PHASES OF THE INTERSTELLAR MEDIUM

Component	Fractional volume	Scale Height (pc)	Temperature	Density	State of Hydrogen	Observational Technique
Molecular Clouds	< 1%	70	10 - 20	10 ² - 10 ⁶	H ₂	Radio and infrared (molecules)
Cold Neutral Medium (CNM)	1 - 5%	100 - 300	50 - 100	20 - 50	HI	21 cm
Warm Neutral Medium (WNM)	10 - 20%	300 - 400	5000- 8000	0.2 - 0.5	ні	21 cm
Warm Ionized Medium (WIM)	20 - 50%	1000	6000 - 12000	0.2 - 0.5	нп	$^{\rm H}_{lpha}$ pulsar (n $_{ m e}$)
H II Regions	<1%	70	8000	10² - 10⁴	нш	н _а
Coronal Gas (Hot Ionized Medium (HIM)	30 - 70%	1000 - 3000	10 ⁶ = 10 ⁷	10 ⁻⁴ - 10 ⁻²	H II metals also ionized	x-ray ultraviolet

Star Formation and Pressure

http://apod.nasa.gov/apod/astropix.html

In which of these components can star formation take place?

A necessary condition is a region of gas that has greater gravitational binding energy than internal energy. (The force pulling the region together must be greater than the pressure pushing it apart.)

Since internal energy increases with the amount of mass that is present while binding energy increases as M^2 , there is a critical mass that is bound.

$$\Omega \approx \frac{3}{5} \frac{GM^2}{R} \approx (\text{Number of particles}) \left(\frac{3}{2} kT\right)$$

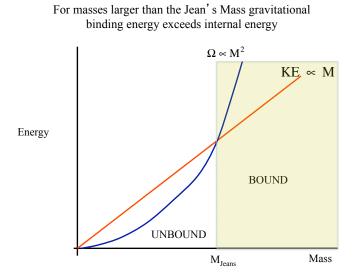
$$Ignore factor of 2 in the Virial Theorem. The clouds we are envisioning have not reached equilibrium.
$$\approx \frac{M}{m_H} \frac{3}{2} kT \quad (\text{if made of pure hydrogen})$$

$$= N_A M \frac{3}{2} kT \quad (N_A \text{ is Avogadro's Number, 6.02 } \times 10^{23})$$
This can be solved for the "Lean's Mass" M$$

This can be solved for the "Jean's Mass", M_J

$$\frac{\frac{3}{5}\frac{GM_j^2}{R}}{M_J} = \frac{\frac{3}{2}N_AM_JkT}{M_J}$$
$$\frac{M_J}{M_J} = \frac{\frac{5N_AkTR}{2G}}{M_J}$$

Clouds of gas with radius R and temperature T that have a mass bigger than this are unstable to gravitational collapse



It is easier to measure densities and temperatures rather than radii, so the equation on the previous page can be transformed using

$$R = \left(\frac{3M}{4\pi\rho}\right)^{1/3} \qquad \text{assume sphere, constant density} \quad M = \frac{4}{3}\pi R^3 \rho$$
previous page $M_J = \frac{5N_A kTR}{2G} = \frac{5N_A kT}{2G} \left(\frac{3M_J}{4\pi\rho}\right)^{1/3}$
 $M_J^{2/3} = \frac{5N_A k}{2G} \left(\frac{3}{4\pi}\right)^{1/3} \left(\frac{T^3}{\rho}\right)^{1/3}$
 $M_J = \left(\frac{5N_A k}{2G}\right)^{3/2} \left(\frac{3}{4\pi}\right)^{1/2} \left(\frac{T^3}{\rho}\right)^{1/2}$
 $= 8.5 \times 10^{22} \text{ gm } \left(\frac{T^{3/2}}{\rho^{1/2}}\right) = 4.2 \times 10^{-11} \left(\frac{T^{3/2}}{\rho^{1/2}}\right) M_{\odot}$

PHASES OF THE INTERSTELLAR MEDIUM

It is more frequent that one finds the density in this context
expressed as atoms/cm ^{3} rather than gm/cm ^{3} .
If $n = \rho N_A$ (actually true only for H I), then

$$M_{J} = 8.5 \times 10^{22} \frac{T^{3/2} N_{A}^{1/2}}{n^{1/2}} \text{ gm}$$
$$M_{J} = 34 \frac{T^{3/2}}{n^{1/2}} M_{\odot}$$

where n is the density in atoms cm⁻³.

By this criterion, only molecular clouds and possibly portions of the coldest neutral medium (depending on mass) are unstable to collapse.

Component	Fractional volume	Scale Height (pc)	Temperature Density		State of Hydrogen	Observational Technique
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Example: Molecular cloud; T = 20 K, n = 10⁴ atoms cm⁻³

$$M_J = 34 \frac{T^{3/2}}{n^{1/2}}$$

= 34 $\frac{(20)^{3/2}}{(10^4)^{1/2}} = 34 \frac{89.4}{100}$
= 30 M_{\overline{o}}}

Any cloud with this temperature and density and a mass over 30 solar masses is unstable to collapse

How long does the collapse take?

$$v_{esc} = \sqrt{\frac{2GM}{R}} \qquad \tau_{ff} \approx \frac{R}{v_{esc}} = \sqrt{\frac{R^3}{2GM}}$$

but, ρ , the density, is given by
$$\rho = \frac{3M}{4\pi R^3} \Rightarrow \frac{R^3}{M} = \frac{3}{4\pi\rho}$$

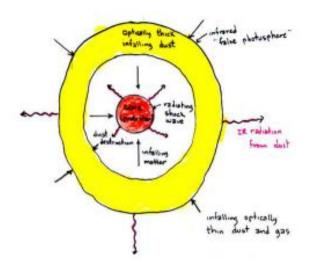
so,
$$\tau_{ff} \approx \sqrt{\frac{3}{8\pi G\rho}} \approx 1000 \operatorname{seconds}/\sqrt{\rho} \qquad Denser regions collapse faster$$

but $\rho \approx n/N_A$, so

$\tau_{\rm ff} \approx 10$ million years/ \sqrt{n}

where n is the number of atoms per cubic cm.

1 million years if n = 10⁴ atoms/cm³

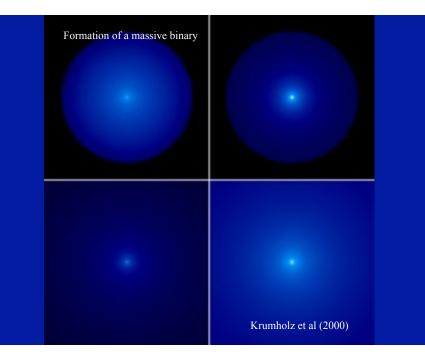


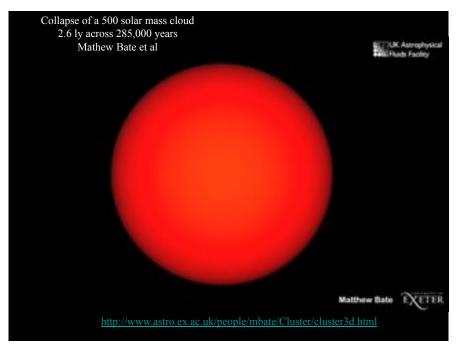
Star formation is inefficient. Even of the collapsing gas only 10 - 20 % of the gas ends up in the star, and overall an even smaller fraction of the cloud collapses to protostars.

Fragmentation

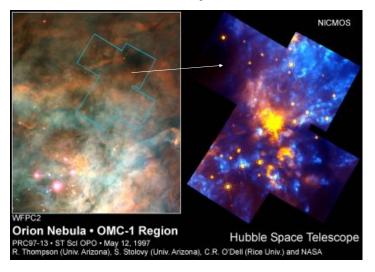


Complications: Rotation Magnetic fields





Power of observing in the infrared



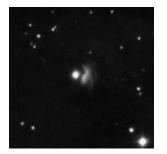


LH 95 A Stellar Nursery in the Large Magellanic Cloud (HST)



The star formation region N11B in the LMC taken by WFPC2 on the NASA/ESA Hubble Space Telescope

T-Tauri Stars

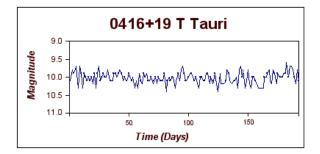


T-Tauri – in Taurus close to the Pleaides

T-Tauri discovered by John Hind in 1852 as a 10th magnitude star. A faint nebula was subsequently discovered nearby ("Hind' s nebula"). Both the star and nebula had variable brightness. The nebula was a "reflection" nebula, shining from the reflected light of T-Tauri.

By 1861 the nebula disappeared from view and by 1890 T-Tauri itself had faded to 14th magnitude, about the limit of telescopes then. A faint nebula at the site of T-Tauri itself was observed at that time,

Over the next 10 - 20 years, T-Tauri brightened back to 10^{th} magnitude and its local nebula became invisible against the glare. T-Tauri has remained at about 10^{th} magnitude since (but varies).



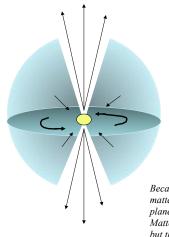


T-Tauri - about 400 ly away at the edge of a molecular cloud. FOV here is 4 ly at the distance of T-Tauri <u>http://apod.nasa.gov/apod/ap071213.htm</u>

T-Tauri Stars

- Short lived phase in life of stars under 2 solar masses. Heavier stars evolve quicker and start burning by the time the star is visible. Above 2 solar masses the objects evolve rapidly and are rarely seen - "Herbig Ae and Be stars".
- Accretion disks and jets are common features
- Emission and absorption lines
- Powered by gravitational contraction, not nuclear burning
- May be forming planetary systems
- High lithium abundance
- Embedded in dense, dusty regions
- Can be highly variable

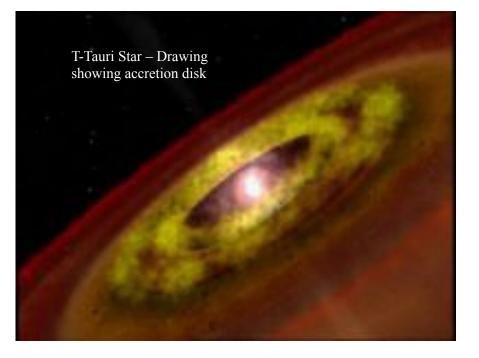
When the star first becomes visible it may still be surrounded by the gas and dust from which it formed. Often jets are seen.

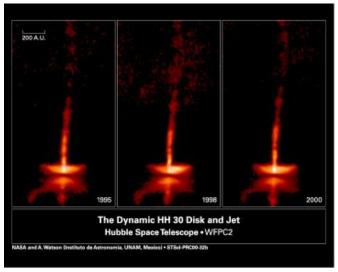


Because of rotational support matter hangs up in the equatorial plane forming an "accretion disk". Matter first rains down on the poles, but then later reverses direction in a strong collimated outflow called a "jet".

Protoplanetary disks orbit over half of T-Tauri stars. This shows 5 such stars in the constellation Orion. Picture using HST - field is about 0.14 ly across <u>http://en.wikipedia.org/wiki/T_Tauri_star</u>

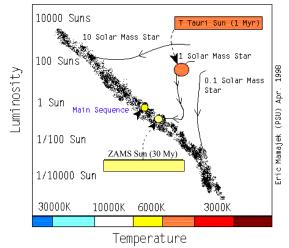






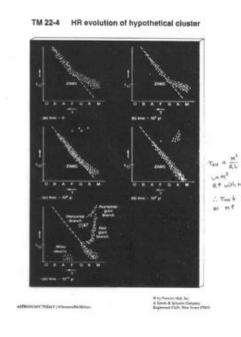
30" west of the brightest point in Hind's nebula is a disk-jet system, Herbig-Haro 30. At the center of this is probably another T-Tauri like star.

Hertzsprung-Russell Diagram



Protostars start off with very large radii because they begin as contracting clouds of gas. They additionally have high luminosities because they are fully convective (more about this later) and able to transport the energy released by gravitational contraction efficiently to their surface.

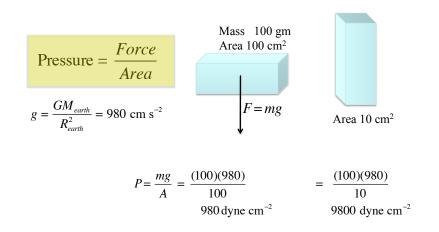
Most of the time is spent close to the main sequence.

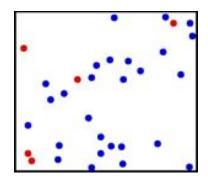


x.

Stellar Interiors - Kinds of Pressure

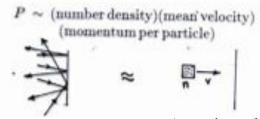
Pressure is force per unit area

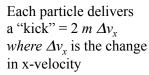




http://intro.chem.okstate.edu/1314f00/laboratory/glp.htm

Qualitatively





Approximate this with a group of particles n in one cubic cm all moving to the right with $v_x = v$. The particle flux then = n times v and each particle imparts momentum of roughly mv

 $P \approx (mv)(nv) = n m v^2$

For a gas, pressure is defined as

$$P = \frac{1}{3} \int \frac{dn}{dp} v \, p \, dp$$

where (dn/dp) * dp is the number density (per cm³) of particles having momentum between p and p+dp, and v is their speed. The 1/3 is from an integral over angles.

Pressure thus has units

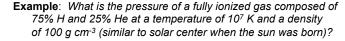
1	ст	gm cm	_ gm cm _	dyne
$\overline{cm^3}$	S	S	$-\frac{1}{cm^2 s^2}$	cm^2

Approximation:

suppose p (and therefore v) is constant and Then

$$\frac{1}{3}\int\frac{dn}{dp}vp\,dp\approx\frac{1}{3}vp\int\frac{dn}{dp}dp=\frac{1}{3}vpn$$

where n is the total number density of particles per cubic cm. When one integrates over a distribution of momenta, the 1/3 out front changes.



- In each cm³ of gas there are 75 gm of hydrogen and 25 gram of helium.
- In 75 gm of hydrogen there are

$$\frac{75 \text{ gm}}{m_{proton}} = 75 \text{ N}_A = 75 \times 6.02 \times 10^{23} = 4.52 \times 10^{25} \text{ protons}$$

In 25 gram of helium there are (the helium nucleus weighs approximately 4 m_{proton})

$$\frac{25 \text{ gm}}{4m_{proton}} = 6.25 \text{ N}_A = 6.25 \times 6.02 \times 10^{23} = 3.76 \times 10^{24} \text{ helium nuclei}$$

In addition, each hydrogen contributes to the ionized plasma 1 electron and each helium contributes two

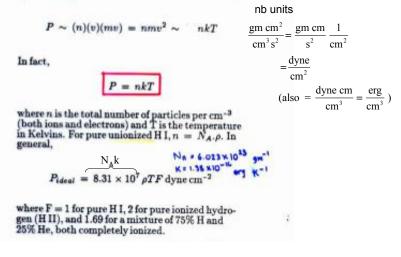
$$N = 4.52 \times 10^{25} + 4.52 \times 10^{25} + 3.76 \times 10^{24} + 2(3.76 \times 10^{24})$$

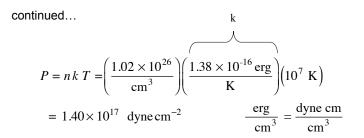
= 1.02 × 10²⁶ particles per cm³

IDEAL GAS PRESSURE

• Due to thermal motion of particles such as electrons, atoms, and ions. Particles are assumed to only interact during their collisions.

Qualitatively

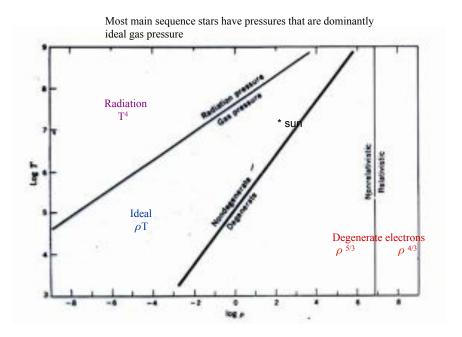




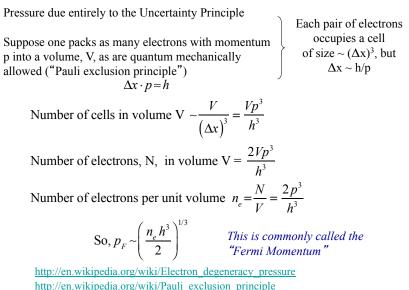
But it is easier and just as accurate to use the formula

$$P = 8.31 \times 10^{7} \rho T F$$

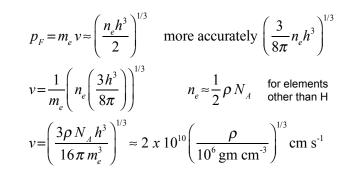
= $(8.31 \times 10^{7})(100)(10^{7})(1.69)$
= 1.40×10^{17} dyne cm⁻²



DEGENERACY PRESSURE



As n_e goes up the speed of each electron rises



At around 10^7 gm cm⁻³ the electrons will move close to the speed of light.

DEGENERACY PRESSURE

Now the pressure

$$P \sim n_e p_F v = n_e p_F \frac{mv}{m} = \frac{n_e p_F^2}{m}$$
$$\sim \frac{n_e}{m} \left(\frac{n_e h^3}{2}\right)^{2/3}$$
$$P_{deg} \sim \frac{h^2 n_e^{5/3}}{2^{2/3} m}$$

The contribution of electrons, when present, is much larger than from neutrons or protons because of the 1/m

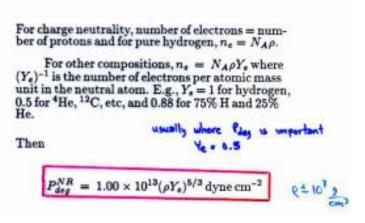
"*non* – *relativistic*" degeneracy pressure = P_{NRD}

$$P_{NRD} \sim \frac{n_e p_F^2}{m_e} = \frac{n_e \left(\frac{n_e h^3}{2}\right)^{2/3}}{m}$$
$$= \frac{h^2}{2^{2/3} m_e} n_e^{5/3}$$

A more accurate calculation gives

$$\mathbf{P}_{NRD} = \frac{1}{20} \left(\frac{3}{\pi}\right)^{2/3} \frac{h^2}{m_e} n_e^{5/3}$$

http://scienceworld.wolfram.com/physics/ElectronDegeneracyPressure.html



Note that the degeneracy pressure depends only on the density and not on the temperature

RELATIVISTIC DEGENERACY PRESSURE

The above remains true only so long as v of the electrons remains << c. As v approaches c

$$P_{deg} \sim (n_e)(c)(p) \sim n_e^{4/3} \qquad (p \times n_e^{4/3})$$

and in fact

$$P_{deg}^R = 1.24 \times 10^{15} (\rho Y_e)^{4/3} \,\mathrm{dyne} \,\mathrm{cm}^{-2}$$
 $\chi \gtrsim 10^3 \,\mathrm{g/cm^3}$

Once the electrons move near the speed of light, the pressure does not increase as rapidly with density as before.

RADIATION PRESSURE

Because electromagnetic radiation (light) carries energy, it also carries momentum. In general, for non-relativistic motion (v << c), momentum = (2)(kinetic energy)/(velocity), e.g., $2(1/2mv^2)/v = mv = p$. For photons the relation is a little different.

 $p=E/c=h\nu/c$

So to get momentum flux just divide energy flux by c.

THE "PRESSURE" OF SUNLIGHT

From the sun, at the earth's orbit (1AU), we receive a flux of radiation

$$\phi = \frac{L}{4\pi d^2} = \frac{L_{\odot}}{4\pi (AU)^2}$$

$$= 1.37 \times 10^{6} \text{ erg cm}^{-2} \text{ s}^{-1}$$

This corresponds to a momentum flux, or pressure

$$P = \frac{\phi}{c} = \frac{(1.37 \times 10^6)}{(3.00 \times 10^{10})} \frac{\text{erg}}{\text{cm}^2 \text{ s}} \frac{(\text{s})}{(\text{cm})}$$
$$= 4.57 \times 10^{-5} \frac{\text{dyne}}{\text{cm}^2} \text{ since (dyne)(cm)} = \text{erg}$$

(1 square meter (10^4 cm²) would be accelerated 0.46 cm/s² if it weighed 1 gm; would reach c in about 1000 years)



1997 Comet Hale Bop

The pressure is then

$\begin{array}{l} P &\sim (\mathrm{number\,flux})(\mathrm{momentum\,per\,photon}) \\ &= \left(\frac{\mathrm{E\,flux}}{\mathrm{energy\,per\,photon}} \right) (\mathrm{momentum\,per\,photon}) \\ &= \left(\frac{\sigma T^4}{h\nu} \right) (\frac{h\nu}{c}) \\ &= \frac{\sigma}{-} T^4 \end{array}$

In fact the correct expression is

$$P_{rad} = \frac{4\sigma}{3c}T^4 = \frac{1}{3}aT^4$$

where $a = 7.56 \times 10^{-15} \,\text{dyne cm}^{-2} \,(\text{K})^{-4}$. = $\frac{4\sigma}{c}$

IN SUMMARY

There are 3 kinds of pressure:

- Ideal gas pressure ($\propto \rho$ and T)
- Radiation pressure ($\propto T^4$)
- Degeneracy pressure $(\propto \rho^n)$ $\frac{4}{5} < \pi < \frac{5}{5}$

The total pressure is given by

$$P_{tot} = P_{ion} + P_{rad} + P_e$$

Except in neutron stars, P_{ion} is ideal. P_e can be quite complex (semidegenerate, semirelativistic) which can lead to some difficult math (Fermi integrals) which we will not consider.

