

## Lecture 19

# Black Holes and Gamma-Ray Bursts

<http://apod.nasa.gov/apod/astropix.html>

### Some Properties of Black Holes

- Entirely defined by their mass, rotation rate, and charge. All memory of how the hole was made is lost. Almost like an elementary particle. “Black holes have no hair” (Wheeler, Israel, Hawking, etc.)
- Believed that all the mass is concentrated at the center in a small quantum-mechanical “singularity”
- The effective density of stellar mass black holes, as defined by their event horizons is very high, but there are supermassive black hole in active galactic nuclei with “average densities” no greater than water. they are just very big (this ignores the central concentration in a singularity though.) The average density matters to tidal forces.
- The gravitational field of a black hole close to the event horizon is complicated, but by the time you are several Schwarzschild radii away, it is indistinguishable from that of an ordinary star. Of course there’s no light.

Black holes in nature – end points of stellar evolution

- In our galaxy alone, theory suggests 50 million black holes (2 SN per century for  $10^{10}$  years  $\frac{1}{4}$  of which make black holes)
- Most massive galaxies have massive black holes at their centers ( $10^9$  galaxies)
- Dozens of black hole binary x-ray sources per galaxy – at least
- One gravitational radiation detection so far

They are out there...

Kinds of black holes:

	Class	Mass (solar masses)	Size
AGN	Supermassive	$\sim 10^5 - 10^{10}$	0.001 - 10 AU
?	Intermediate	$\sim 1000$	$\sim R_{\text{earth}}$
XRBin	Stellar	$\sim 10$	$\sim 30$ km
?	Primordial	Up to $\sim$ Moon	Up to $\sim 0.1$ mm

$$R_s = \left( \frac{2GM}{c^2} \right) = 2.96 \text{ km} \left( \frac{M}{M_{\odot}} \right)$$

### Event Horizon

$$R_s = \left( \frac{2GM}{c^2} \right) = 2.96 \text{ km} \left( \frac{M}{M_\odot} \right)$$

Note that this “size” is proportional to M.  
 Very massive black holes - the maximum is  $4 \times 10^{10}$  solar masses have been inferred to exist in some Galactic centers. These black holes would be  $\sim 10$  AU in size.

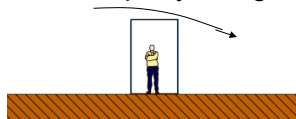
Note that the “average density” of a black hole scales as  $M^{-2}$ .

$$\rho = \frac{M}{(4/3)\pi R^3} \propto \frac{M}{M^3} \propto \frac{1}{M^2}$$

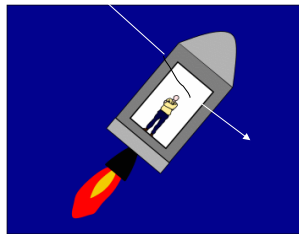
$$= 1.8 \times 10^{16} \left( \frac{M_\odot}{M} \right)^2 \text{ g cm}^{-3}$$

### **EQUIVALENCE PRINCIPLE**

(anything regardless of mass accelerates equally in a gravitational field)



equals



**Gravity “bends” light**

some deflection just because you are moving but even more if you are accelerating

### **Tidal Force**

$$\Delta F_{\text{tidal}} = \frac{dF_{\text{grav}}}{dr} \times d = \frac{2GMm}{r^3} d$$

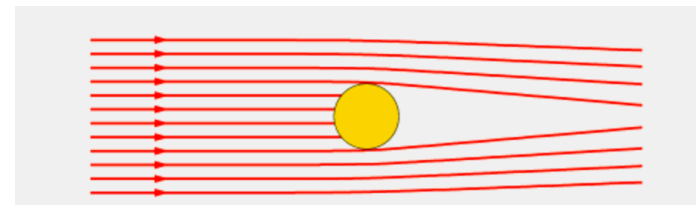
$$= \left( \frac{GMm}{r^2} \right) \left( \frac{2d}{r} \right) = \text{your weight} \times \frac{2d}{r} \propto \frac{1}{M^2}$$

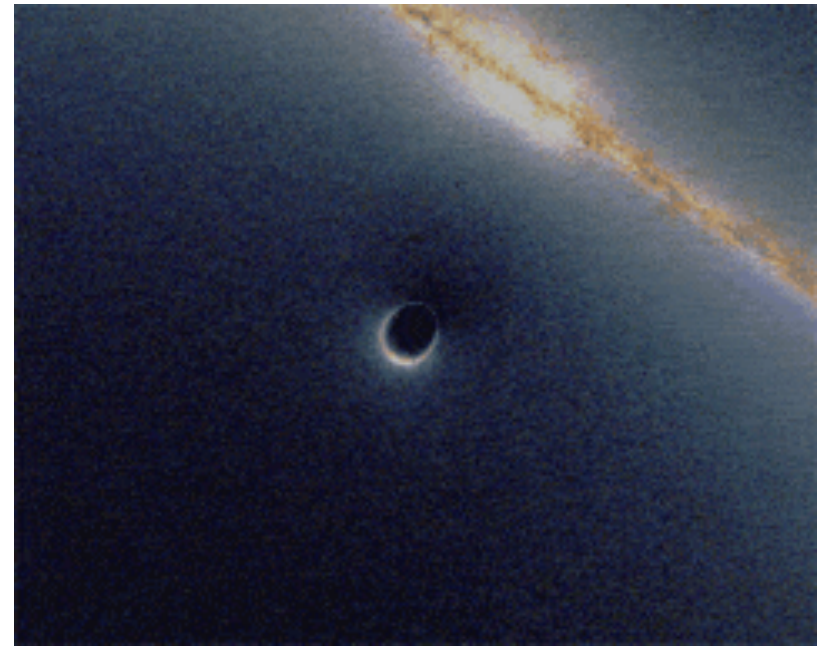
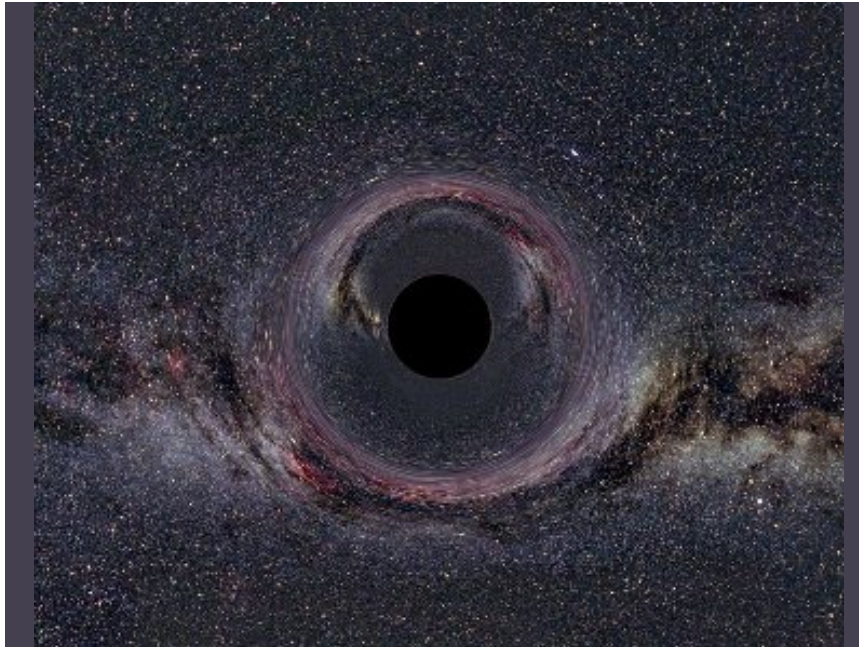
The tidal force would be reduced by  $1/M^2$ .

A rocket crossing the event horizon of a 100,000 solar mass black hole might just survive and black holes of  $10^{10}$  solar masses are known in the nuclei of active galaxies

<http://en.wikipedia.org/wiki/Spaghettification>

But once inside the black hole the tidal forces would continue to grow even in a supermassive black hole.





**Gravitational time dilation.**

An outcome of the equivalence principle, without derivation

$$t_{remote} = t_{near\ BH} / \sqrt{1 - r_s / r} \quad r_s = \frac{2GM}{c^2}$$

$$r > r_s$$

<http://www.upscale.utoronto.ca/PVB/Harrison/GenRel/TimeDilation.html>

has been measured on Earth with atomic clocks ~ nanoseconds

Circumference of orbit	Time experienced by outside observer per orbiter day
20,000 km	1.41 days
15,000 km	1.73 days
12,000 km	2.44 days
11,000	3.32
10,500	4.50
10,250	6.4
10,050	14.18
10,025	20.02
10,005	44.73
10,000.75	115.47
10,000.50	141.42
10,000.25	200.00
10,000.125	282.84
10,000.005	447.21
10,000.001	3162.28 days

For a black hole with circumference 10,000 km

About 500 solar masses

If you could go inside what would you see? **I don't know**

According to one view, mostly vacuum. The collapse continues to a "point" at the center. The event horizon is just a cloak that prohibits (outwards) communication with the universe. Roger Penrose (1960's) proved a theorem that all black holes have "singularities". Quantum mechanics was neglected.

The matter piles up at the center and the density classically can approach infinity. But quantum mechanics does not allow an infinite mass energy density to exist at a geometrical point.

At this time there is no agreed upon theory that unites the basics of quantum mechanics and general relativity.

However, combinations of the fundamental constants, G, c, and h set some scales for quantum gravitational effects.

$$\text{Planck mass} \quad \left(\frac{c\hbar}{G}\right)^{1/2} = 2.2 \times 10^{-5} \text{ gm}$$

$$\text{Planck time} \quad \left(\frac{G\hbar}{c^5}\right)^{1/2} = 5.4 \times 10^{-44} \text{ sec} \quad \hbar = \frac{h}{2\pi}$$

$$\text{Planck length} \quad \left(\frac{G\hbar}{c^3}\right)^{1/2} = 1.6 \times 10^{-33} \text{ cm} = \frac{G (\text{Planck mass})}{c^2} \\ \approx R_s \text{ for the Planck mass}$$

$$\text{Planck density} = \left(\frac{\text{Planck mass}}{(\text{Planck length})^3}\right) = 5 \times 10^{93} \text{ gm/cm}^3$$

$$c = 2.99 \times 10^{10} \text{ cm s}^{-1}$$

$$G = 6.67 \times 10^{-8} \text{ dyne cm}^2 \text{ gm}^{-2}$$

$$\hbar = 1.05 \times 10^{-27} \text{ erg s}$$

$$\frac{\hbar c}{G} = \frac{(2.99 \times 10^{10})(1.05 \times 10^{-27})}{(6.67 \times 10^{-8})} \frac{\text{cm}}{\text{s}} \frac{\text{gm}^2}{\text{dyne cm}^2} \text{ erg s}$$

$$= 4.70 \times 10^{-10} \frac{\text{gm}^2 \text{ erg}}{\text{dyne cm}} = 4.70 \times 10^{-10} \text{ gm}^2$$

$$\left(\frac{\hbar c}{G}\right)^{1/2} = 2.17 \times 10^{-5} \text{ gm}$$

## Uncertainty Principle

(Uncertainty in energy)(Uncertainty in time)  $\sim \hbar$

(Planck Mass  $\times c^2$ )(Planck time)  $\sim \hbar$

$$\left(\frac{c\hbar}{G}\right)^{1/2} c^2 \left(\frac{G\hbar}{c^5}\right)^{1/2} = \hbar$$

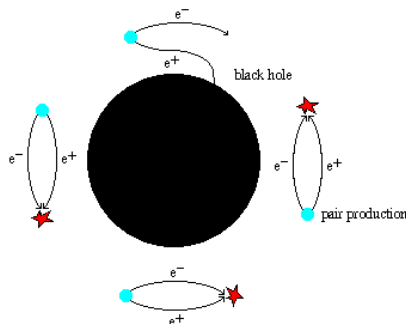
Space time viewed on a scale of the Planck length can be expected to look very unlike the space-time of common experience:

- Curled up dimensions?
- Quantum foam?
- Time undefined

*Can the constants G, c, and h be assumed to stay constant across so many decades of extrapolation?*

### Hawking Radiation

the strong gravitational field around a black hole causes pair production



if a pair is produced outside the event horizon, then one member will fall back into the black hole, but the other member will escape and the black hole loses mass

the amount of mass lost is greater for small black holes, therefore quantum sized black holes disintegrate in very short timescales

Is every black hole that forms the birth of a new universe? **I don't know**

e.g. <http://phys.org/news/2012-05-black-hole-universe-physicist-solution.html>

The singularity inside a black hole resembles that at the beginning of the universe, but it is very difficult to do experiments. Is this science?

The next 50 years is going to be very interesting in this field – maybe.

### Hawking Penrose radiation

$$\tau \sim \frac{5120\pi G^2 M^3}{\hbar c^4} = 8.4 \times 10^{-17} \left(\frac{M}{\text{kg}}\right)^3 \text{ sec}$$

$2 \times 10^{67}$  years for a 1 solar mass BH

but a Hubble time for  $10^{14}$  gm

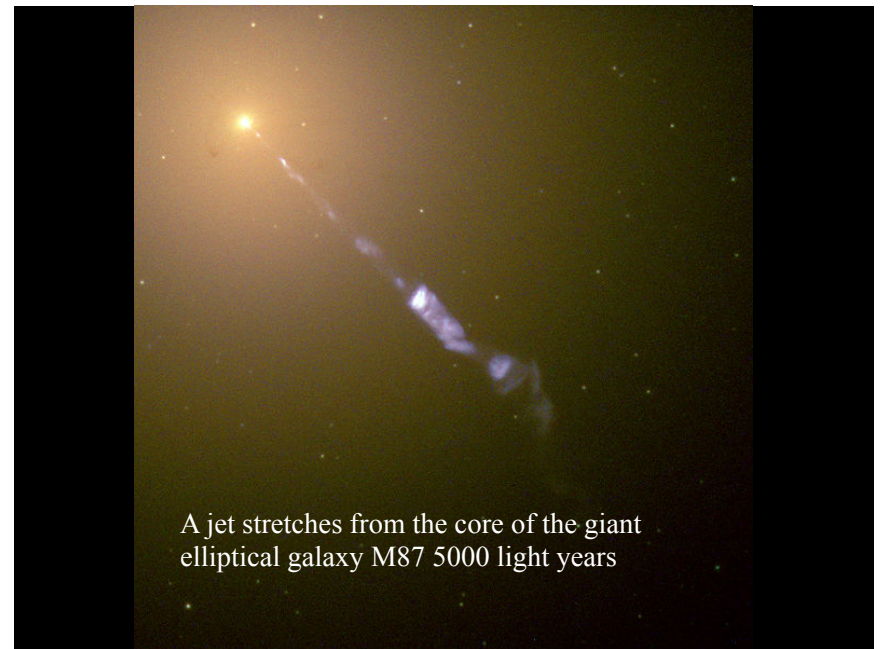
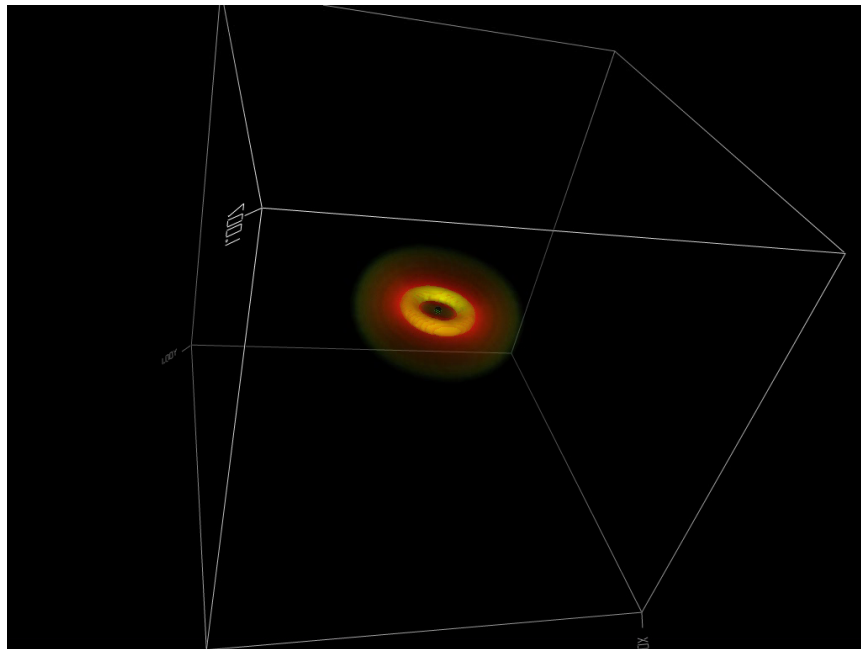
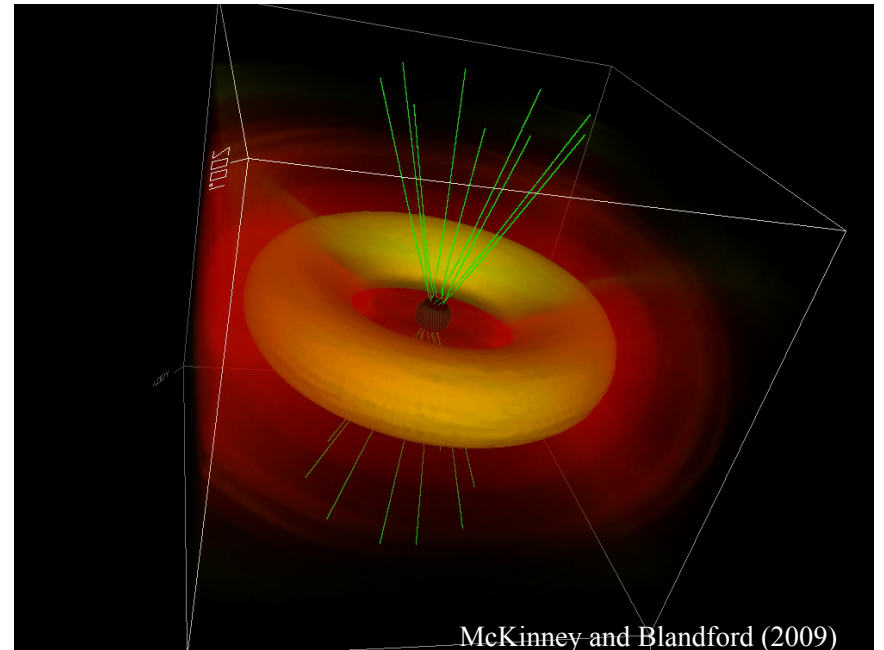
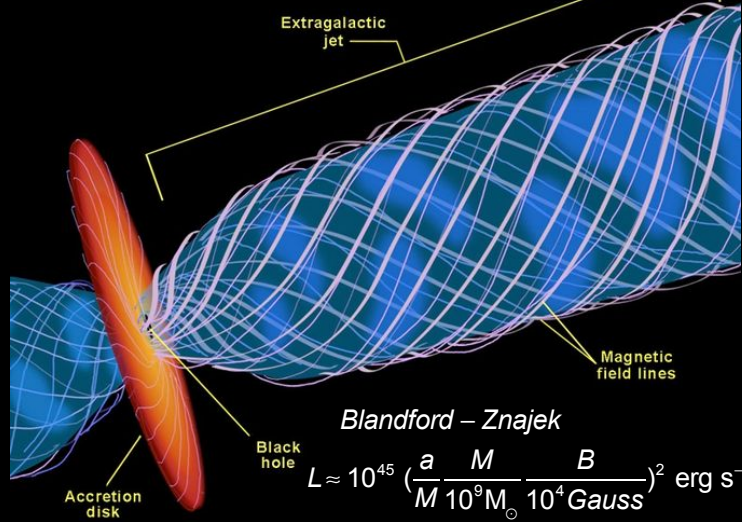
[https://en.wikipedia.org/wiki/Hawking\\_radiation](https://en.wikipedia.org/wiki/Hawking_radiation)

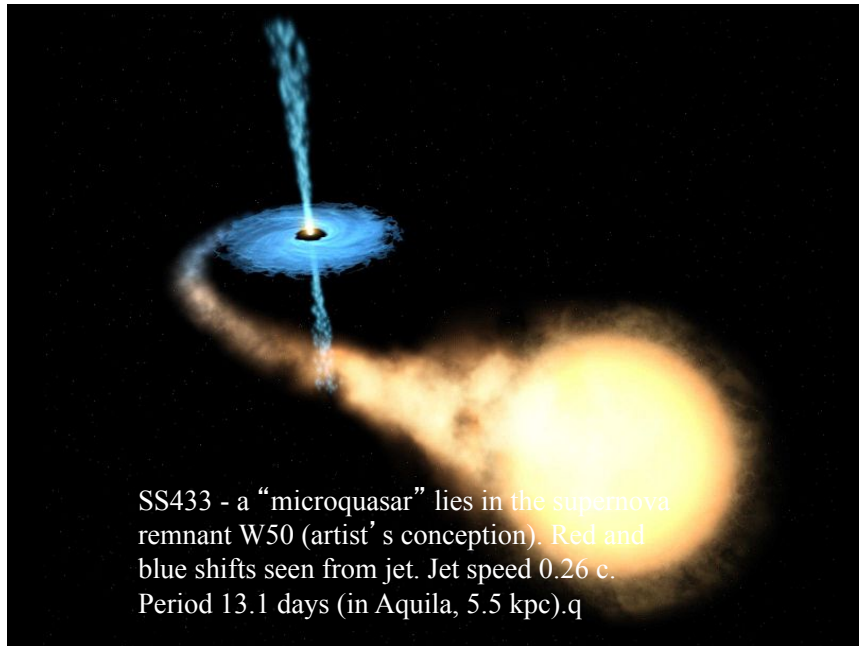
$$T_{\infty} = \frac{\hbar c^3}{8\pi G M k_B} \left( \approx \frac{1.227 \times 10^{23} \text{ kg}}{M} \text{ K} = 6.169 \times 10^{-8} \text{ K} \times \frac{M_{\odot}}{M} \right)$$

$$L = \frac{\hbar c^6}{15360\pi G^2 M^2} = 9 \times 10^{-22} \left(\frac{M_{\odot}}{M}\right) \text{ erg s}^{-1}$$

ignoring the microwave background radiation!

## Formation of extragalactic jets from black hole accretion disk



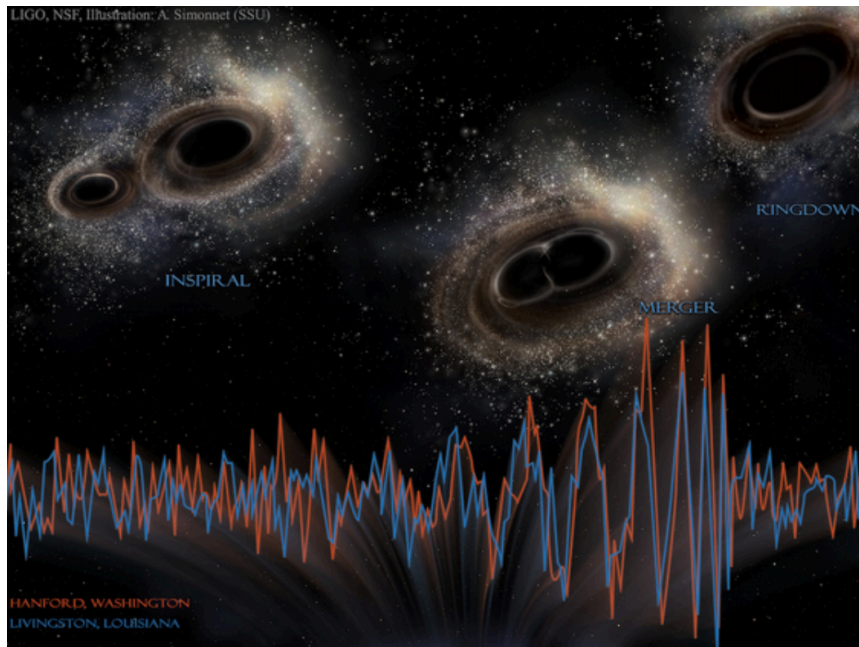
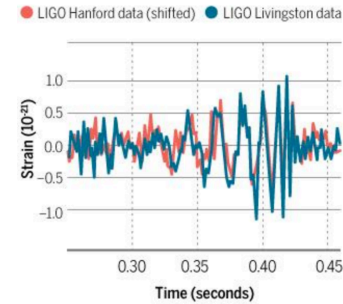


And now .... gravitational radiation detected 9/14/15  
announced 2/11/16

<https://www.ligo.caltech.edu/news/ligo20160211>

### Signals in synchrony

When shifted by 0.007 seconds, the signal from LIGO’s observatory in Washington (red) neatly matches the signal from the one in Louisiana (blue).



### WHAT WE LEARNED

- Black holes exist
- Two of them, 29 and 36 solar masses, merged 1.3 million years ago (masses from period, distance from amplitude of the signal)
- From theory – the masses of the stars that made the black holes were about 70 and 90 solar masses respectively.
- May have evolved by common envelope. One of them may have been a pulsational-pair instability supernova along the way
- 0.4 s a gamma-ray burst may have been detected by the Fermi gamma-ray telescope

## Gamma-Ray Bursts (which maybe related to BHs)

A *Cosmic Gamma-Ray Burst*, GRB for short, is a brief, bright flash of gamma-rays lasting typically about 20 seconds that comes from an unpredictable location in the sky.

Some, in gamma-rays, are as bright as the planet Venus. Most are as bright as the visible stars. It is only because of the Earth's atmosphere and the fact that our eyes are not sensitive to gamma-rays that keep us from seeing them frequently.

With appropriate instrumentation, we see about one of these per day at the Earth. They seem never to repeat from the same source.

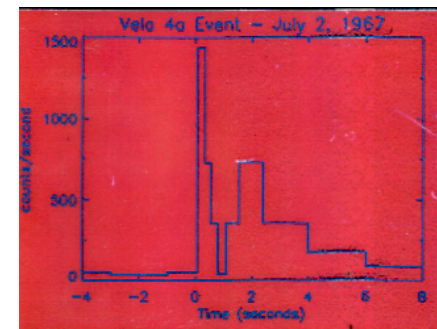
*Vela – to watch*



*Nuclear Test Ban Treaty, 1963  
First Vela satellite pair launched 1963*

The Vela 5 satellites were placed in orbit by the Advanced Research Projects of the DoD and the AEC. Launched on May 23, 1969 into high earth orbit (118,000 km), this pair of satellites and their predecessors, Vela 4, discovered the first gamma-ray bursts. The discovery was announced in 1973.

*First Gamma-Ray Burst*



*The Vela 5 satellites functioned from July, 1969 to April, 1979 and detected a total of 73 gamma-ray bursts in the energy range 150 – 750 keV (n.b., Greater than 30 keV is gamma-rays). Discovery reported Klebesadel, Strong, and Olson (1973).*





Ian Strong – left Ray Klebesadel – right  
September 16, 2003

Gamma-ray bursts (GRBs) discovered 1969 - 72 by Vela satellites. Published by Klebesadel, Strong and Olson (1973)

- Interstellar warfare
- Primordial black hole evaporation
- Flares on nearby stars
- Distant supernovae
- Neutron star quakes
- Comets falling on neutron stars
- Comet anti-comet annihilation
- Thermonuclear explosions on neutron stars
- Name your own ....

*During the 1970's until the early 90's, uncertainty in distance – a factor of one billion.*

## An Observational Dilemma

The gamma-ray detectors could detect brightness and spectra but had only crude angular resolution (> several degrees).

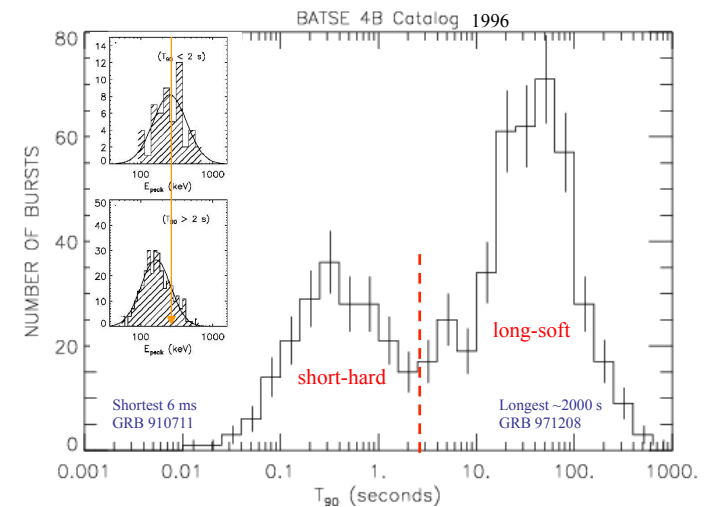
After the burst was over, these huge error boxes showed nothing particularly unusual (or maybe too many unusual things).

We thus had no idea of the distance to the objects emitting the bursts – and hence no knowledge of their energy.

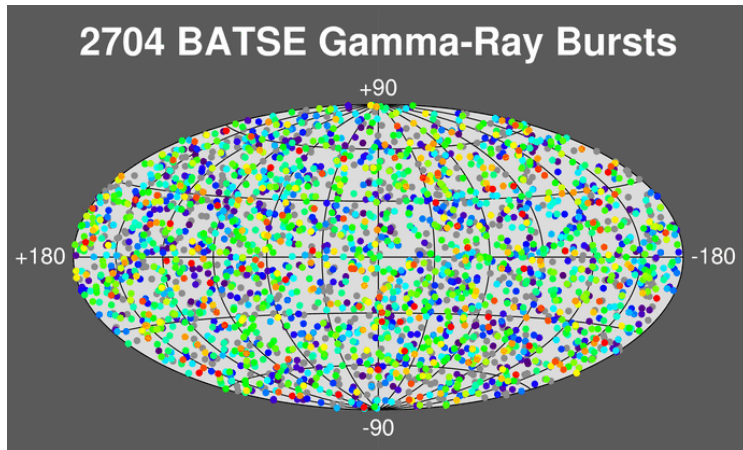
Early on some weak indication of association with the Galactic disk

By the late 90's we knew ...

GRBs come in at least two flavors



In the late 90' s



Bright long bursts are red; short fainter bursts are purple. The rest are intermediate. Note – no correlation with Galactic disk. Each burst was localized to about 1 degree.

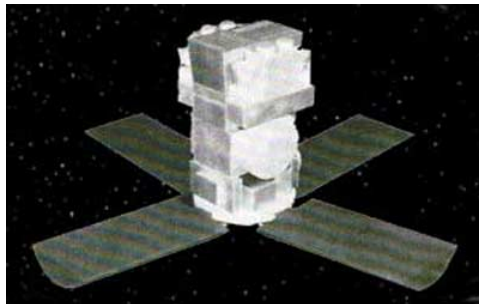
What could do that?

The high degree of isotropy – with us at its “center” implied either an extremely close source (Oort cloud? nearby stars?) or something so far away that the distance from here to the center of the Milky Way (8.5 kpc) meant nothing.

Debate Lamb vs Paczynski (1995) similar to Curtis Shapley debate of (1920)

*Intermezzo* – HETE – 1 (High Energy Transient Explorer)

Launch April 11, 1996; died April 14, 1996



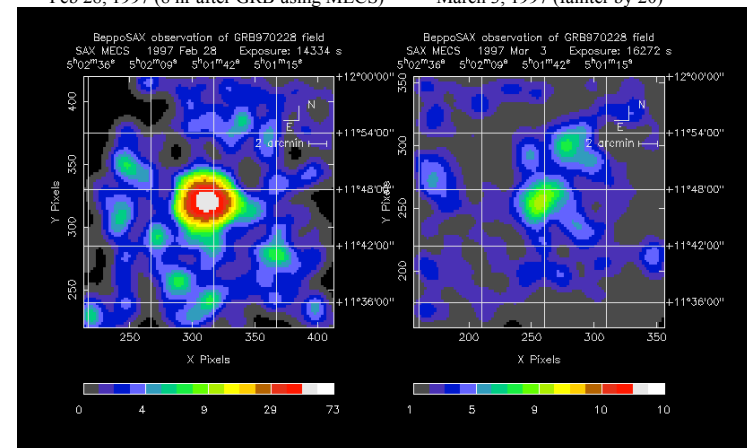
<http://nssdc.gsfc.nasa.gov/nmc/spacecraftDisplay.do?id=1996-061A>

175 kg; Instruments – FREGATE, WXM, UVC, SXC  
\$27 M

(HETE – 2 – launched September 9, 2000)

BeppoSax GRB 970228 (discovered with WFC)

Feb 28, 1997 (8 hr after GRB using MECS)      March 3, 1997 (fainter by 20)

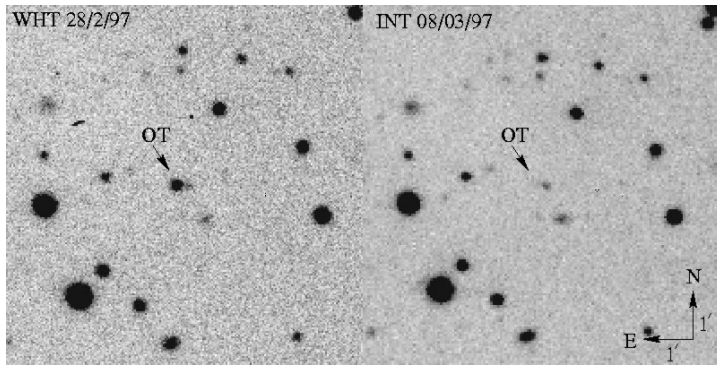


Each square is about 6 arc min or 1/5 the moon' s diameter

## GRB 970228

William Herschel Telescope

Isaac Newton Telescope



Groot, Galama, von Paradijs, et al IAUC 6584, March 12, 1997

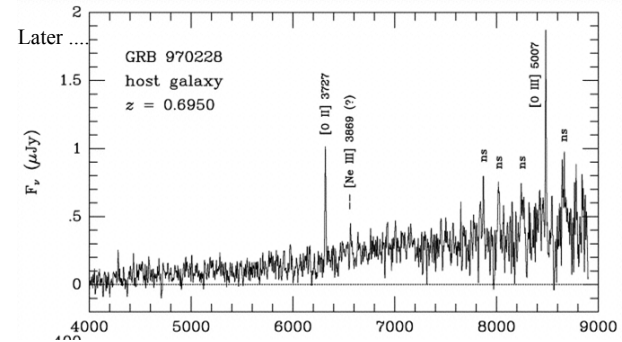
Looked hard and found a little faint galaxy when the OT faded

From the red shift a distance could be inferred – billions of light years. Far, far outside our galaxy.

From the distance and brightness an energy could be inferred.

**$1.6 \times 10^{52}$  erg in gamma rays alone**

*This is 13 times as much energy as the sun will radiate in its ten billion year lifetime, but emitted in gamma-rays in less than a minute. It is 2000 times as much as a really bright supernova radiates in several months.*



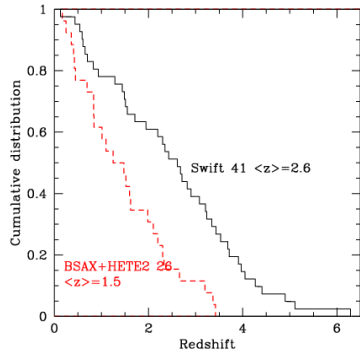
Spectrum of the host galaxy of GRB 970228 obtained at the Keck 2 Telescope. Prominent emission lines of oxygen and neon are indicated and show that the galaxy is located at a redshift of  $z = 0.695$ . (Bloom, Djorgovski, and Kulkarni (2001), ApJ, 554, 678. See also GCN 289, May 3, 1999.

Even brighter was GRB 990123 at redshift 1.6

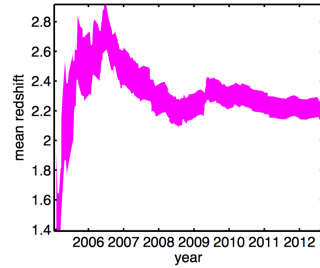
*Given the known brightness of the burst (in gamma-rays) this distance implies an energy of over several times  $10^{54}$  erg. About the mass of the sun turned into pure energy.*

*Had this burst occurred on the far side of our Galaxy, at a distance of 60,000 light years, it would have been as bright – in gamma-rays – as the sun. This is ten billion times brighter than a supernova and equivalent to seeing a one hundred million trillion trillion megaton explosion.*

After a new satellite, SWIFT, was launched in November 2004, much more and better data was obtained

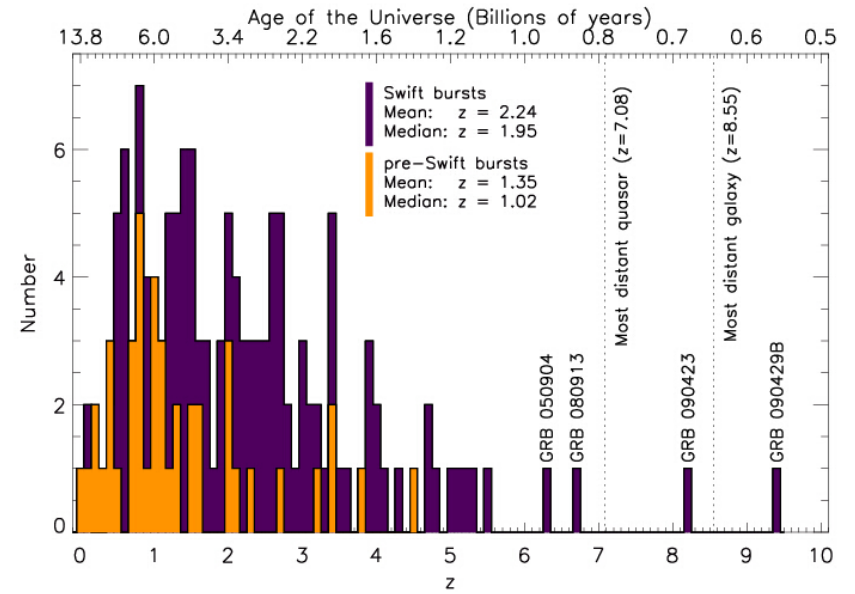


In 2007

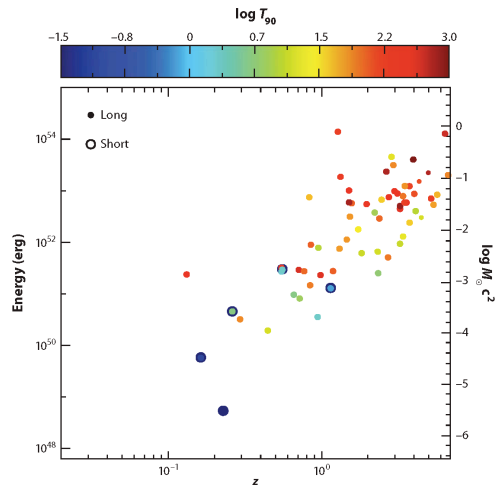


Average redshift with time shows convergence on  $z = 2.2$  (Coward et al. 2012)

Tracks star formation

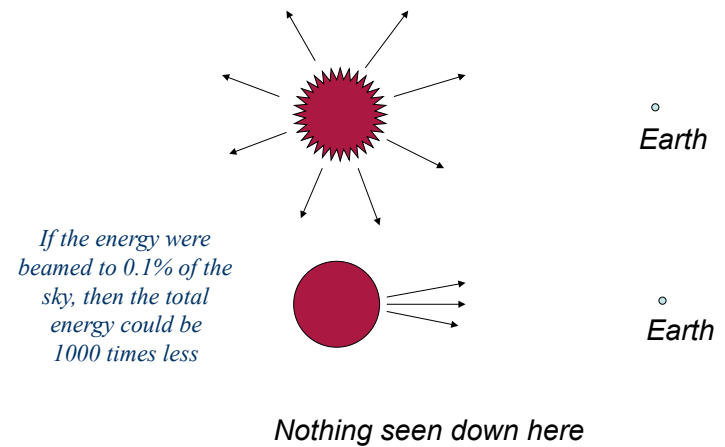


Inferred energy if bursts emit their radiation equally at all angles extends up to  $10^{54}$  erg

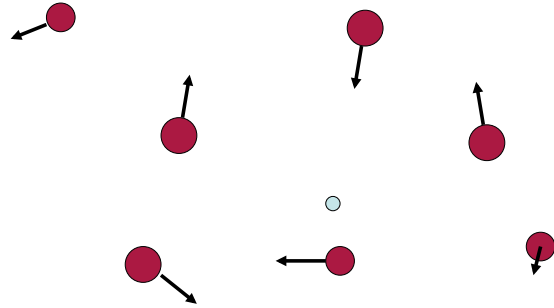


$$M_{\odot}c^2 = 1.8 \times 10^{54} \text{ erg !}$$

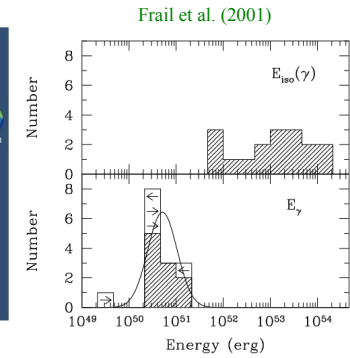
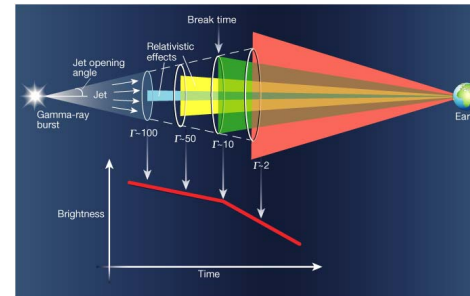
But are the energies required really as great as  $10^{54}$  erg?



But then there would be a lot of bursts that we do not see for every one that we do see.  
About 300 in fact.

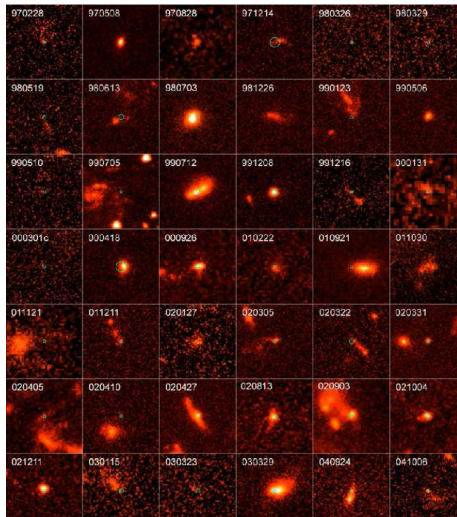


GRBs are beamed and their total energy in relativistic ejecta is  $\sim 10^{51}$  erg.



*As a relativistic jet decelerates we see a larger fraction of the emitting surface until we see the edges of the jet. These leads to a panchromatic break slope of the the afterglow light curve.*

LS-GRBs occur in star-forming regions

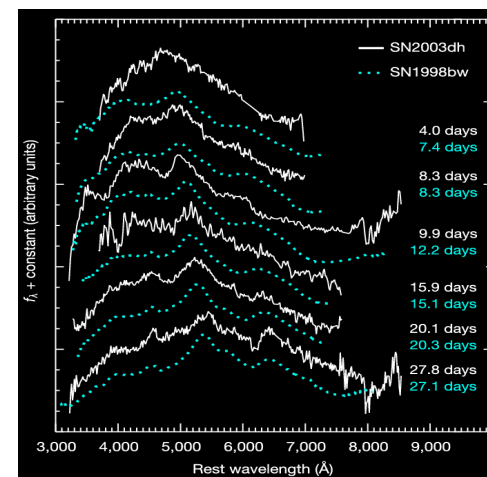


Fruchter et al (2005).

*The green circles show long soft GRB locations to an accuracy of 0.15 arc sec.*

*Conclusion: GRBs trace star formation even more than the average core-collapse supernova. They are thus to be associated with the most massive stars. They also occur in young, small, star forming galaxies that might be metal poor.*

LS-GRBs, at least frequently, occur in simultaneous conjunction with supernovae of Type Ic



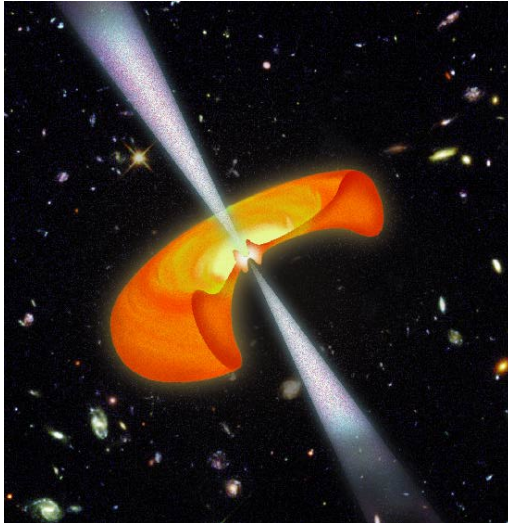
GRB980425/  
SN1998bw

GRB030329/  
SN2003dh

GRB031203/  
SN2003lw

GRB060218/  
SN2006aj

The Collapsar Model  
(Woosley 1993)



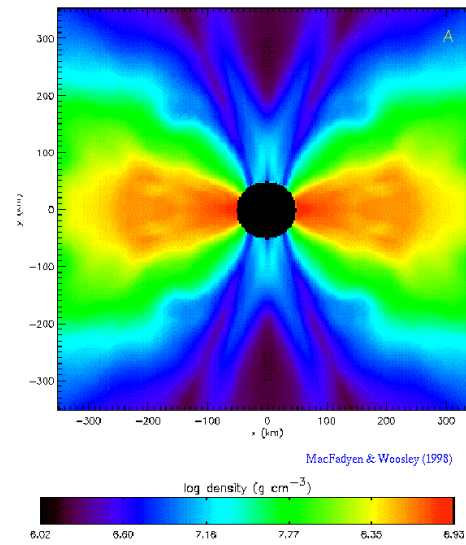
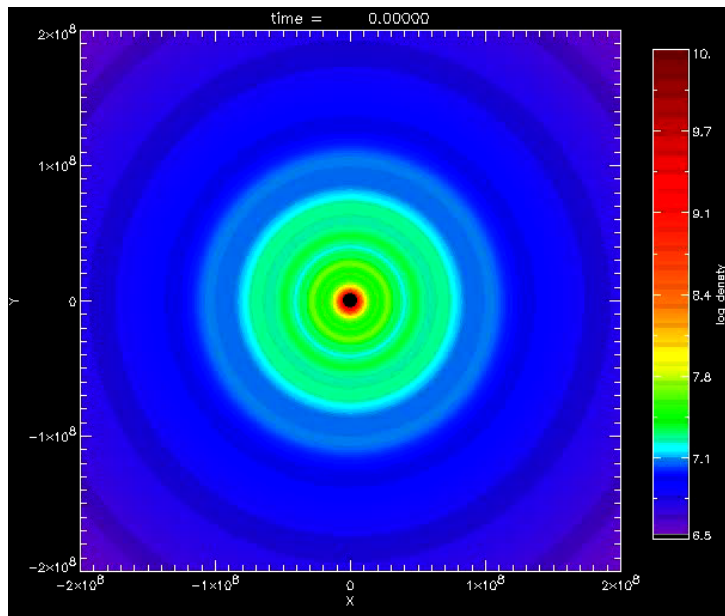
Usually massive stars make supernovae. Their iron core collapses to a neutron star and the energy released explodes the rest of the star.

But what if the explosion fizzled? What if the iron core collapsed to an object too massive to be a neutron star – a black hole.

A star without rotation would then simply disappear....

But what if the star had too much rotation to all go down the (tiny) black hole?

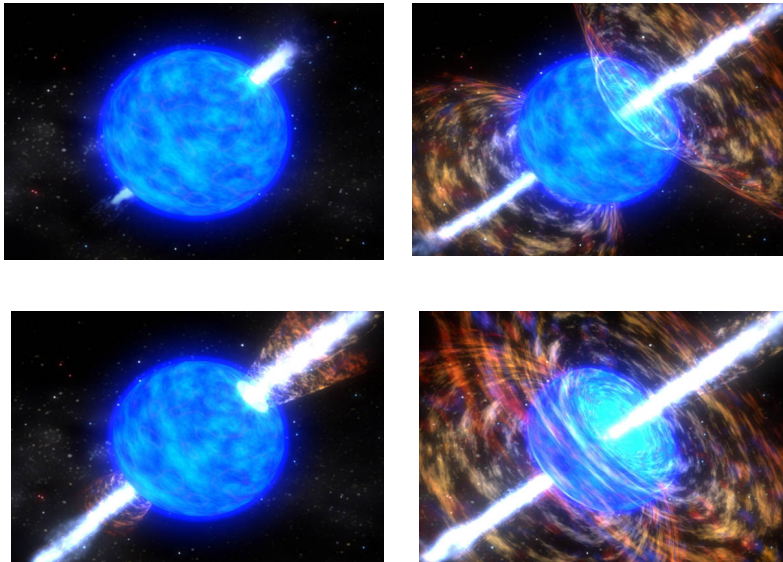
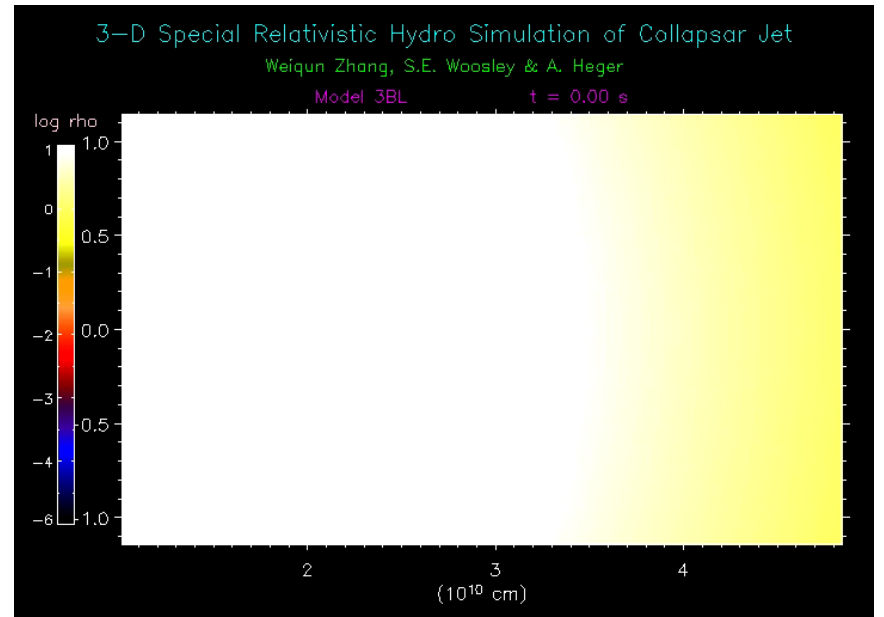
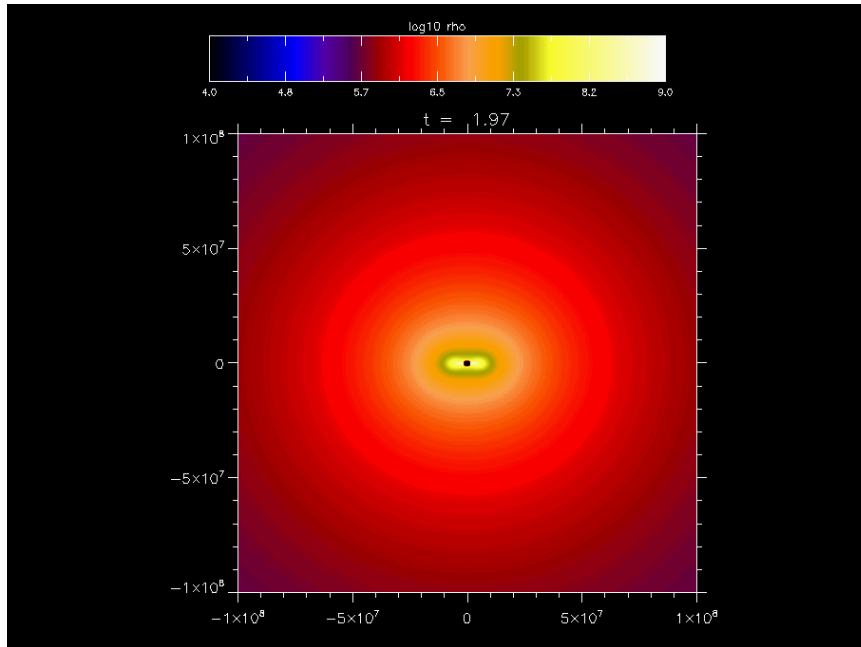
If supernovae are the observational signal that a neutron star has been born, what is the event that signals the birth of a black hole?



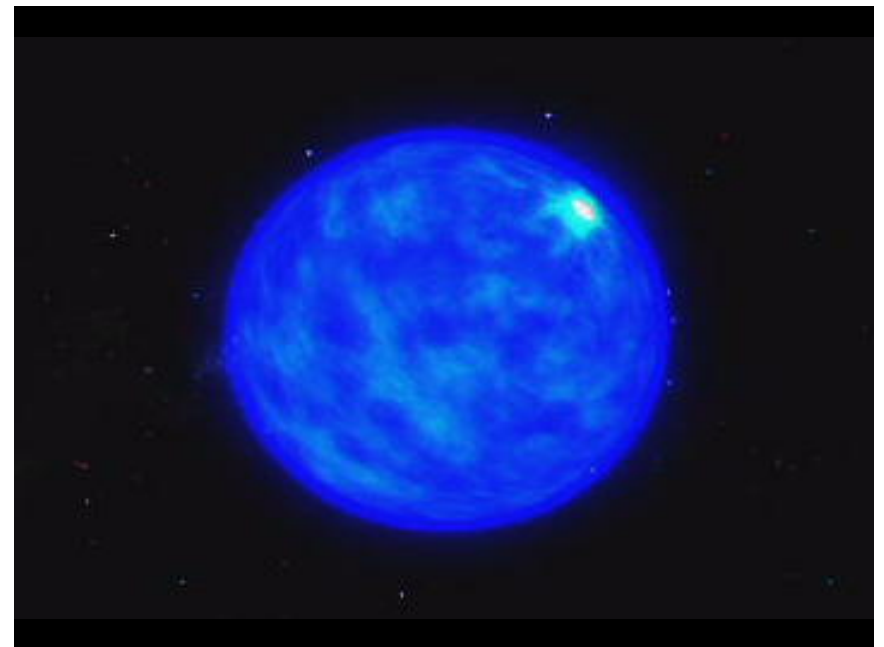
In the vicinity of the rotational axis of the black hole, by a variety of possible processes, energy is deposited.

The exact mechanism for extracting this energy either from the disk or the rotation of the black hole is fascinating physics, but is not crucial to the outcome, so long as the energy is not contaminated by too much matter.

7.6 s after core collapse; high viscosity case.



Dana Berry (Skyworks) and SEW



## Predictions of the Collapsar Model

- ✓ Gamma-ray bursts should occur in star regions
- ✓ GRBs should be accompanied by Type I b or c supernovae (the jet doesn't get out of a giant star in time, need to lose envelope)
- ✓ GRBs should be favored by low metallicity and high redshift

## But there is an alternative: Millisecond Magnetars

Magnetars have fields  $\sim 10^{14-15}$  G  
They might be born as fast rotators  
Efficient dynamo implies  $P \sim t_{\text{conv}} \sim \text{ms}$

*Pro*

NS are naturally associated to core collapse SN  
Less angular momentum required than BH-AD  
NS population can explain transition from asymmetric SNe to XRFs to GRBs

Millisecond magnetar have the correct energy

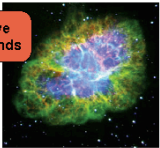
$$E_{\text{rot}} \approx 2 \times 10^{52} \left( \frac{P}{1 \text{ ms}} \right)^{-2} \text{ ergs}$$

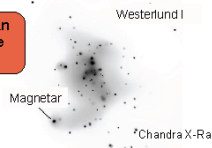
Typical spin-down times are  $\sim 100-1000$  sec

$$E \approx 10^{49} \left( \frac{P}{1 \text{ ms}} \right)^{-4} \left( \frac{B_{\text{dip}}}{10^{15} \text{ G}} \right)^2 \text{ ergs s}^{-1}$$

Magnetars can have massive progenitors

Pulsars have relativistic winds





Westerlund 1

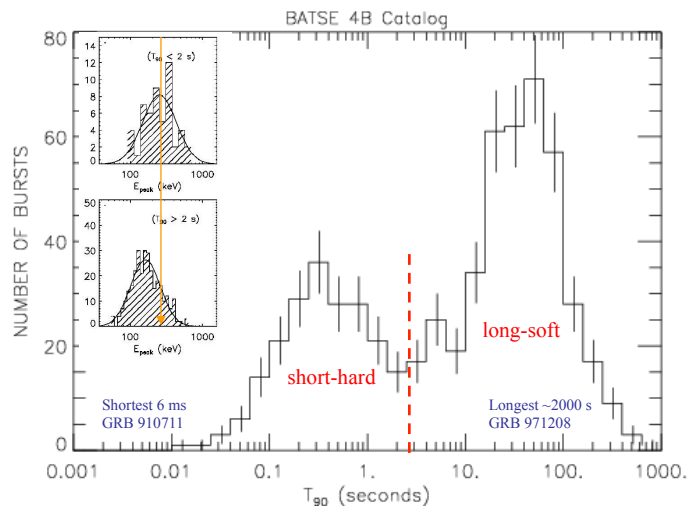
Magnetar

Chandra X-Ray

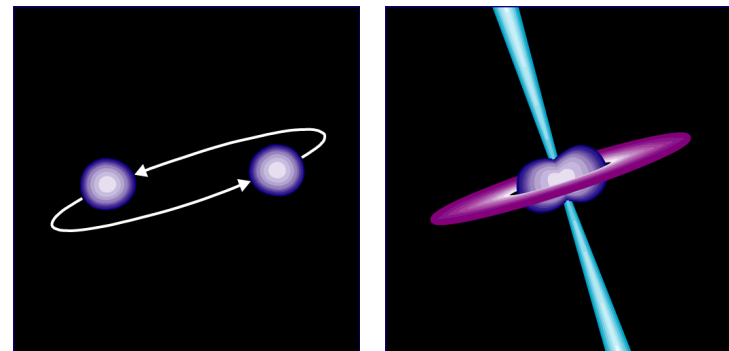
Faintest Cluster Members are O7 (Muno 2006)

Slide from N. Bucciantini

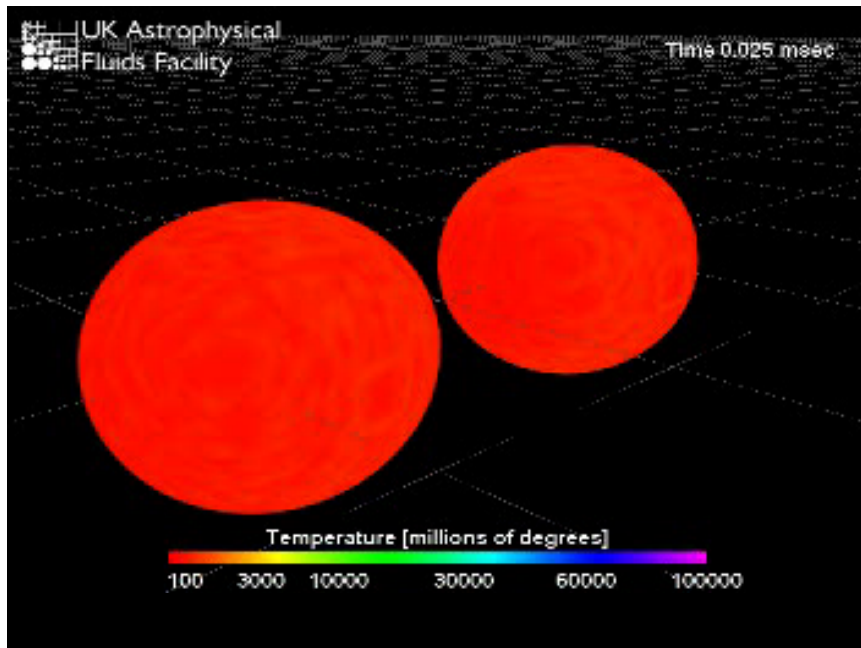
But what about the short hard bursts?



## One Model: Merging Neutron Stars



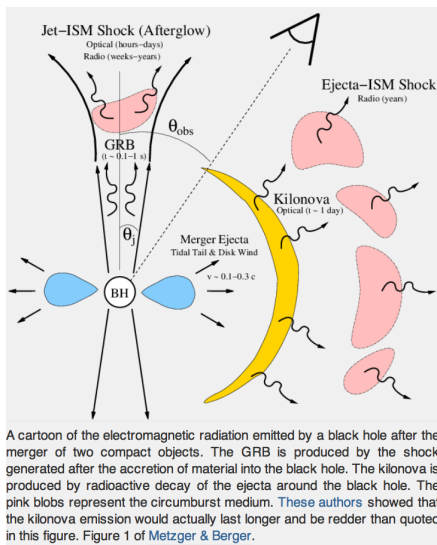




Starting in May 2005, about a half dozen short hard bursts were localized by the HETE-2 and SWIFT satellites.

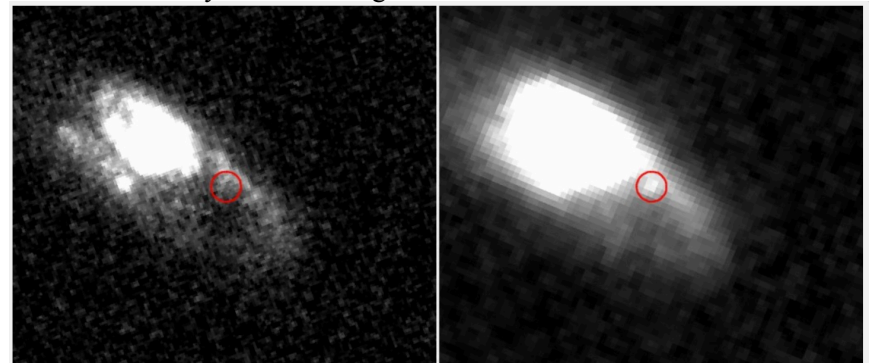
These bursts did not come from star forming regions, and in fact showed all the characteristics expected of merging neutron stars. It is widely believed that merging neutron stars (and neutron stars merging with black holes) have now been observed as short hard gamma-ray bursts. In the next 10 - 15 years, gravitational radiation detectors may detect these mergers.

These GRBs are much closer than the LS GRBs and have ~30 times less energy.



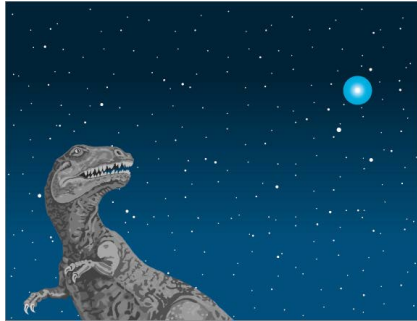
### GRB130603B

Point source identified in a galaxy 3 hours later  
10 days later a strong infrared source was identified



The position where the short GRB occurred in its host galaxy, obtained with the Hubble Space Telescope. The left and right panel show the same galaxy in the optical and the infrared, respectively. In the right panel, Tanvir et al. detect a source in coincidence with the position of the short GRB. Figure 1 of Tanvir et al.

Afterglow or kilonova??



A  $10^{53}$  erg event situated 30,000 light years away (distance from here to the Galactic center) would give as much energy to the earth in 10 seconds as the sun – equivalent to a 200 megaton explosion.

Does it matter having an extra sun in the sky for 10 seconds?

Probably not. This is spread all over the surface of the earth and the heat capacity of the Earth's atmosphere is very high. Gamma-rays would deposit their energy about 30 km up. Some bad nitrogen chemistry would happen.

Noticeable yes, deadly to all living things – No.

#### Biological Hazards of Gamma-Ray Bursts

Distance (kpc)	Events /10 by	Megatons	Results
10	100 – 1000	200	Some ozone damage, EMP acid rain
1	1 – 10	20,000	Ozone gone, acid rain, blindness 2 <sup>nd</sup> and 3 <sup>rd</sup> degree burns*
0.1	0.01 – 0.1	two million	Shock waves, flash incineration, tidal waves, radioactivity ( $^{14}\text{C}$ ) End of life as we know it.

\* Depends on uncertain efficiency for conversion of energetic electrons to optical light