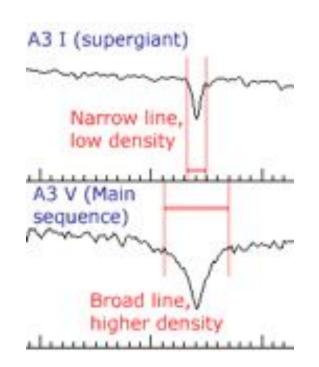
To support itself against this higher gravity, a the stellar photosphere must have a larger pressure. As we shall see later for an ideal gas P = n k T

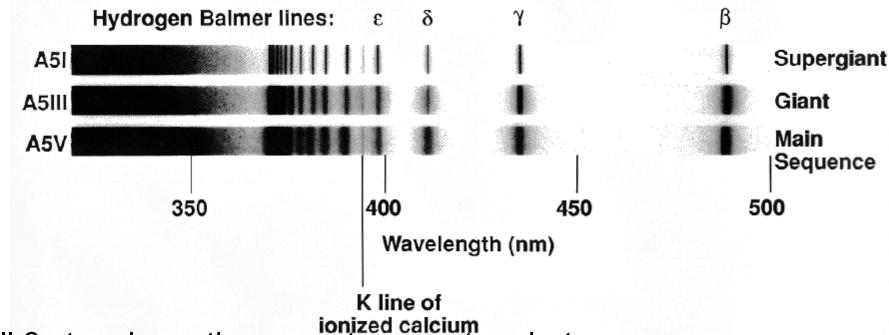
where n is the number density and T is the temperature. If two stars have the same temperature, T, the one with the higher pressure (smaller radius) will have the larger n, i.e., its atoms will be more closely crowded together. This has two effects:

1) At a greater density (and the same T) a gas is less ionized

2) If the density is high, the electrons in one atom "feel" the presence of other nearby nuclei. This makes their binding energy less certain. This spreading of the energy level is called "Stark broadening"







All 3 stars have the same temperature but,

- The supergiants have the narrowest absorption lines
- Small Main-Sequence stars have the broadest lines
- Giants are intermediate in line width and radius

- In 1943, Morgan & Keenan added the *Luminosity Class* as a second classification parameter:
 - -Ia = Bright Supergiants
 - -Ib = Supergiants
 - -II = Bright Giants
 - -III = Giants
 - -IV = Subgiants
 - -V = Main sequence

And so the sun is a G2-V star

ABUNDANCES AND IONIZATION

http://www.spms.ntu.edu.sg/PAP/courseware/statmech.pdf

The Boltzman equation derived from MB statistics

describes excitation in a single atom

$$\frac{n_s}{N} = \frac{g_s \exp(-\beta\varepsilon_s)}{\sum_r g_r \exp(-\beta\varepsilon_r)} \qquad \beta = \frac{1}{k7}$$

from the Boltzmann equation one can also derive the

Saha equation which describes ionization http://www.phy.ohiou.edu/~mboett/astro401_fall12/saha.pdf

$$\frac{N_{i+1}}{N_i} = \frac{g_{i+1}}{g_i} \frac{2}{n_e h^3} (2\pi m_e kT)^{3/2} \exp(-\chi / kT)$$

where g_i and g_{i+1} are the partition functions for the two ionization states of the species i and i+1 and χ is the ionization potential of the species i (the difference in energy between states i and i+1). 2 is because the spins of the proton and electron can be alligned or counteralligned in the neutral atom Aside:

$$V\Delta^{3}p \sim h^{3}$$
$$1/V \sim n_{e}$$
$$\Delta p^{3} \sim h^{3}n_{e}$$

One often sees terms like $(2\pi m_k T)$ and $1/(n_k^3)$ when dealing with quantum statistics. As we will discuss a bit more next week, there exists a volume in momentum space, much like in real space - $4\pi p^2 dp$ (like $4\pi r^2 dr$ in spherical 3D coordinates). The ratio $8\pi p^2 dp / n_h^3$ is essentially how many electrons one can have in that volume (between p and p +dp) according to the uncertainty principle (2 electrons per cell) in phase space times the volume of one electron V = $1/n_{a}$

In summing over all the states in a continuous distribution of momenta, one gets integrals like

$$\frac{8\pi}{n_e h^3} \int_0^\infty p^2 e^{-p^2/2mkT} dp = \frac{4\pi}{n_e h^3} \left(2m_e kT\right)^{3/2} \int_0^\infty \sqrt{x} e^{-x} dx$$

where x = p² / (2m_e kT). The integral is $\sqrt{\pi}$ / 2 so
one gets $\frac{2\left(2\pi m_e kT\right)^{3/2}}{n_e h^3}$

As an example, lets apply these equations to understand the strength of Ca and H lines in the sun. In the spectrum the lines of Ca II (Ca⁺) appear stronger than those of H. Is the sun made of calcium?

The calculation proceeds in 2 steps and follows GK 1.

We take as given the sun's photospheric temperature (5780 K) and *electron* pressure (this will be discussed more later) – 15 dyne cm^{-2.}The latter will be used to provide the electron density, n_e , assuming ideal gas pressure $P_e = n_e kT$.

$$n_e = \frac{P_e}{kT} = \frac{15}{(1.38 \times 10^{-16})(5780)} = 1.9 \times 10^{13} \text{ cm}^{-3}$$

First is hydrogen neutral or ionized?

$$\frac{n(H \, II)}{n(H \, I)} = \frac{g_{II}}{g_{I}} \frac{2}{n_{e}h^{3}} (2\pi m_{e}kT)^{3/2} \exp(-\chi \,/\,kT)$$

 g_{μ} is just the statistical weight of the proton - 1 if it is unbound

g, is the partiction function for the neutral H atom which in the general case is a bit complicated because one must assign statistical weights to all the bound states. From QM each energy state n is 2n² degenerate (i.e., there are n² levels with different m and I having the same energy. Further the binding energy of each state

is 13.6 eV
$$(1-\frac{1}{n^2})$$
 so

$$g_{I} = \sum_{n=1}^{\infty} g_{n} e^{-(E_{I} - E_{1})/kT} = \sum_{n=1}^{\infty} 2n^{2} \exp\left(\frac{-13.6 eV}{kT} \left(1 - \frac{1}{n^{2}}\right)\right)$$

but since kT =8.622×10⁻⁵ (5780 K)=0.50 eV, all terms are negligible except n = 1, the ground state for which g_1 =2. The electron and the proton spins may be alligned or counter-alligned

$$\frac{n(H II)}{n(H I)} = \frac{1}{2} \frac{2}{1.9 \times 10^{13}} \left(\frac{2\pi m_e kT}{h^2}\right)^{3/2} e^{-13.6/0.50}$$
$$\left(\frac{2\pi m_e kT}{h^2}\right)^{3/2} = 2.41 \times 10^{15} T(K)^{3/2}$$
$$n(H II)$$

 $\frac{n(H II)}{n(H I)} = 8 \times 10^{-5}$

The hydrogen is neutral to a high degree.

Note that this also implies that the number of free electrons is very much less than that of the ions and electronic pressure, in the solar photosphere is a small fraction of the total pressure. What about the number of H in the n = 2

level that can absorb Balmer alpha?

The difference in the n = 1 and 2 energy levels

is 13.6 eV times
$$(1 - \frac{1}{4}) = 10.2$$
 eV. The population

factor is then given by the Boltzmann distribution

$$\frac{N_{n=2}}{N_{n=1}} = \frac{g_2}{g_1} \exp(-10.2 / kT) = \frac{2(2^2)}{2} e^{-10.2 / 0.50}$$
$$= 5.5 \times 10^{-9}$$

a) Less than one hundred millionth of the H atoms are in their first excited state (many fewer in higher states)

 b) The number rises rapidly with increasing temperature so (Balmer) hydrogen lines should be stronger in stars more massive than the sun - for awhile. What about Ca? Experimentally GK say the partition function for neutral Ca between 5000 and 6000 K is 1.32 and for Ca II is 2.30. The ratio of singly ionized Ca to neutral Ca is then

$$\frac{n(Ca II)}{n(Ca I)} = \frac{2g(Ca II)}{g(Ca I)n_e} \left(\frac{2\pi m_e kT}{h^2}\right)^{3/2} \exp(-6.11 eV / kT)$$
$$= \frac{2(2.3)}{1.32(1.9 \times 10^{13})} 2.41 \times 10^{15} (5780)^{3/2} e^{-6.11/0.50}$$
$$= 950$$

Unlike H, Ca is overwhelmingly ionized. We could also calculate the ratio of Ca III/Ca II but it is small.

The fraction of Ca that is in the ground state is the partition function for the ground state, which, it turns out, is 2, divided by the total partition function for Ca II which is 2.3, so 87% is in the ground state. Together these results imply that:

 a) Hydrogen is neutral but only 5 x 10⁻⁹ is in the first excited state and capable of absorbing a Balmer alpha photon

b) Most calcium is Ca II in its ground state

If the observed line strengths show 400 more Ca II absorbers than H_a absorbers, the actual abundance ratio of Ca to H is $\frac{N(Ca)}{N(H)} = 400 \left(\frac{5.5 \times 10^{-9}}{0.87}\right) = 2.5 \times 10^{-6}$

As we shall see the actual modern abundance ratio is 2.1×10^{-6}

Oscilator strengths?

For the same electron pressure, at what temperature will hydrogen be half ionized?

$$\frac{N_{i+1}}{N_i} = 1 = \frac{g_{i+1}}{g_i} \frac{2}{n_e h^3} (2\pi m_e kT)^{3/2} \exp(-\chi / kT)$$
$$= \frac{g_{i+1}}{g_i} \frac{2}{P_e} \left(\frac{2\pi m_e}{h^2}\right)^{3/2} (kT)^{5/2} \exp(-\chi / kT)$$
$$\left(\frac{2\pi m_e}{h^2}\right)^{3/2} = 1.49 \times 10^{39} \qquad \chi = 13.6 \,\text{eV}$$

kT in erg = 1.602×10⁻¹² kT in eV (kT)^{5/2} in erg = 3.25×10⁻³⁰ (kT)^{5/2} in eV

IF
$$P_e = constant = 15 dyne cm^{-2}$$

 $1 = (1.49 \times 10^{39})(3.25 \times 10^{-30})\frac{(kT)_{eV}^{5/2}}{15}e^{-13.6/kT_{eV}}$
 $x^{5/2}e^{-13.6/x} = 3.10 \times 10^{-9}$ $x = 0.724 \text{ eV}$ or $T = 8400 \text{ K}$
But this underestimates T considerably because P_e will
increase with temperature due to ionization. Note that
bigger P_e (or n_e) means less ionization

Done correctly, 'when H becomes mostly ionized. $n_{e} = n(HII).$ $\frac{n^{2}(HII)}{n(HI)} = \frac{2g_{II}}{g_{I}} \left(\frac{2\pi m_{e}kT}{h^{2}}\right)^{3/2} e^{-13.6/kT}$ $n(HI) + n(HII) = n(H) = \rho X_{H}N_{A} \quad \text{Let } n(HII) = y n(H)$

$$n(H I) = (1 - y)n(H)$$
 $X_{H} = 0.7$

Then

$$\frac{y^2 n(H)}{(1-y)} = \left(\frac{2\pi m_e kT}{h^2}\right)^{3/2} e^{-13.6/kT}$$
$$\frac{y^2}{(1-y)} = \frac{1}{\rho N_A X_H} \left(\frac{2\pi m_e kT}{h^2}\right)^{3/2} e^{-13.6/kT} \qquad P_{gas} = \frac{\rho N_A kT}{\mu}$$
$$= \frac{1}{\mu P_{gas}} \left(\frac{2\pi m_e kT}{h^2}\right)^{3/2} (kT) e^{-13.6/kT}$$

The left hand side is 1/2 if y = 1/2, so we have pretty much the same equation we had before except with μP_{gas} ($\mu \approx 0.6$) instead of P_{e}

$$\frac{1}{2} = \frac{1}{\mu P_{gas}} \left(\frac{2\pi m_e kT}{h^2} \right)^{3/2} (kT) e^{-13.6/kT}$$

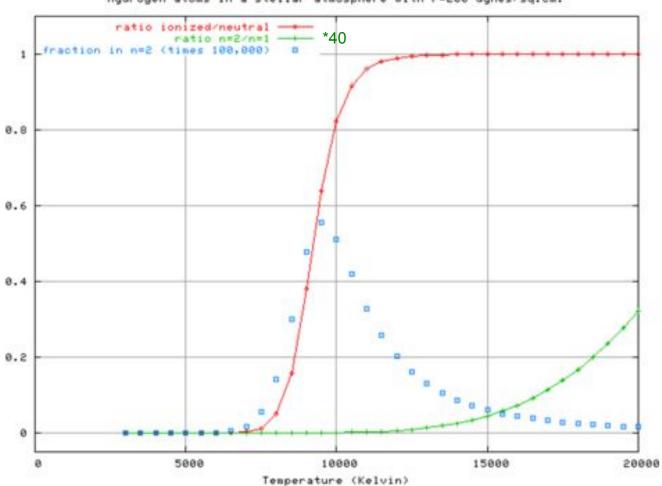
As we shall show next time the pressure in the solar photosphere times μ is a few $\times 10^4$ and this declines as "g" in heavier stars. Solving as before (and including the .7 for Habundance and the 33% contribution of electron pressure)

$$x^{5/2}e^{-13.6/x} \approx 2 \times 10^{-6}$$

T \approx 12,000 K

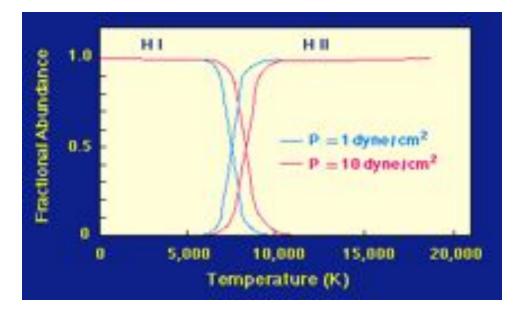
and this is closer to correct, though not very different because of the exponential. Actually P_{gas} declines at higher masses so this is an overestimate.

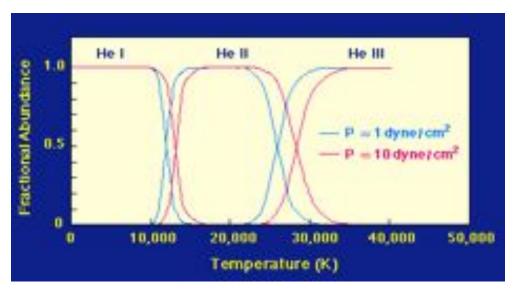
http://spiff.rit.edu/classes/phys440/lectures/saha/saha.html

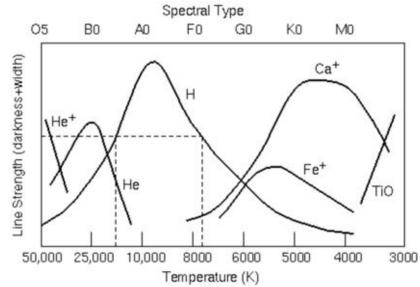


Hydrogen atoms in a stellar atmosphere with P=200 dynes/sq.cm.

http://csep10.phys.utk.edu/astr162/lect/stars/spectra.html

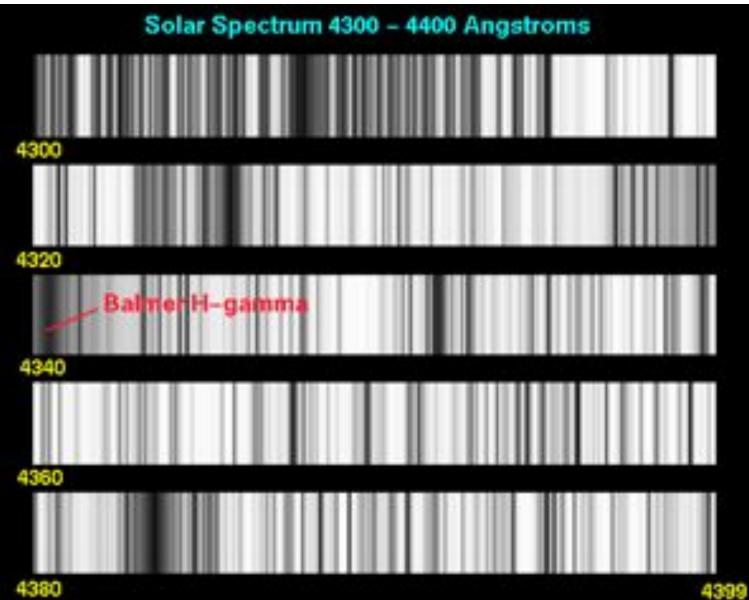






(Part of) the solar spectrum

Over 100,000 lines are visible in the entire spectrum 70 Elements have been measured



In practice, to obtain abundances, one builds a model "stellar atmosphere" in which heat flux, gravity, and hydrostatic equilibrium (TBD) are given and solves consistently for the ionization, electron density, pressure, and line strengths.

One of many concerns is the assumption of "local thermodynamic equilibrium", that the level populations are accurately represented by the Boltzmann equation.

In non-LTE situations one must solve rate equations to get the level populations.

Complications for photospheric abundance determinations

Oscillator strengths:

Need to be measured in the laboratory - still not done with sufficient accuracy for a number of elements.

Line width

Depends on atomic properties but also thermal and turbulent broadening. Need an atmospheric model.

Line blending

Ionization State

Model for the solar atmosphere

Turbulent convection. Possible non-LTE effects. 3D models differ from 1 D models. See Asplund, Grevesse, and Sauval (2007).

Meteorites

Meteorites can provide accurate information on elemental abundances in the presolar nebula. More precise than solar spectra data in some cases. Principal source for isotopic information.

But some gases escape and cannot be determined this way (for example hydrogen and noble gases)

Not all meteorites are suitable - most of them are fractionated and do not provide representative solar abundance information. Chondrites are meteorites that show little evidence for melting and differentiation.

Group	Subgroup	Frequency
Stones	Chondrites	86%
	Achondrites	7%
Stony Irons		1.5%
Irons		5.5%

Classification of meteorites:

Carbonaceous chondrites are 4.6% of meteor falls.

H Schatz

Use carbonaceous chondrites (~5% of falls)

Chondrites: Have Chondrules - small ~1mm size shperical inclusions in matrix believed to have formed very early in the presolar nebula accreted together and remained largely unchanged since then

Carbonaceous Chondrites have lots of organic compounds that indicate very little heating (some were never heated above 50 degrees K)



http://www.psrd.hawaii.edu/May06/meteoriteOrganics.html

"Some carbonaceous chondrites smell. They contain volatile compounds that slowly give off chemicals with a distinctive organic aroma. Most types of carbonaceous chondrites (and there are lots of types) contain about 2% organic compounds, and these are very important for understanding how organic compounds might have formed in the solar system. They even contain complex compounds such as amino acids, the building blocks of proteins."

There are various subclasses of carbonaceous chondrites. The C-I's and C-M's are general thought to be the most primitive because they contain water and organic material. They are fine grained and contain no chondrules or refractory inclusions.

The CM meteorite Murchison, has over 70 extraterrestrial amino acids and other compounds including carboxylic acids, hydroxy carboxylic acids, sulphonic and phosphoric acids, aliphatic, aromatic, and polar hydrocarbons, fullerenes, heterocycles, carbonyl compounds, alcohols, amines, and amides.



Five CI chondrites have been observed to fall: Ivuna, Orgueil, Alais, Tonk, and Revelstoke. Several others have been found by Japanese expeditions in Antarctica. They are very fragile and subject to weathering. They do not survive long on the earth's surface after they fall. The table on the following page summarizes (Lodders et al (2009) view of) the current elemental abundances and their uncertainties in the sun and in meteorites.

The Orgueil meteorite is especially popular for abundance analyses. It is a very primitive (and rare) carbonaceous chondrite that fell in France in 1864. Over 13 kg of material was recovered.



http://www.meteoritestudies.com/protected_ORGUEIL.HTM

Katharina Lodders, Astrophysical Journal, 591, 1220 (2003) and 2009 update (will be posted)

Uncertain elements above CNO.

Indium, tungsten, to a lesser extent TI, Au, CI, Rb, Hf

Unseen in the sun

Arsenic, selenium, bromine, technetium (unstable), iodine, cesium, tantalum, rhenium, mercury, bismuth, promethium (unstable)

-			[log N(H)	= A(H) = 12]				
		Solar Photosphere	σ dex	Orgueil CI-chondrite	σ dex	Sun/Meteorite Num/Nmet		
I.	Н	12		8.24	0.04	5710		
2	He	10.925	0.02	1.31		4.1E+09		
3	Li	1.10	0.10	3.28	0.05	0.01		
4	Be	1.38	0.09	1.32	0.03	1.15		
5	в	2.70	0.17	2.81	0.04	0.78		
6	C	8.39	0.04	7.41	0.04	9.46		
7	N	7.86	0.12	6.28	0.06	38.4		
8	0	8.73	0.07	8.42	0.04	2.06		
9	F	4.56	0.30	4.44	0.06	1.32		
10	Ne	8.05	0.10	-1.10		1.4E+09		
11	Na	6.30	0.03	6.29	0.02	1.03		
12	Mg	7.54	0.06	7.55	0.01	0.98		
13	AL	6.47	0.07	6.45	0.01	1.05		
14	Si	7.52	0.06	7.53	0.01	0.97		
15	P	5.46	0.04	5.45	0.04	1.03		
16	s	7.14	0.01	7.17	0.02	0.92		
17	Cl	5.50	0.30	5.25	0.06	1.79		
18	Ar	6.50	0.10	-0.48		9.6E+06		
19	ĸ	5.12	0.03	5.10	0.02	1.06		
20	Ca	6.33	0.07	6.31	0.02	1.04		

Table 4. Elemental abundances in the solar photosphere and in CI-chondrites

22	0.77	Contraction of the second seco	0.00	15752	0.000.000	
21	Sc	3.10	0.10	3.07	0.02	1.07
22	Ti	4.90	0.06	4.93	0.03	0.94
23	V	4.00	0.02	3.98	0.02	1.05
24	Cr	5.64	0.01	5.66	0.01	0.96
25	Mn	5.37	0.05	5.50	0.01	0.75
26	Fe	7.45	0.08	7.47	0.01	0.95
27	Co	4.92	0.08	4.89	0.01	1.08
28	Ni	6.23	0.04	6.22	0.01	1.03
29	Cu	4.21	0.04	4.27	0.04	0.55
30	Zn	4.62	0.15	4.65	0.04	0.94
31	Ga	2.88	0.10	3.10	0.02	0.61
32	Ge	3.58	0.05	3.60	0.04	0.95
33	As			2.32	0.04	
34	Se			3.36	0.03	
35	Br			2.56	0.06	
36	Kr	3.28	0.08	-2.25		3.4E+05
37	Rb	2.60	0.10	2.38	0.03	1.64
38	Sr	2.92	0.05	2.90	0.03	1.04
39	Y	2.21	0.02	2.19	0.04	1.05
40	Zr	2.58	0.02	2.55	0.04	1.07
41	Nb	1.42	0.06	1.43	0.04	0.98

	$[\log N(H) - A(H) - 12]$							
		Solar	σ	Orgueil	e	Sun Meteorite		
		Photosphere	dex	CI-chondrite	dex	N _{mm} /N _{met}		
42	Mo	1.92	0.05	1.96	0.04	0.92		
44	Ru	1.84	0.07	1.78	0.03	1.14		
45	Rh	1.12	0.12	1.08	0.04	1.09		
46	Pd	1.65	0.04	1.67	0.02	0.97		
47	Ag	0.94	0.30	1.22	0.02	0.52		
48	Cd	1.77	0.11	1.73	0.03	1.10		
49	In	<1.50	UL	0.78	0.03	5.21		
50	Sn	2.00	0.30	2.09	0.06	0.81		
51	Sb	1.00	0.30	1.03	0.06	0.94		
52	Te			2.20	0.03			
53	1			1.57	80.0			
54	Xe	2.27	0.08	-1.93		1.6E+04		
55	Cs			1.10	0.02			
56	Ba	2.17	0.07	2.20	0.03	0.94		
57	La	1.14	0.03	1.19	0.02	0.88		
58	Ce	1.61	0.06	1.60	0.02	1.02		
59	Pr	0.76	0.04	0.78	0.03	0.96		
60	Nd	1.45	0.05	1.47	0.02	0.96		
62	Sm	1.00	0.05	0.96	0.02	1.10		
63	Eu	0.52	0.04	0.53	0.02	0.97		
64	Gd	1.11	0.05	1.07	0.02	1.10		

Table 4. Elemental abundances in the solar photosphere and in CI-chondrites

32	1.1	2.0.02	0.00	0.020		1.2.2
65	Tb	0.28	0.10	0.34	0.03	0.88
66	Dy	1.13	0.06	1.15	0.02	0.96
67	Ho	0.51	0.10	0.49	0.03	1.04
68	Er	0.96	0.06	0.94	0.02	1.04
69	Tm	0.14	0.04	0.14	0.03	1.00
70	Yb	0.86	0.10	0.94	0.02	0.83
71	Lu	0.12	0.08	0.11	0.02	1.02
72	Hf	0.88	0.08	0.73	0.02	1.43
73	Ta			-0.14	0.04	
74	W	1.11	0.15	0.67	0.04	2.75
75	Re			0.28	0.04	
76	Os.	1.45	0.11	1.37	0.03	1.21
77	Ir	1.38	0.05	1.34	0.02	1.10
78	Pt	1.74	0.30	1.64	0.03	
79	Au	1.01	0.18	0.82	0.04	1.54
80	Hg			1.19	0.08	
81	TI	0.95	0.20	0.79	0.03	1.43
82	Pb	2.00	0.06	2.05	0.03	0.85
83	Bi			0.67	0.04	
90	Th	< 0.08	UL	0.08	0.03	1.01
92	U	< -0.47	UL	-0.52	0.03	1.11

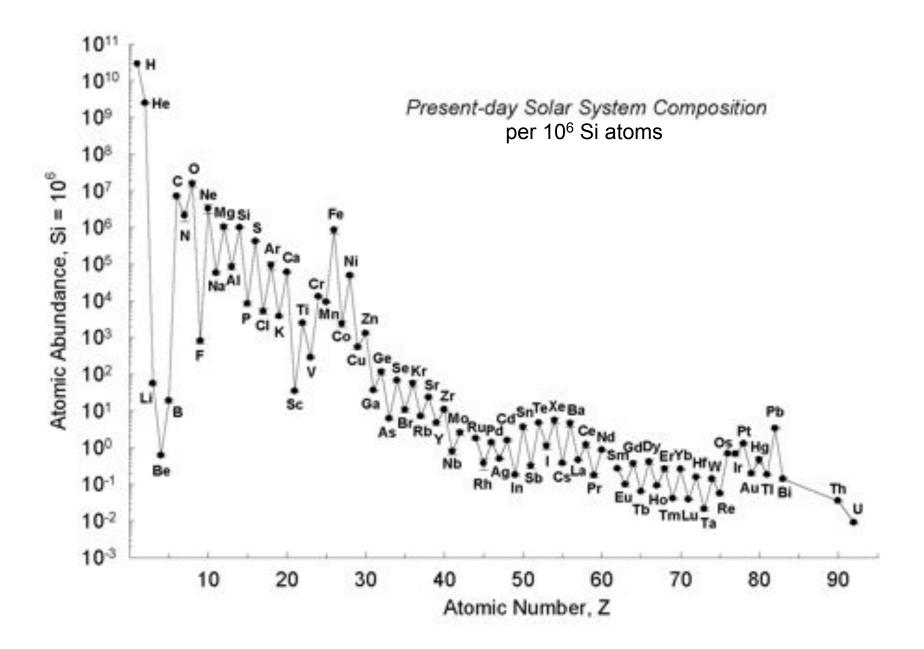
σ - standard deviation in dex: (10^(# is des)-1)< 100 - σ in %;

meteorite data: log N_{EI}+ 1.533 where N_{EL} = abundance relative to 10⁸ Si atoms (Table 1); UL - upper limit;

Last column: Values in italics indicate the 39 elements used for calculating conversion factor.

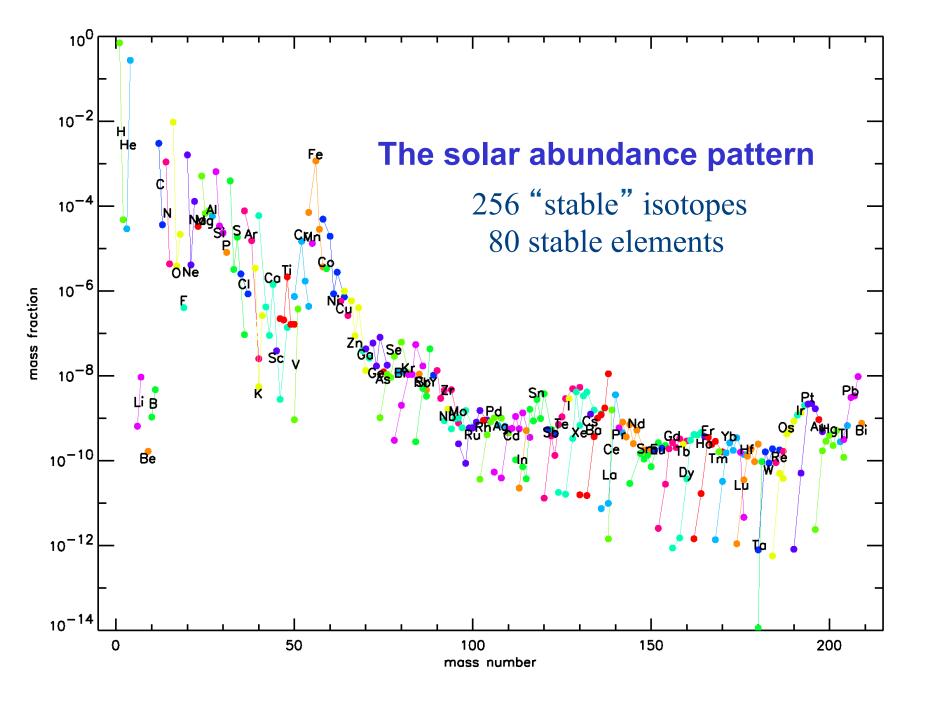
Scanning the table one notes:

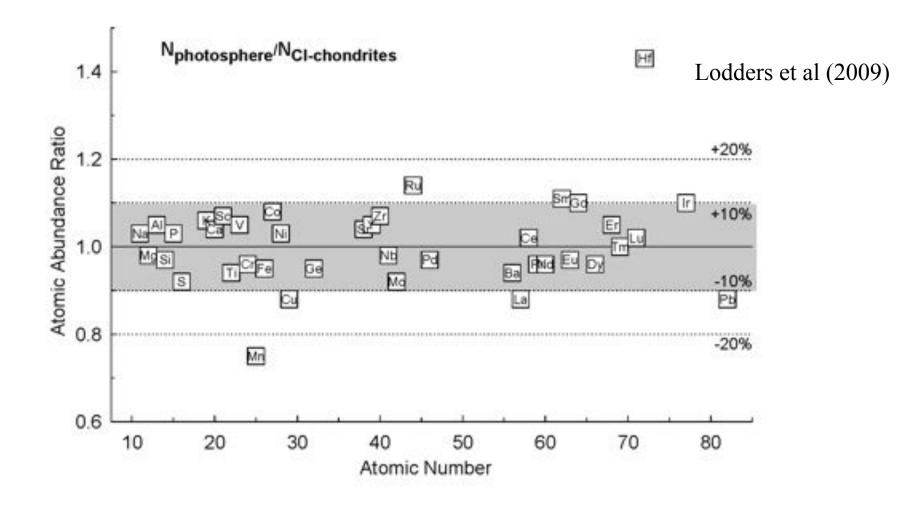
- a) H and H have escaped from the meteorites
- b) Li is depleted in the sun, presumably by nuclear reactions in the convection zone
- c) CNO also seem to be depleted in the meteorites
- d) The noble gases have been lost, Ne, Ar, etc
- e) Agreement is pretty good for the rest where the element has been measured in both the sun and meteorites



Lodders (2009) translated into mass fractions

h1 7.11E-0	1 si28 7.02E-04	ti47 2.34E-07	zn66 6.48E-07
h2 2.75E-0			zn67 9.67E-08
he3 3.42E-0			zn68 4.49E-07
he4 2.73E-0			zn70 1.52E-08
li6 6.90E-1	1		ga69 4.12E-08
			e
li7 9.80E-0			ga71 2.81E-08
be9 1.49E-1			ge70 4.63E-08
b10 1.01E-0	9 s36 7.00E-08	cr52 1.54E-05	ge72 6.20E-08
b11 4.51E-0	09 cl35 3.72E-06	cr53 1.79E-06	ge73 1.75E-08
c12 2.32E-0	03 cl37 1.25E-06	cr54 4.54E-07	ge74 8.28E-08
c13 2.82E-0	os ar36 7.67E-05	mn55 1.37E-05	ge76 1.76E-08
n14 8.05E-0	04 ar38 1.47E-05	fe54 7.27E-05	as75 1.24E-08
n15 3.17E-0	06 ar40 2.42E-08	fe56 1.18E-03	se74 1.20E-09
o16 6.83E-0)3 k39 3.71E-06	fe57 2.78E-05	se76 1.30E-08
o17 2.70E-0)6 k40 5.99E-09	fe58 3.76E-06	se77 1.07E-08
o18 1.54E-0)5 k41 2.81E-07	co59 3.76E-06	se78 3.40E-08
f19 4.15E-0	07 ca40 6.36E-05	5 ni58 5.26E-05	se80 7.27E-08
ne20 1.66E-0	03 ca42 4.45E-07	ni60 2.09E-05	se82 1.31E-08
ne21 4.18E-0	06 ca43 9.52E-08	8 ni61 9.26E-07	br79 1.16E-08
ne22 1.34E-0	04 ca44 1.50E-06	6 ni62 3.00E-06	br81 1.16E-08
na23 3.61E-0	ca46 3.01E-09	ni64 7.89E-07	Etc.
mg24 5.28E-	04 ca48 1.47E-07	cu63 6.40E-07	
mg25 6.97E-		cu65 2.94E-07	
mg26 7.97E-			





Off scale In, W, TI, Au, CI, Rb

Abundances outside the solar neighborhood?

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H. Schatz
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Abundances outside the solar system can be determined through:

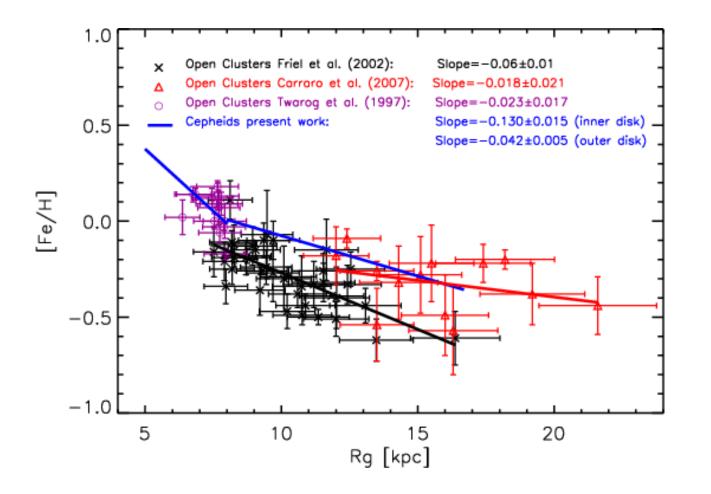
- Stellar absorption spectra of other stars than the sun
- Interstellar absorption spectra
- Emission lines, H II regions
- Emission lines from Nebulae (Supernova remnants, Planetary nebulae, ...)
- γ -ray detection from the decay of radioactive nuclei
- Cosmic Rays
- Presolar grains in meteorites

	Present	& G stars				B dwarfs			Orion nebula				
	-day solar system	solar	metalli	city	age	< 1 Ga	8						
EL	this work	A	σ_{ebd}	σ_*	A	σ_{*}	ref	A	σ.	ref.	A	σ_{abd}	nij
He	10.93						101	11.02	0.05	3	10.9 9	0.01	10
C	8.39	8.37	0.06	0.11	8,39	0.11	2	8.32	0.10	4	8,52	0.05	10
N	7.86							7.73	0.28	5	7.73	0.09	10
0	8.73	8.75		0.07	8.77	0.13	1	8.63	0.18	4	8.73	0.09	10
Ne	8.05							7.97	0.07	6	8.05	0.07	10
Na	6.29	6.30	0.03	0.16	6.27	0.10	1						
Mg	7.54	7.63	0.06	0.32	7.64	0.21	1	7.59	0.15	7			
AL	6.46	6.52	0.05	0.24	6.54	0.22	1	6.24	0.14	5			
Si	7.53	7.60	0.05	0.28	7.61	0.23	1	7.50	0.21	5			
s	7.16	7.17	0.16		7.29	0.10		7.22	0.10	4	7.22	0.04	10
Ar	6.50							6.63	0.06	8	6.62	0.05	10
Ca	6.31	6.42	0.03	0.37	6.48	0.39	1						
Ti	4.93	4.92	0.03	0.11	4.94	0.14	1						
Cr	5.65	5.66	0.02	0.13	5.73	0.28	1						
Fe	7.46	7.55	0.06	0.12	7.61	0.25	1	7.46	0.08	9			
Ni	6.22	6.22	0.02	0.09	6.25	0.07	1						
Zn	4.65	4.53	0.06	0.27	4.54	0.13	1						
Z	0.0141	0.0141			0.0148			0.0119					

Table 11. Average abundances (A) of main sequence F and G stars with close to solar metallicity ([∆[Fe/H]]<0.05) and of young stars (age −1 Ga) from the solar neighborhood, of main sequence B stars from a ±2 kpc wide ring around the solar circle, and abundances of the Orion nebula

 σ_{abd} - accuracy of the individual abundance determinations from stellar spectra, σ_{s} - scattering of the stellar abundances of the corresponding group of stars around the mean; Z - metallicity estimated from these abundances. Sun: Tables 6,7.

Data sources: (1)[05B3], (2)[06B], (3)[04L2], (4)[04D], (5)[00R], (6)[08M2], (7)[05L2], (8)[08L4], (9)[94C2], (10)[04E]

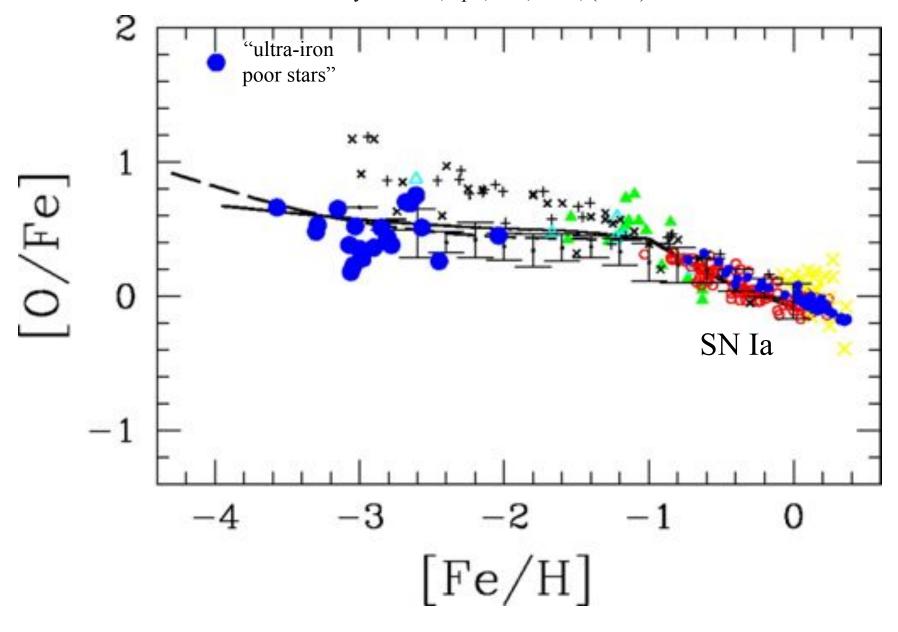


but see also Najarro et al (ApJ, 691, 1816 (2009)) who find solar iron near the Galactic center.

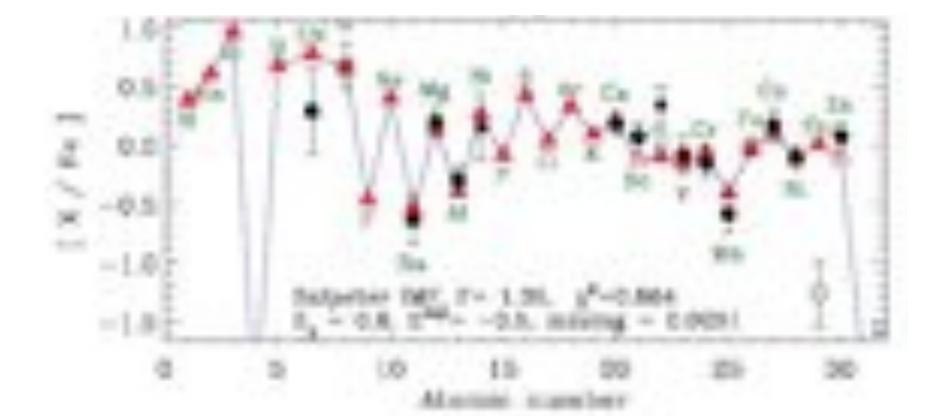
From Pedicelli et al. (A&A, 504, 81, (2009)) studied abundances in Cepheid variables. Tabulated data from others for open clusters.

For entire region 5 - 17 kpc, Fe gradient is -0.051+-0.004 dex/kpc but it is ~ 3 times steeper in the inner galaxy. Spans a factor of 3 in Fe abundance.

Variation with metallicity Kobayashi et al, *ApJ*, **653**, 1145, (2006)



Integrated yield of 126 masses 11 - 100 M_{\odot} (1200 SN models), with Z= 0, Heger and Woosley (2008, ApJ 2010) compared with low Z observations by Lai et al (*ApJ*, 681, 1524, (2008)). Odd-even effect due to sensitivity of neutron excess to metallicity and secondary nature of the s-process.



28 metal poor stars in the Milky Way Galaxy -4 < [Fe/H] < -2; 13 are < -.26