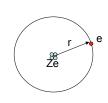
## Quantum Mechanics and Stellar Spectroscopy

http://apod.nasa.gov/apod/

#### Rutherford Atom (1911)



Protons in nucleus. Electrons orbit like planets. The neutron was not discovered until 1932 (Chadwick)

for a single electron Z = 1,2,3,...H, He, Li, etc classically, any value of v or r is allowed. Much like planets.

#### The Electrical Force

Recall the electric force. Like gravity it is a "1/r2" force/ That is:

$$\begin{array}{l} {\rm e} = 4.803 \times 10^{-10} \; {\rm es} u \\ {\rm e}^2 = 2.307 \times 10^{-19} \; {\rm dyne} \; {\rm cm}^2 \end{array} \qquad F_{elec} = \frac{Z_1 Z_2 e^2}{r^2}$$

$$F_{elec} = \frac{Z_1 Z_2 e^2}{r^2}$$

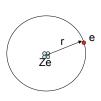
$$Z_1 \longleftrightarrow m$$
 
$$Z_2 \longleftrightarrow M$$

$$e^2 \leftrightarrow G$$

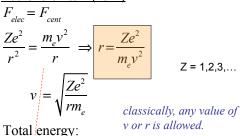
where  $Z_1$  and  $Z_2$  are the (integer) numbers of electronic charges. Similarly, the electric potential energy is

$$E_{elec} = -\frac{Z_1 Z_2 e^2}{r}$$

#### Rutherford Atom (1911)



Protons in nucleus. Electrons orbit like planets. The neutron was not discovered until 1932 (Chadwick)



$$E_{tot} = KE + PE = \frac{m_e v^2}{2} - \frac{Ze^2}{r}$$
$$= \frac{Ze^2}{2r} - \frac{Ze^2}{r} = -\frac{Ze^2}{2r}$$

i.e., 2KE = -PE (if PE is negative) Virial theorem still works for the electric force.

#### Rutherford Atom (1911)



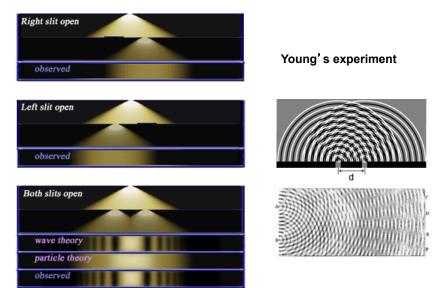
$$E_{tot} = -\frac{Ze^2}{2r}$$

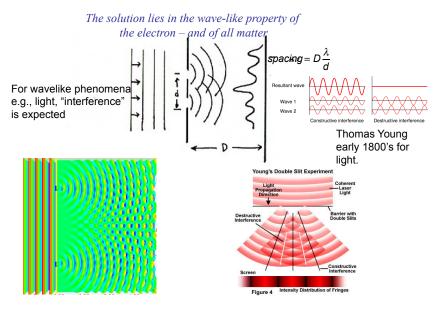
#### BUT,

As the electron moves in its classical orbit it is accelerated, and therefore emits radiation. Because energy is being radiated, the total energy of the system must decrease – become more negative. This means r must get smaller and v must increase. But smaller r and larger v also imply greater acceleration and radiation.

In approximately  $10^{-6}$  s the electron spirals into the nucleus. Goodbye universe...

#### http://en.wikipedia.org/wiki/Double-slit experiment





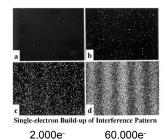
http://en.wikipedia.org/wiki/Interference (wave propagation)

#### Same basic result obtained using electrons!

$$\lambda = \frac{h}{p}$$
  $h = 6.626 \times 10^{-27} \text{ erg sec}$   
=  $6.626 \times 10^{-27} \frac{\text{gm cm}^2}{\text{sec}}$ 

where p is the momentum of the electron,  $m_{\rm e}v$  which has units gm cm/sec

8e- 270e-



Hitachi labs (1989)

In 1924, Louis-Victor de Broglie formulated the DeBroglie hypothesis, claiming that all matter, not just light, has a wavelike nature. He related the wavelength (denoted as  $\lambda$ ) and the momentum (denoted as p)

$$\lambda = \frac{h}{p}$$

A property of our universe

#### HEISENBERG UNCERTAINTY RELATION

The condition that a particle cannot be localized to a region  $\Delta x$  smaller than its wavelength  $\lambda = h/p$  implies

$$\lambda < \Delta x \implies p \, \Delta x > h \implies p > \frac{h}{\Delta x}$$

One cannot confine a particle to a region  $\Delta x$  without making its momentum increase

$$p = \frac{h}{\Delta x}$$
 is the "degenerate" limit

This is a little like the relation Planck had for photons

$$p = \frac{hv}{c} = \frac{h}{\lambda}$$

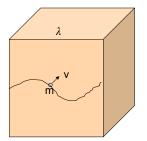
$$\lambda = \frac{h}{p}$$

http://en.wikipedia.org/wiki/Wave-particle\_duality

Light and particles like the electron (and neutron and proton) all have wavelengths, and the shorter the wavelength, the higher the momentum p

This is also known as the Heisenberg Uncertainty Principle. The more accurately you locate a particle ( $\lambda$ ), the more unbounded is its momentum

## Consider one electron in a contracting box





As you squeeze on the box, the particle in the box has to move faster. This is in addition to any thermal motion the particle may have

$$\lambda = \frac{h}{p} = \frac{h}{mv}$$

$$\lambda \downarrow \Rightarrow v \uparrow$$

The squeezing provides the energy to increase v

A little thought will show how this is going to solve our problem with the stability of matter (and also, later, the existence of white dwarfs)

As the electron is forced into a smaller and smaller volume, it must move faster. Ultimately this kinetic energy can support it against the electrical attraction of the nucleus.

Since 
$$p = \frac{h}{\lambda} \Rightarrow KE = \frac{1}{2} m_e v^2 = \frac{p^2}{2m_e} \approx \frac{1}{\lambda^2} \sim \frac{1}{r^2}$$
  
but  $PE = -\frac{Ze^2}{r} \approx \frac{1}{r}$ 

The kinetic energy increases quadratically with 1/r, the electrical potential, only linearly.

There comes a minimum radius where the electron cannot radiate because the sum of its potential and kinetic energies has reached a minimum.

#### Ground state of the hydrogen atom – Neils Bohr (1913)

(lowest possible energy state)

Must fit the wavelength of the electron inside a circle of radius r, the average distance between the electron and the proton.

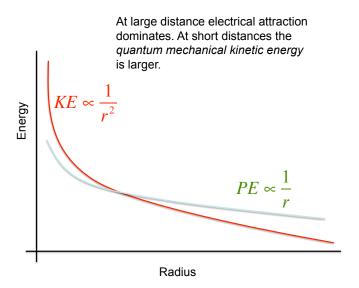
$$\lambda = 2\pi r$$

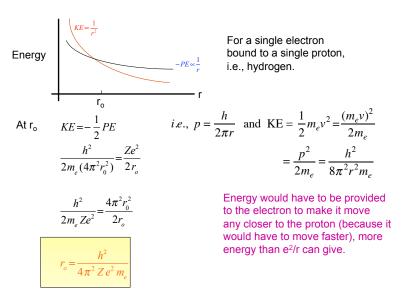
$$= \frac{h}{p}$$
The  $2\pi$  here is rather arbitrary but gives the right answer and omits deeper discussion of "wave functions"
$$KE = \frac{mv^2}{2} = \frac{m^2v^2}{2m} = \frac{p^2}{2m} = \frac{h^2}{2m(4\pi^2r^2)}$$

$$Assuming Z_1 = Z_2 = 1$$

$$PE = -\frac{e^2}{r}$$
 as before

Note that PE goes as 1/r and KE goes as 1/r<sup>2</sup>





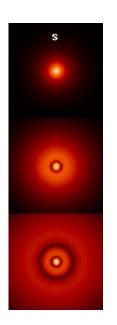
For Z=1 (hydrogen)  $r_0 = 0.529189379 \text{ A} = 5.29189379 \times 10^{-9} \text{ cm}$ 

This is the (average) radius of the "ground state" of the hydrogen atom, 0.529189... A. It is permanently stable. There is no state with lower energy to make a transition to.

However, there also exist "excited states" of atoms that have a transitory existence.

n = 1

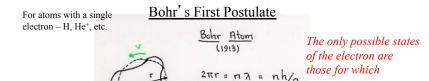
n=3



In the full quantum mechanical solution the electron is described by a "wave function" that gives its probability for being found at any particular distance from the nucleus.

n=2
In the simplest case these distributions are spherical.

The radius in the Bohr model is the average radius but the energy is precise.



Solve as before:

$$r = \frac{n^2 h^2}{4\pi^2 Z e^2 m_e} = 0.53 \frac{n^2}{Z} \text{ Angstroms}$$

$$E_{tot} = -\frac{Z e^2}{2r} = -\frac{2\pi^2 Z^2 e^4 m_e}{n^2 h^2}$$

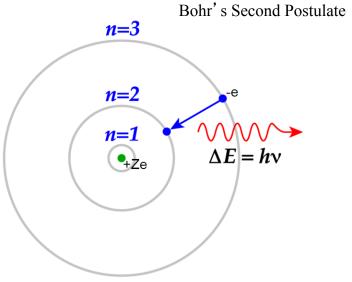
$$E_{tot} = -13.6 \text{ eV} \left(\frac{Z^2}{n^2}\right)$$

$$1 \text{ eV} = 1.602 \times 10^{-12} \text{ erg}$$

$$n = 1 \text{ is the "ground state"}$$

For atoms with only a single electron.

For hydrogen Z = 1



Only the "ground state", n = 1, is permanently stable

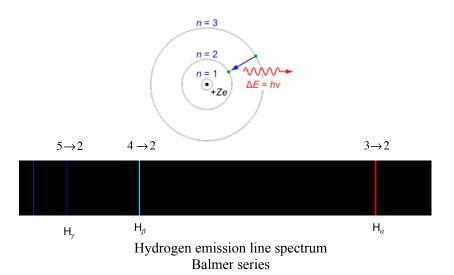
#### **Bohr's Second Postulate**

Radiation in the form of a single quantum (photon) is Emitted (or absorbed) as the electron makes a transition From one state to another. The energy in the photon is the Difference between the energies of the two states.

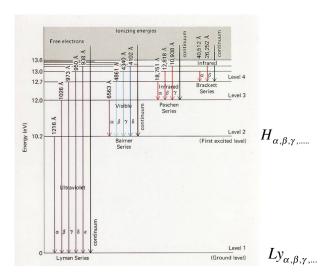
emission absorption 
$$\mathbf{E}_m \rightarrow \mathbf{E}_n + h v \qquad \qquad \mathbf{E}_n + h v \rightarrow \mathbf{E}_m \qquad m > n$$
 
$$hv = \frac{hc}{\lambda} = E_m - E_n$$
 
$$\frac{1}{\lambda} = \frac{E_m - E_n}{hc} = \frac{2\pi^2 Z^2 e^4 m_e}{h^3 c} \left(\frac{1}{n^2} - \frac{1}{m^2}\right)$$
 
$$\frac{1}{\lambda_{mn}} = 1.097 \times 10^5 \ Z^2 \left(\frac{1}{n^2} - \frac{1}{m^2}\right) \ \mathrm{cm}^{-1}$$
 
$$\lambda_{mn} = \frac{911.6 \ \mathrm{A}}{Z^2} \left(\frac{1}{n^2} - \frac{1}{m^2}\right)^{-1}$$

(for atoms with only one electron)

#### **BALMER SERIES**

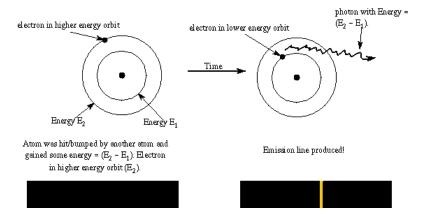


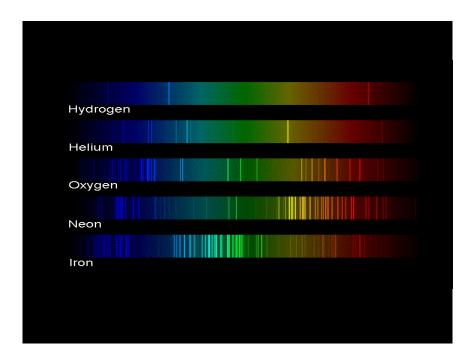
 $\lambda_{mn} = \frac{911.6 \text{ A}}{Z^2} \left( \frac{1}{n^2} - \frac{1}{m^2} \right)^{-1}$ E.g., m = 2, n = 1, Z = 1 $\lambda = 911.6 \text{ A} \left(\frac{1}{1^2} - \frac{1}{2^2}\right)^{-1} = 911.6 \left(\frac{3}{4}\right)^{-1}$  $=911.6\left(\frac{4}{3}\right)=1216\text{ Å}$ Lines that start or end on n=1 are m=3, n=1, Z=1called the "Lyman"  $\lambda = 911.6 \left( \frac{1}{1^2} - \frac{1}{3^2} \right)^{-1} = 911.6 \left( \frac{8}{9} \right)^{-1}$ series. All are between 911.6 and 1216 A.  $=911.6 \left(\frac{9}{8}\right) = 1026 \text{ Å}$ m = 3, n = 2, Z = 1 $\lambda = 911.6 \left( \frac{1}{2^2} - \frac{1}{3^2} \right)^{-1} = 911.6 \left( \frac{1}{4} - \frac{1}{9} \right)^{-1}$ Lines that start or end on n=2 are  $=911.6 \left(\frac{5}{36}\right)^{-1} = 911.6 \left(\frac{36}{5}\right) = 6563 \text{ A}$ called the "Balmer" series. All are between 3646 and 6564 A.



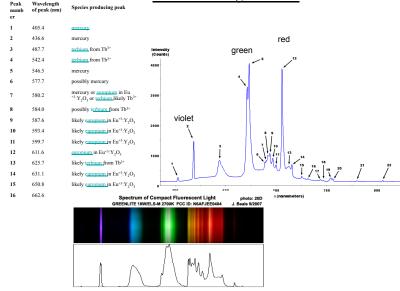
Adjusting the energy of each state in hydrogen by adding 13.6 eV (so that the ground state becomes zero), one gets a diagram where the energies of the transitions can be read off easily.

#### Emission line





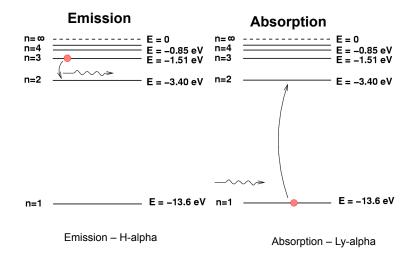
#### Fluorescent Light Fixture

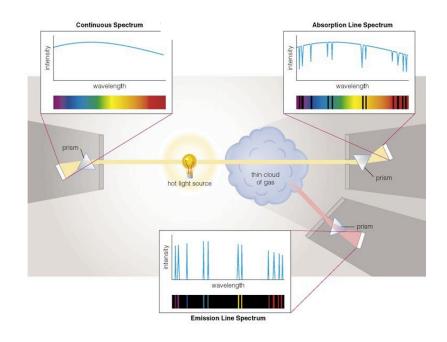


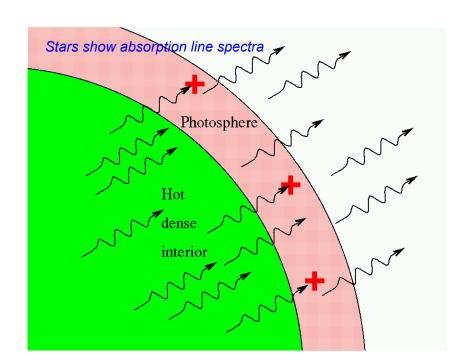
How are excited states populated?

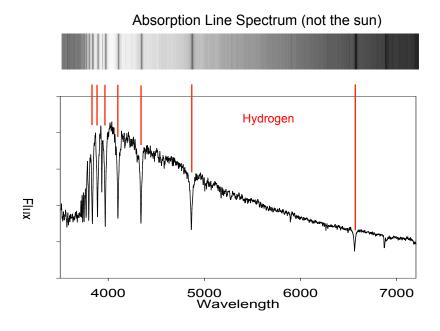
- Absorb a photon of the right energy
- Collisions
- Ionization recombination

#### http://spiff.rit.edu/classes/phys301/lectures/spec lines/Atoms Nav.swf



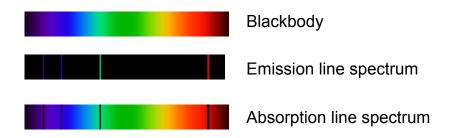


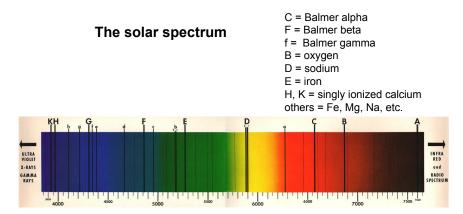




When we examine the spectra of stars, with a few exceptions to be discussed later, we see blackbody spectra with a superposition of *absorption* lines.

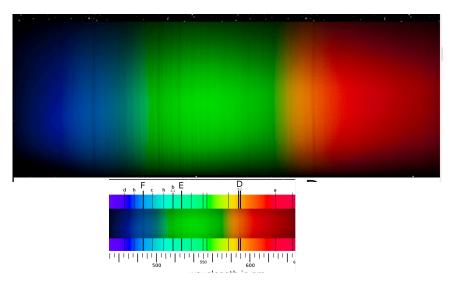
The identity and intensity of the "spectral lines" that are present reflect the temperature, density and composition of the stellar photosphere.



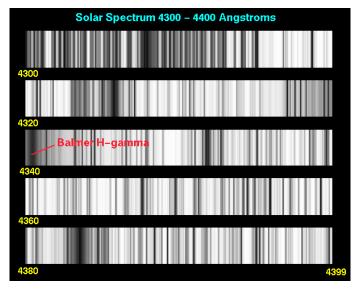


Wollaton (1802) discovered dark lines in the solar spectrum. Fraunhaufer rediscovered them (1817) and studied the systematics

# The sun through a low resolution spectrograph



(Part of) the high resolution solar spectrum

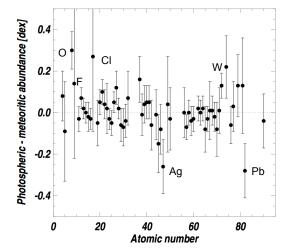


Almost every element has been observed spectroscopically in the sun and has an accurate abundance determination. The rest, except for noble gases and "volatile" elements, have an accurate determination from primitive meteorites (carbonaceous chondrites)

20	$\mathbf{Ca}$	$6.34 \pm 0.04$	$6.29 \pm 0.02$	64	$\operatorname{Gd}$	$1.07 \pm 0.04$	$1.05 \pm 0.02$
21	Sc	$3.15 \pm 0.04$	$3.05 \pm 0.02$	65	$\operatorname{Tb}$	$0.30 \pm 0.10$	$0.32 \pm 0.03$
22	$\mathrm{Ti}$	$4.95 \pm 0.05$	$4.91 \pm 0.03$	66	$\mathbf{D}\mathbf{y}$	$1.10 \pm 0.04$	$1.13 \pm 0.02$
23	V	$3.93 \pm 0.08$	$3.96 \pm 0.02$	67	Но	$0.48 \pm 0.11$	$0.47 \pm 0.03$
24	$\operatorname{Cr}$	$5.64 \pm 0.04$	$5.64 \pm 0.01$	68	$\mathbf{Er}$	$0.92 \pm 0.05$	$0.92 \pm 0.02$
25	Mn	$5.43 \pm 0.05$	$5.48 \pm 0.01$	69	Tm	$0.10 \pm 0.04$	$0.12 \pm 0.03$
26	Fe	$7.50 \pm 0.04$	$7.45 \pm 0.01$	70	Yb	$0.84 \pm 0.11$	$0.92 \pm 0.02$
27	Co	$4.99 \pm 0.07$	$4.87 \pm 0.01$	71	Lu	$0.10 \pm 0.09$	$0.09 \pm 0.02$
28	Ni	$6.22 \pm 0.04$	$6.20 \pm 0.01$	72	$_{ m Hf}$	$0.85 \pm 0.04$	$0.71 \pm 0.02$
29	Cu	$4.19 \pm 0.04$	$4.25 \pm 0.04$	73	Ta		$\textbf{-}0.12 \pm 0.04$
30	$\mathbf{Z}\mathbf{n}$	$4.56 \pm 0.05$	$4.63 \pm 0.04$	74	W	$0.85 \pm 0.12$	$0.65 \pm 0.04$
31	$_{\mathrm{Ga}}$	$3.04 \pm 0.09$	$3.08 \pm 0.02$	75	Re		$0.26 \pm 0.04$
32	Ge	$3.65 \pm 0.10$	$3.58 \pm 0.04$	76	Os	$1.40 \pm 0.08$	$1.35 \pm 0.03$
33	As		$2.30 \pm 0.04$	77	Ir	$1.38 \pm 0.07$	$1.32 \pm 0.02$
34	Se		$3.34 \pm 0.03$	78	$\operatorname{Pt}$		$1.62 \pm 0.03$
35	$\operatorname{Br}$		$2.54 \pm 0.06$	79	Au	$0.92 \pm 0.10$	$0.80 \pm 0.04$
36	Kr	$[3.25 \pm 0.06]$	-2.27	80	Hg		$1.17 \pm 0.08$
37	Rb	$2.52 \pm 0.10$	$2.36 \pm 0.03$	81	Tl	$0.90 \pm 0.20$	$0.77 \pm 0.03$
38	$\operatorname{Sr}$	$2.87 \pm 0.07$	$2.88 \pm 0.03$	82	Pb	$1.75 \pm 0.10$	$2.04 \pm 0.03$
39	$\mathbf{Y}$	$2.21 \pm 0.05$	$2.17 \pm 0.04$	83	$\operatorname{Bi}$		$0.65 \pm 0.04$
40	$\operatorname{Zr}$	$2.58 \pm 0.04$	$2.53 \pm 0.04$	90	$\operatorname{Th}$	$0.02 \pm 0.10$	$0.06 \pm 0.03$
41	Nb	$1.46 \pm 0.04$	$1.41 \pm 0.04$	92	U		$\textbf{-}0.54 \pm 0.03$
42	Mo	$1.88 \pm 0.08$	$1.94 \pm 0.04$				

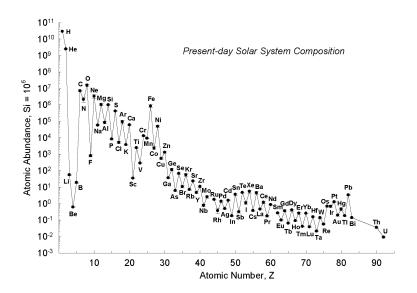
Table 1: Element abundances in the present-day solar photosphere. Also given are the corresponding values for CI carbonaceous chondrites (Lodders, Palme & Gail 2009). Indirect photospheric estimates have been used for the noble gases (Sect. 3.9).

	Elem.	Photosphere	Meteorites		Elem.	Photosphere	Meteorites
1	Н	12.00	$8.22 \pm 0.04$	44	Ru	$1.75 \pm 0.08$	$1.76 \pm 0.03$
2	$_{\mathrm{He}}$	$[10.93 \pm 0.01]$	1.29	45	$\operatorname{Rh}$	$0.91 \pm 0.10$	$1.06 \pm 0.04$
3	$_{ m Li}$	$1.05\pm0.10$	$3.26 \pm 0.05$	46	$\operatorname{Pd}$	$1.57 \pm 0.10$	$1.65 \pm 0.02$
4	${ m Be}$	$1.38 \pm 0.09$	$1.30 \pm 0.03$	47	$\mathbf{A}\mathbf{g}$	$0.94 \pm 0.10$	$1.20\pm0.02$
5	В	$2.70 \pm 0.20$	$2.79 \pm 0.04$	48	$\operatorname{Cd}$		$1.71 \pm 0.03$
6	$\mathbf{C}$	$8.43 \pm 0.05$	$7.39 \pm 0.04$	49	$_{ m In}$	$0.80 \pm 0.20$	$0.76 \pm 0.03$
7	N	$7.83 \pm 0.05$	$6.26 \pm 0.06$	50	$\operatorname{Sn}$	$2.04 \pm 0.10$	$2.07 \pm 0.06$
8	O	$8.69 \pm 0.05$	$8.40 \pm 0.04$	51	$\operatorname{Sb}$		$1.01 \pm 0.06$
9	$\mathbf{F}$	$4.56 \pm 0.30$	$4.42 \pm 0.06$	52	${ m Te}$		$2.18 \pm 0.03$
10	Ne	$[7.93 \pm 0.10]$	-1.12	53	I		$1.55 \pm 0.08$
11	Na	$6.24 \pm 0.04$	$6.27 \pm 0.02$	54	Xe	$[2.24 \pm 0.06]$	-1.95
12	Mg	$7.60 \pm 0.04$	$7.53 \pm 0.01$	55	Cs		$1.08 \pm 0.02$
13	$\mathbf{A}\mathbf{l}$	$6.45 \pm 0.03$	$6.43 \pm 0.01$	56	$_{\mathrm{Ba}}$	$2.18 \pm 0.09$	$2.18 \pm 0.03$
14	$\operatorname{Si}$	$7.51 \pm 0.03$	$7.51 \pm 0.01$	57	$_{ m La}$	$1.10 \pm 0.04$	$1.17 \pm 0.02$
15	P	$5.41 \pm 0.03$	$5.43 \pm 0.04$	58	Ce	$1.58 \pm 0.04$	$1.58 \pm 0.02$
16	$\mathbf{S}$	$7.12 \pm 0.03$	$7.15 \pm 0.02$	59	$\Pr$	$0.72 \pm 0.04$	$0.76 \pm 0.03$
17	Cl	$5.50 \pm 0.30$	$5.23 \pm 0.06$	60	Nd	$1.42 \pm 0.04$	$1.45 \pm 0.02$
18	$\mathbf{Ar}$	$[6.40 \pm 0.13]$	-0.50	62	$\operatorname{Sm}$	$0.96 \pm 0.04$	$0.94 \pm 0.02$
19	$\mathbf{K}$	$5.03 \pm 0.09$	$5.08 \pm 0.02$	63	$\mathbf{E}\mathbf{u}$	$0.52 \pm 0.04$	$0.51 \pm 0.02$
20	$\mathbf{Ca}$	$6.34 \pm 0.04$	$6.29 \pm 0.02$	64	$\operatorname{Gd}$	$1.07 \pm 0.04$	$1.05 \pm 0.02$



Asplund et al (2009; ARAA)

Figure 7: Difference between the logarithmic abundances determined from the solar photosphere and the CI carbonaceous chondrites as a function of atomic number. With a few exceptions the agreement is excellent. Note that due to depletion in the Sun and meteorites, the data points for Li, C, N and the noble gases fall outside the range of the figure.



### Notation: Ionization stages

ΗΙ	neutral hydrogen	1 p	1 e
ΗII	ionized hydrogen	1 p	0 e
			_
He I	neutral helium	2 p	2 e
He II	singly ionized helium	2 p	1 6
He III	doubly ionized helium	2 p	0 e
CI	neutral carbon	6 p	6 e
C II	$C^+$	6 p	5 e
C III	C <sup>++</sup>	6 p	4 e
etc.			

## Ionization

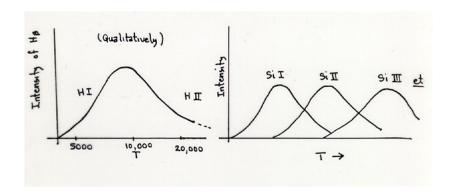
As the temperature in a gas is raised, electrons will be removed by collisions and interactions with light. The gas comes *ionized*.

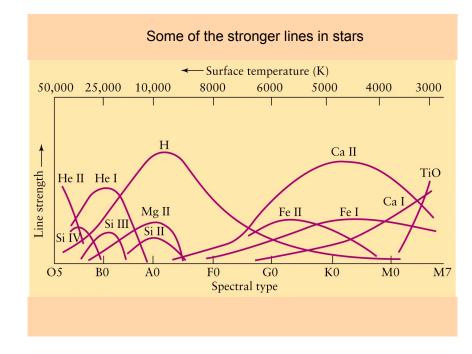
The degree of ionization depends on the atom considered and the temperature.

The ionization energy is the energy required to remove a single electron from a given ion. The excitation energy is the energy required to excite an electron from the ground state to the first excited state.

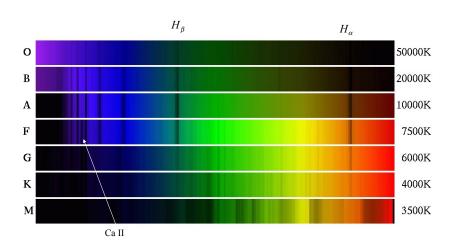
Ion		Excitation energy (eV)	Ionization energy (eV)
	ΗΙ	10.2	13.6
	He I	20.9	24.5
	He II	40.8	54.4
rare	Li I	1.8	5.4
	Ne I	16.6	21.5
	Na I	2.1	5.1
	Mg I	2.7	7.6
	Ca I	1.9	6.1

Li is He plus one proton, Na is Ne plus 1 proton, Ca is Ar plus 2 protons. The noble gases have closed electron shells and are very stable.





## Spectral Sequence



Spectral Type	Principal Characteristics	Spectral Criteria
0	Hottest blue stars Relatively few lines He II dominates	Strong He II lines—in absorption, sometimes emission. He I lines weak, but increasing in strength from O5 to O9. Hydrogen Balmer lines prominent, but weak compared to later types. Lines of Si IV, O III, N III, and C III.
В	Hot blue stars More lines He I dominates	He I lines dominate, with maximum strength at B2; He II lines virtually absent. Hydrogen lines strengthening from B0 to B9. Also Mg II and Si II lines.
A	Blue stars Ionized metal lines Hydrogen dominates	The hydrogen lines reach maximum strength at A0. Lines of ionized metals (Fe II, Si II, Mg II) at maximum strength near A5. Ca II lines strengthening. The lines of neutral metals are appearing weakly.

F	White stars Hydrogen lines declining Neutral metal lines increasing	The hydrogen lines are weakening rapidly, while the H and K lines of Ca II strengthen. Neutral metal (Fe I and Cr I) lines gaining on ionized metal lines by late F.
G . :	Yellow stars Many metal lines Ca II lines dominate	The hydrogen lines are very weak. The Ca II H and K lines reach maximum strength near G2. Neutral metal (Fe I, Mn I, Ca I) lines strengthening, while ionized metal lines diminish. The molecular G-band of CH becomes strong.
К .	Reddish stars Molecular bands appear Neutral metal lines dominate	The hydrogen lines are almost gone. The Ca lines are strong. Neutral metal lines are very prominent. By late K the molecular bands of- TiO begin to appear.
M	Coolest red stars Neutral metal lines strong Molecular bands dominate	The neutral metal lines are very strong. Molecular bands are prominent, with the TiO bands dominating the spectrum by M5. Vanadium oxide (VO) bands appear.

			Fraction MS stars
			solar neighborhood
O	> 25,000 K	Delta Orionis	1/3,000,000
В	11,000 - 25,000	Pleiades brightest	1/800
A	7500 - 11,000	Sirius	1/160
F	6000 - 7500	Canopus	1/133
G	5000 - 6000	Sun	1/13
K	3500 - 5000	Arcturus	1/8
M	< 3500	Proxima Centauri	3/4

<b>Main sequence</b> stars would look like this to the human eye	
M K G F A B	

http://en.wikipedia.org/wiki/Stellar classification

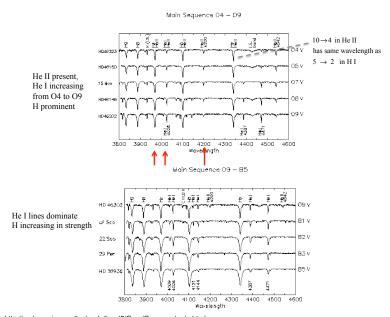
- Cannon further refined the spectral classification system by dividing the classes into numbered subclasses:
- For example, A was divided into A0 A1 A2 A3 ... A9

A0 is hotter than A9

B9 comes before A0

**OBAFGKM** 

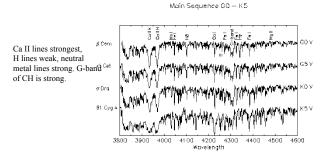
F1 comes after A9



http://nedwww.ipac.caltech.edu/level5/Gray/Gray\_contents.html

#### **Balmer Series**

Transition	3 -> 2	4 -> 2	5 -> 2	6 -> 2	7-> 2
Name	${\rm H}_{\alpha}$	$^{H}\!eta$	$^{H_{\gamma}}$	$H_{\delta}$	$H_{\varepsilon}$
Wavelength	6563	4861	4341	4102	3970
Color	Red	Blue- green	Violet	Violet	Ultra- violet



H lines weak. Lines of neutral metals present but weakening. Major characteristic is bands from molecules like TiO and MgH

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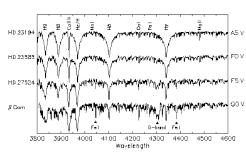
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Main Sequence B5 — A5

85 V 88 v 8 Per H lines reach maximum a Lyi AO V strength. Ca II growing. Fe II, Si II, Mg II reach & Leo A3 V 3800 3900 4000 4100 4200 4300 4400 4500 4600 Wavelength Main Sequence A5 — G0

H lines start to decrease in strength. Ca II strong. Fe I growing in strength. Mg II decreasing.



 $H_{\nu} = 4341 A$ 

 $H_{\delta} = 4102 \text{ A}$ 

## DISTINGUISHING MAIN SEQUENCE STARS FROM RED GIANTS OF THE SAME COLOR

The surface gravity  $g = \frac{GM}{R^2}$ 

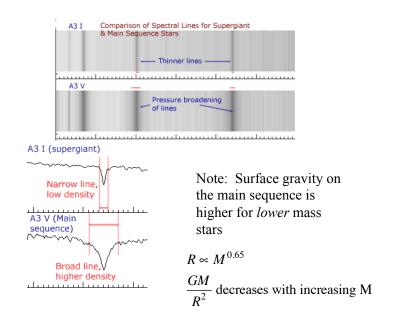
of a star is clearly larger for a smaller radius (if M is constant)

To support itself against this higher gravity, a the stellar photosphere must have a larger pressure. As we shall see later for an ideal gas

$$P = nkT$$

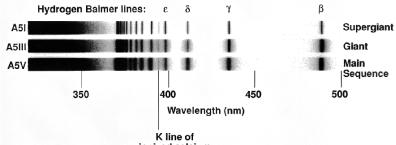
where n is the number density and T is the temperature. If two stars have the same temperature, T, the one with the higher pressure (smaller radius) will have the larger n, i.e., its atoms will be more closely crowded together. This has two effects:

- 1) At a greater density (and the same T) a gas is less ionized
- 2) If the density is high, the electrons in one atom "feel" the presence of other nearby nuclei. This makes their binding energy less certain. This spreading of the energy level is called "Stark broadening"



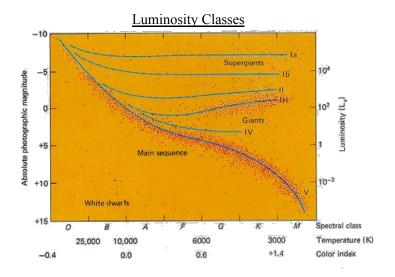
- In 1943, Morgan & Keenan added the Luminosity Class as a second classification parameter:
  - −Ia = Bright Supergiants
  - −Ib = Supergiants
  - -II = Bright Giants
  - -III = Giants
  - -IV = Subgiants
  - -V = Main sequence

And so the sun is a G2-V star



All 3 stars have the same temperature but,

- The supergiants have the narrowest absorption lines
- Small Main-Sequence stars have the broadest lines
- Giants are intermediate in line width and radius



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