

5. How much energy is produced by nuclear fusion in the core of the Sun each second?

$$L_{\odot} = \frac{\text{Energy}}{\text{sec}} \Rightarrow \boxed{\text{Energy in 1 sec} = L_{\odot} \cdot 1 \text{ sec} = 4 \times 10^{33} \frac{\text{erg}}{\text{s}} \cdot 1 \text{ s} = 4 \times 10^{33} \text{ ergs}}$$

6. How long will a $0.3M_{\odot}$ star with $L = 0.01L_{\odot}$ spend on the main-sequence? (Hint, the main-sequence lifetime of the Sun is 10 billion years).

$$\text{From } L = \frac{\Delta E}{\Delta t} = \frac{\Delta M c^2}{\Delta t} \Rightarrow \Delta t_{\text{life}} \propto \frac{M}{L} \Rightarrow t_{\text{life}} = t_{\text{life}, \odot} \cdot \frac{M/M_{\odot}}{L/L_{\odot}}$$

$$\Rightarrow \boxed{\Delta t_{\text{life}} = \frac{0.3 M_{\odot}/M_{\odot}}{0.01 L_{\odot}/L_{\odot}} \cdot 10 \text{ billion years} = \frac{0.3}{0.01} \cdot 10 \text{ bill yrs} = 300 \text{ billion years}}$$

7. In the fusion of four protons into helium, 4.7×10^{-26} grams of matter is turned into energy. How much energy does this amount of matter produce?

$$\boxed{\Delta E = \Delta M c^2 = (4.7 \times 10^{-26} \text{ g}) (3 \times 10^{10} \text{ cm/s}) = 4.23 \times 10^{-5} \text{ ergs}}$$

8. Four stars occupy the four corners of an H-R diagram (UL, LL, UR, LR).

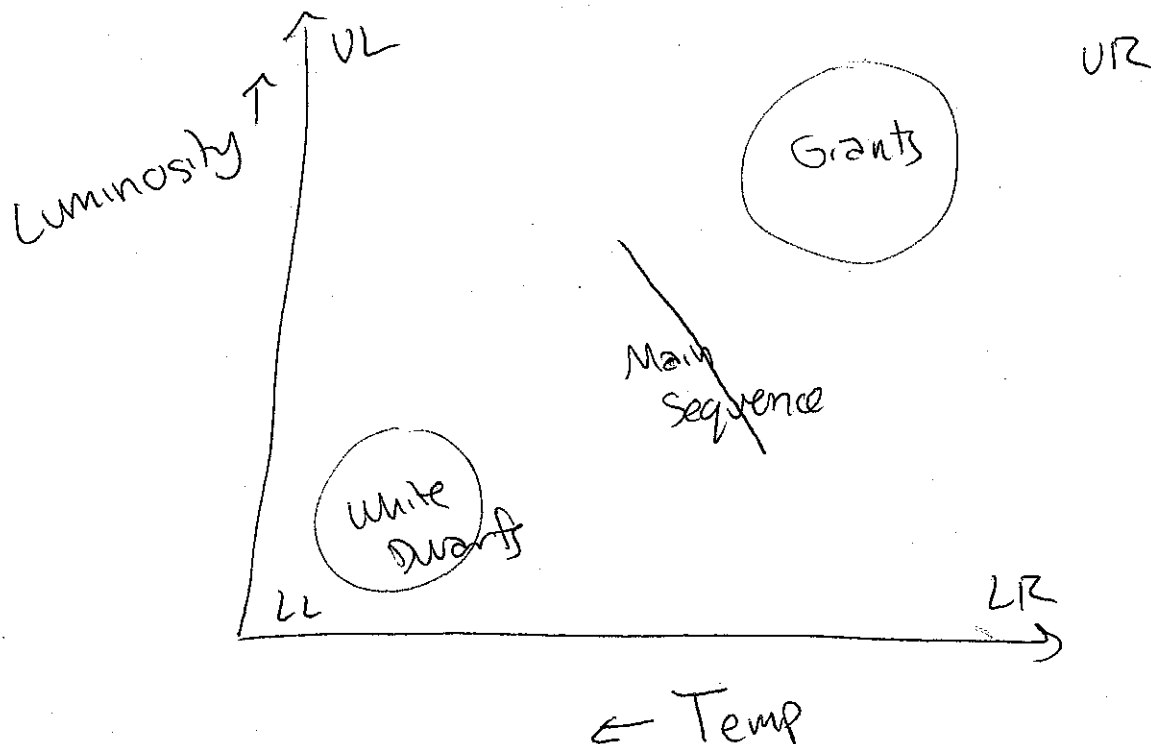
UR In which corner(s) is (are) the largest star(s)? (low T , high $L \Rightarrow$ big R
Since $L = 4\pi R^2 T^4$)

UL, UR In which corner(s) is (are) the most luminous star(s)?

UL, LL In which corner(s) is (are) the hottest star(s)?

LR In which corner(s) is (are) the lowest mass main-sequence stars?

(on M.S. $L \propto M^{3.5} \Rightarrow$ low L means low M)



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Some numbers: $L_{\odot} = 4 \times 10^{33}$ ergs/second $M_{\odot} = 2 \times 10^{33}$ grams $c = 3 \times 10^{10}$ cm/second.

1. What is the energy source for the Sun? (select one)

☐ Nuclear fission reactions

☒ Nuclear fusion of hydrogen into helium

☐ Conversion of gravitational potential energy into heat and light

☐ None of the above

2. Why are high temperatures required for fusion reactions? (select one)

☐ The high temperature is required to counteract gravity

☒ Only at high temperature do the nuclei in a gas approach close enough for the nuclear force to overcome electrical repulsion

☐ Uranium only undergoes radioactive decay at high temperature

☐ The strong force only exists in high temperature environments.

3. Label the following questions about star formation processes True or False.

☐ Dust is required to shield molecular cloud cores from starlight and thereby allow the cores to cool

☐ Protostars enter the HR Diagram from the upper left corner (upper right)

☒ Most or all stars form in groups or clusters of stars (Pleiades)

☒ Protostars stop their gravitational contraction when their central temperature is high enough for hydrogen fusion to begin

4. Coal burning releases 4×10^{12} ergs per gram of coal.

(a) What is the total amount of energy that could be generated if the Sun were coal-powered and made of coal?

$$E_{\text{tot}} = M_{\odot} \cdot \left(\frac{\# \text{ ergs}}{\text{gram}} \text{ released} \right) = 2 \times 10^{33} \text{ g} \cdot 4 \times 10^{12} \frac{\text{erg}}{\text{g}} = 8 \times 10^{45} \text{ erg}$$

(b) How long would the coal-powered Sun of part (a) last before running out of fuel?

$$L = \frac{\Delta E}{\Delta t} \Rightarrow \Delta t_{\text{life}} \approx \frac{\Delta E}{L} = \frac{\Delta E \text{ from (a)}}{L_{\odot}}$$

$$= \frac{8 \times 10^{45} \text{ ergs}}{4 \times 10^{33} \text{ erg/s}} = 2 \times 10^{12} \text{ s} \cdot \frac{1 \text{ mm}}{100 \text{ s}} \cdot \frac{1 \text{ hr}}{60 \text{ min}} \cdot \frac{1 \text{ day}}{24 \text{ hr}} \cdot \frac{1 \text{ yr}}{365 \text{ d}}$$

(canceling unit terms)

$$\Rightarrow \Delta t_{\text{life}} \approx 63420 \text{ years}$$

assuming all of sun's mass is turned into energy