Once the relevant nuclear physics is known in terms of the necessary rate factors, $\lambda = N_A < \sigma_V > =$ function (T, ρ) , the evolution of the composition can be solved from the coupled set of rate equations. For the species *I*:

$$\frac{dY_I}{dt} = -\sum_{j,k}^{\text{destruction}} Y_I Y_j \rho \lambda_{jk}(I) + \sum_{k,j,L \ \Im \ L+k=I+j}^{\text{creation}} Y_L Y_k \rho \lambda_{kj}(L)$$

The rather complicated looking restriction on the second summation simply reflects the necessary conservation conditions for the generic forward reaction, I(j,k)L and its reverse, L(k,j)I.

k and j are typically n, p, α , or γ .

In the special case of weak decay one substitutes for $Y_j \rho \lambda$ the inverse mean lifetime against the weak interaction, $\lambda = 1/\tau_{beta}$. The mean lifetime is the half-life divided by ln 2 = 0.693. Then one has a term with a single Y_i times λ .

THE CNO BI-CYCLE (e^{+}, v) (p, γ) (e^{+}, v) (p, γ) (p, γ)

Lecture 9

Hydrogen Burning Nucleosynthesis,

Classical Novae, and X-Ray Bursts

Suppose we write the differential equation for ¹⁴N in the CNO-1 cycle. In general ¹⁴N might be created and destroyed by a large variety of reactions, $(\alpha, \gamma), (n, p), (\alpha, p), (n, \gamma), (p, \alpha), (p, n), (\gamma, \alpha), etc$. But here there are just two:

$$\frac{dY(^{14}N)}{dt} = Y(^{13}C)Y_{\rho} \lambda_{\rho,\gamma}(^{13}C) - Y(^{14}N)Y_{\rho} \lambda_{\rho,\gamma}(^{14}N)$$

Now suppose ¹³*C* and ¹⁴*N* are in steady state. That is every time ${}^{13}C(p,\gamma){}^{14}N$ creates a ${}^{14}N, {}^{14}N(p,\gamma){}^{15}O$ destroys it.

red = slow

Then
$$\frac{dY({}^{14}N)}{dt} \approx 0 \Rightarrow \frac{Y({}^{13}C)}{Y({}^{14}N)} \approx \frac{\lambda_{\rho\gamma}({}^{14}N)}{\lambda_{\rho\gamma}({}^{13}C)}$$

and by similar reasoning Everywhere that $\frac{dY_i}{dt} \approx 0$

$$\frac{Y({}^{13}C)}{Y({}^{12}C)} = \frac{\lambda_{p\gamma}({}^{12}C)}{\lambda_{p\gamma}({}^{13}C)} \qquad \qquad \frac{Y({}^{15}N)}{Y({}^{14}N)} = \frac{\lambda_{p\gamma}({}^{14}N)}{\lambda_{p\gamma}({}^{15}N) + \lambda_{p\alpha}({}^{15}N)}$$

and if the entire first loop was in steady state

$$\frac{Y({}^{12}C)}{Y({}^{14}N)} = \frac{\lambda_{p\gamma}({}^{14}N)}{\lambda_{p\gamma}({}^{12}C)}$$

i.e.,
$$\frac{Y({}^{14}N)}{Y({}^{12}C)} = \left(\frac{Y({}^{14}N)}{Y({}^{13}C)}\right) \left(\frac{Y({}^{13}C)}{Y({}^{12}C)}\right) = \left(\frac{\lambda_{p\gamma}({}^{13}C)}{\lambda_{p\gamma}({}^{14}N)}\right) \left(\frac{\lambda_{p\gamma}({}^{12}C)}{\lambda_{p\gamma}({}^{13}C)}\right)$$

That is, the ratio of the abundances of any two species in steady state is the inverse ratio of their destruction rates

How long does it take for a pair of nuclei to reach steady state?

The time to reach steady state is approximately the reciprocal of the *destruction rate for the more fragile nucleus*.

Eg. for ¹²C and ¹³C [absorb
$$\rho Y_p$$
 into λ for simplicity];
i.e. $\lambda_{12} = \rho Y_p \lambda_{p\gamma} ({}^{12}\text{C}); \ \lambda_{13} = \rho Y_p \lambda_{p\gamma} ({}^{13}\text{C})]$
 $\frac{dY_{13}}{dt} = -Y_{13} \lambda_{13} + Y_{12} \lambda_{12} \qquad \frac{dY_{12}}{dt} \approx -Y_{12} \lambda_{12} \qquad \text{lgnore any reactions that create } 1^2\text{C}$
Let $u = Y_{13} / Y_{12}$ then

$$\frac{du}{dt} = \frac{1}{Y_{12}} \frac{dY_{13}}{dt} - \frac{Y_{13}}{Y_{12}^2} \frac{dY_{12}}{dt} = \lambda_{12} - \frac{Y_{13}}{Y_{12}} \lambda_{13} + \frac{Y_{13}}{Y_{12}} \lambda_{12}$$
$$= \lambda_{12} + u (\lambda_{12} - \lambda_{13})$$

A sampling of Bates from Cauchian and Foulay /1988)

Integrating and assuming $Y_{13} = 0$ at t = 0 and $\frac{Y_{13}}{Y_{12}} = \frac{\lambda_{12}}{\lambda_{13}}$

after a time τ_{ss} = time required to reach steady state, one has with some algebra

$$\tau_{ss} = \frac{\ln\left(\frac{\lambda_{12}}{\lambda_{13}}\right)}{(\lambda_{12} - \lambda_{13})}$$

nb. always > 0 since ln of a number < 1 is negative

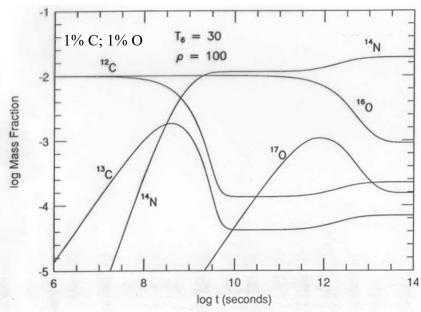
which says steady state will be reached on the faster of the two reaction time scales, $1/\lambda_{12}$ or $1/\lambda_{13}$

		A sampling	of Rates from Cau	ghlan and Fowler (1	988)
	T6	12C (pg)	13C (pg)	14N(pg)	
	246802505000 111505000	8.51(-39) 2.95(-29) 1.24(-24) 1.01(-21) 4.51(-18) 2.86(-16) 3.85(-14) 1.26(-12) 1.79(-11) 8.57(-10) 3.88(-11)	2,69(-38) 9,71(-29) 4,15(-24) 3,44(-21) 4,07(-19) 1,55(-17) 9,90(-16) 1,34(-13) 4,39(-12) 6,27(-11) 3,01(-9) 4,71(-8)	9.88(-44) 4.17(-33) 5.85(-28) 1.02(-24) 2.06(-22) 1.17(-20) 1.18(-18) 2.73(-16) 1.30(-14) 2.46(-13) 1.76(-11) 3.64(-10)	
fastest at 30	2 4 6 8 10 12 15 225 30 50	15N (pa) 1.92(-39) 8.69(-29) 1.28(-23) 2.32(-20) 4.81(-18) 2.82(-16) 2.95(-14) 7.23(-12) 3.62(-10) 7.18(-9) 5.60(-7) 1.25(-5)	160 (pg) 2.68 (-48) 1.23 (-36) 5.52 (-31) 2.00 (-27) 6.79 (-25) 5.75 (-23) 9.11 (-21) 3.60 (-18) 2.51 (-16) 6.35 (-15) 6.94 (-13) 1.93 (-11)	170 (pa) 2.64 (-49) 1.36 (-37) 6.70 (-32) 2.65 (-28) 9.68 (-26) 8.82 (-24) 1.55 (-21) 1.06 (-18) 4.07 (-16) 3.47 (-14) 9.11 (-12) 2.43 (-10)	

At
$$T_6 = 30$$
 $\rho Y_p = 100$

 $\left(\rho Y_{p} \lambda_{p\gamma} {}^{(15}N)\right)^{-1} = 1.4 \times 10^{6} \operatorname{sec} \qquad {}^{!5}N \leftrightarrow {}^{14}N \text{ (quickest)}$ $\left(\rho Y_{p} \lambda_{p\gamma} {}^{(13}C)\right)^{-1} = 1.5 \times 10^{8} \operatorname{sec} \qquad {}^{12}C \leftrightarrow {}^{13}C \text{ (}2^{nd} \text{ quickest)}$ $\left(\rho Y_{p} \lambda_{p\gamma} {}^{(12}C)\right)^{-1} = 5.6 \times 10^{8} \operatorname{sec} \qquad {}^{12}C \leftrightarrow {}^{14}N \text{ (quick)}$ $\left(\rho Y_{p} \lambda_{p\gamma} {}^{(14}N)\right)^{-1} = 4.2 \times 10^{10} \operatorname{sec} \qquad \text{one cycle of the main CNO cycle}$ $\left(\rho Y_{p} \lambda_{p\alpha} {}^{(17}O)\right)^{-1} = 2.9 \times 10^{11} \operatorname{sec} \qquad {}^{17}O \leftrightarrow {}^{16}O \text{ (slow)}$ $\left(\rho Y_{p} \lambda_{p\gamma} {}^{(16}O)\right)^{-1} = 1.6 \times 10^{12} \operatorname{sec} \qquad {}^{16}O \leftrightarrow {}^{14}N \text{ (very slow)}$

Steady state after several times these time scales.



 $\rho = 10$ would be more appropriate for massive stars where T is this high, so the real time scale should be about 10 times greater. Also lengthened by convection.

TABLE 2

STELLAR PARAMETERS AND DERIVED ABUNDANCES

Provided steady state has been achieved the abundance ratios are just given by the λ ' s.

In steady state the abundance ratio ${}^{13}C/{}^{12}C$ is much greater than in the sun.

	Star	T _{eff} (K)	log g	$\log \epsilon (^{12}C)$	¹² C/ ¹³ C	[C/M]		
And this is sometimes			N	<i>1</i> 4				
observed	1403	4200	1.3	6.70	5	-0.67		
	1408	4350	1.6	6.65	5	-0.72		
	1412/V4	4100	0.5	≲5.6		$\lesssim -1.85$		
Giant stars in the	1514	3800	0.4	6.25	5	-1.12		
Giant stars in the	1608	4600	2.0	6.75	6	-0.63		
globular cluster M4	1617	4350	1.6	6.40	3:	-0.93		
giobulai ciustei M4	1622	4650	2.1	7.00	3-5:	-0.35		
	1625	4200	1.3	6.30	5:	- 1.07		
	1701	4500	1.9	7.10	4	-0.25		
Suntzeff and Smith	2206	4150	1.2	6.75	4	-0.60		
	2307	3950	0.9	6.40	4	-0.95		
(ApJ, 381, 160, (1991)	2406/V13	3950	0.6	6.30	3.	- 1.02		
(, .pc, cc , , .cc, (.cc , ,	2410	4350	1.6	6.80	5-10:	-0.59		
	2422	4300	1.5	6.50	3	-0.83		
	2519	4200	1.3	6.85	4	-0.50		
	2608	4300	1.5	6.85	5	-0.52		
	2617	4050	1.1	6.60	5	-0.77		
	2623	4500	1.9	6.65	3-5:	-0.70		
	3309	4700	2.2	7.15		-0.30		
	3404	4700	2.2	7.05		-0.40		
	3612	4150	1.2	6.60	3	-0.73		
	3624	4100	1.1	6.70	5	-0.67		
	4201	4300	1.5	6.70	5	-0.67		
	4310	4250	1.4	6.90	5	-0.47		
	4404	4650	2.1	7.10		-0.35		
	4413	4550	1.9	7.00	3	-0.32		
	4415	4300	1.5	6.70	5:	-0.67		
	4416	4450	1.8	6.50	5-10:	-0.89		
	4421	4350	1.6	6.55	6:	-0.83		
	4509	4650	2.1	6.95	5-10:	-0.44		
	4511	4050	1.0	6.55	6	-0.83		
	4630	4200	1.4	6.75	5	-0.62		

But it doesn't always work so well. E.g. $\frac{{}^{15}N}{{}^{14}N}$ in the sun has a ratio

$$\left(\frac{^{15}N}{^{14}N}\right)_{\odot} = 3.7 \times 10^{-3}$$

T _H	(¹⁵ N/ ¹⁴ N) _{SS}
20	3.8(-5)
30	3.4(-5)
50	2.9(-5)

But the steady state abundance is

	$-\frac{\lambda_{p\gamma}(^{14}N)}{2}$	
$\left(\frac{14}{N}\right)_{\odot}$	$= \frac{1}{\lambda_{p\alpha}({}^{15}N)}$	~ 3 \ 10

Will have to make ^{15}N somewhere else not in steady state with ^{14}N

```
Hydrogen Burning
Nucleosynthesis Summary
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- ¹²C destroyed by hydogen burning. Turned into ¹³C if incomplete cycle. ¹⁴ N otherwise.
- ¹³C produced by incomplete CNcycle. Made in low mass stars. Ejected in red giant winds and planetary nebulae
- ¹⁴N produced by the CNO cycle from primordial ¹²C and ¹⁶O present in the star since its birth. A secondary element. Made in low mass (M < 8 M_o) stars and ejected in red giant winds and planetary nebulae. Exception: Large quantities of "primary" nitrogen can be made in very massive stars when the helium convective core encroaches on the hydrogen envelope.

Also $\frac{{}^{13}C}{{}^{14}N}_{\odot} = 0.035$ but $T_6 \qquad \frac{{}^{13}C}{{}^{14}N}_{ss} = \frac{\lambda_{py}({}^{14}N)}{\lambda_{py}({}^{12}C)}$ 20 2.0(-3) 30 7.9(-3) 40 7.7(-3) So one can make $\frac{{}^{13}C}{{}^{12}C}$ large but cannot make $\frac{{}^{13}C}{{}^{14}N}$ big compared with its solar value. Cardinal rule of nucleosynthesis - you must normalize to your biggest overproduction, nitrogen in this case.

Way out: Make ¹³C in a CN process that has not reached steady state (because of the longer life of ¹³C(p, γ)¹⁴N, e.g., make ¹³C in a region where just a few protons are mixed in with the carbon and then convection cools the material.

- ¹⁵N Not made sufficiently in any normal CNO cycle> Probably made in classical novae as radioactive ¹⁵O
- ¹⁶O Destroyed in the CNO cycle. Made in massive stars by helium burning
- ^{17}O Used to be made in massive stars until the rate for $^{17}\text{O}(\text{p},\alpha)^{14}\text{N}$ was remeasured and found to be large. probably made in classical novae
- ¹⁸O made in helium burning by ¹⁴N(α,γ)¹⁸F(e⁺v)¹⁸O
- ²³Na Partly made by a branch of the CNO cycle but mostly made by carbon burning in massive stars.
- ²⁶AI long lived radioactivity made by hydrogen burning but more by explosive neon burning in massive stars

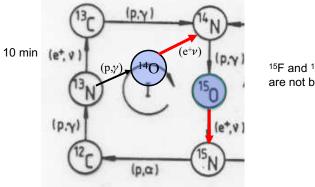
Hydrogen burning at high temperature ($T > 10^8 K$)

Sites:

- Nova explosions on accreting white dwarfs $(T_{9} \sim 0.4)$
- X-ray bursts on accreting neutron stars $(T_0 \sim 1 - 2)$
- Supermassive stars
- neutrino driven wind in core collapse supernovae ?

Suppose keep raising the temperature of the CNO cycle. Is there a limit how fast it can go? Suppose ${}^{13}N(p,\gamma){}^{14}O$ faster than 10 min?

Eventually one gets hung up on the finite life times for ¹⁴O (70.6 s) and ¹⁵O (122 s) to decay by positron emission. This has several interesting consequences:



¹⁵F and ¹⁶F are not bound

Slowest rates are weak decays of ¹⁴O and ¹⁵O.

The β -limited CNO cycle

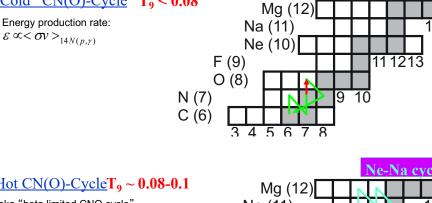
- Material accumulates in ¹⁴O and ¹⁵O rather than ¹⁴N, with interesting nucleosynthetic consequences for ¹⁵N. But can the material cool down fast enough that ¹⁵N is not destroyed by ¹⁵N(p, α)¹²C in the process?
- The nuclear energy generation rate becomes ٠ temperature insensitive and exceptionally simple

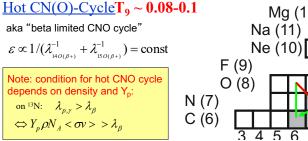
 $\varepsilon_{nuc} = 5.9 \times 10^{15} \text{ Z erg g}^{-1} \text{ s}^{-1}$

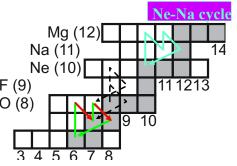
As the temperature continues to rise matter can eventually break out of ¹⁴O and ¹⁵O especially by the reaction ${}^{15}O(\alpha,\gamma){}^{19}Ne(p,\gamma){}^{20}Na(p,\gamma){}^{21}Mg(e^+\nu)$ The rp-process (Wallace and Wooslev 1981).

<u>"Cold" CN(O)-Cycle</u> $T_9 < 0.08$

 $\mathcal{E} \propto < \sigma v >_{14N(p,v)}$

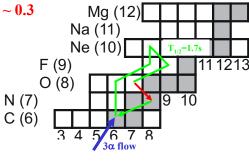






<u>Very Hot CN(O)-Cycle</u> $T_0 \sim 0.3$

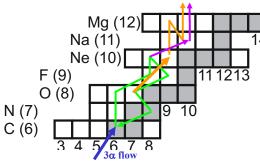
still "beta limited" but other nuclei involved



Breakout

processing beyond CNO cycle after breakout via:

 $T_9 > 0.3 \ {}^{15}O(\alpha, \gamma)^{19}Ne$ $T_9 > 0.6 \ {}^{18}Ne(\alpha, p)^{21}Na$



- Typically the luminosity rises rapidly to the Eddington luminosity for one solar mass (~10³⁸ erg s⁻¹) and stays there for days (fast nova) to months (slow nova)
- In Andromeda (and probably the Milky Way) about 40 per year. In the LMC a few per year.
- Evidence for membership in a close binary –

 Nova Aquila (1918) – Kraft (1964)

 0.06 days
 (GQ-Mus 1983)

 2.0 days
 (GK Per 1901)

 see Warner, Physics of Classical Novae, IAU Colloq 122, 24 (1990)

For a list of novae and their characteristics see

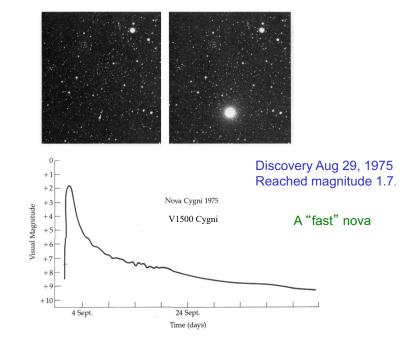
https://en.wikipedia.org/wiki/List_of_novae_in_the_Milky_Way_galaxy

V603 Aquila (1918) m = -0.5; brightest in modern times

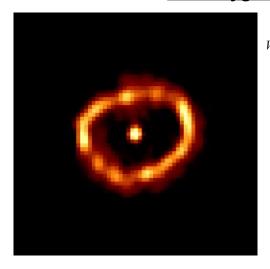
One place where the β -limited CNO cycle is important is classical novae. Another is in x-ray bursts on neutron stars.

Classical Novae

- Distinct from "dwarf novae" which are probably accretion disk instabilities (lower L, shorter recurrence times)
- Thermonuclear explosions on accreting white dwarfs. Unlike supernovae, they recur, usually (but not always) on long (>1000 year) time scales.
- Rise in optical brightness by > 9 magnitudes
- Significant brightness change thereafter in < 1000 days
- Evidence for mass outflow from 100's to 5000 km s⁻¹
- Anomalous (non-solar) abundances of elements from carbon to sulfur



Nova Cygni 1992



Visible to the unaided eye (m = 4.4). Photo at left is from HST in 1994. Discovered Feb. 19, 1992. Spectrum showed evidence for ejection of large amounts of neon, oxygen, and magnesium,

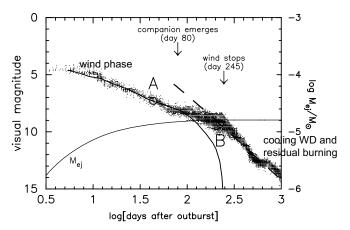
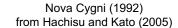
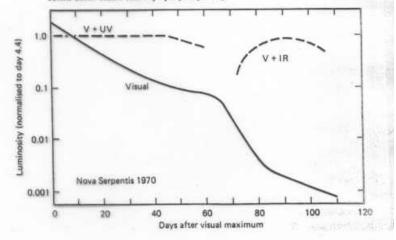


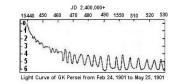
Fig. 4.—*Thick solid line:* visual magnitude of free-free emission from the optically thin ejecta, based on eq. (1), scaled to fit at day 43 (*point* A). The flux decays with a slope of $\sim t^{-3}$ after the wind stops, scaled to fit at day 224 (*point* B). *Thin solid line:* ejected mass (M_0) from the WD by the optically thick winds. Here we assume 1D 2448.665.0 as the date of the outburst. *Points:* observational magnitudes taken from the AVSO archive. Two epochs of the nova outburst are indicated by arrows: the companion emerges from the WD photosphere, and the optically thick nova wind stops. [See the electronic edition of the *Journal for a color version of this figure.*]

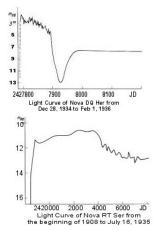


DUST FORMATION

Fig. 4.1.2. The luminosity of the nova FH Serpentis as a function of time since its outburst. The visible light declined soon after outburst, to be replaced by ultraviolet radiation and later by infrared radiation. Thus the total (bolometric) luminosity of FH Ser remained high for several months (adapted from J. S. Gallagher & S. Starrfield, 1978, Ann. Rev. Astr. Astrophys., 16, 171).





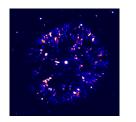


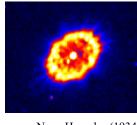
Fast nova – rise is very steep and the principal display lasts only a few days. Falls > 3 mag within 110 days

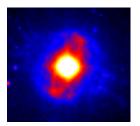
Slow nova – the decline by 3 magnitudes takes at least 100 days. There is frequently a decline and recovery at about 100 days associated with dust formation.

Very slow nova - display lasts for years.

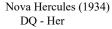
An earth mass or so is ejected at speeds of 100s to 1000s of km/s. Years later the ejected shells are still visible. The next page shows images from a ground-based optical survey between 1993 and 1995 at the William Hershel Telescope and the Anglo-Australian Telescope.





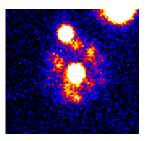


Nova Persei (1901) GK Per





Nova Pictoris (1927) RR Pic



Nova Cygni (1975) V1500 Cygni

Nova Serpentis (1970) FH Ser

http://www.jb.man.ac.uk/~tob/novae/

Models

A white dwarf composed of either C and O (usually $< 1.06 M_{\odot}$) or O, Mg, and Ne (usually > 1.06 M_o) accretes hydrogen - rich material from a companion star at a slow rate of $10^{-8.5\pm1}$ M_o / yr

As the matter piles up, it becomes dense and hot. It is heated at its base chiefly by gravitational compression, though the temperature of the white dwarf itself may play a role.

Ignition occurs at a critical pressure of 2'10¹⁹ dyne cm⁻² (Truran and Livio 1986 - assumptions R, M constant, $\Delta R \ll R$); basically this is the condition that $T_{base} \sim 10^7 \text{ K} = T_{H-ignition}$

This implies a certain critical mass since

$$\Delta M_{ign} \approx \frac{4\pi P_{ign}}{G} \frac{R_{WD}^{4}}{M_{WD}} \sim 10^{-6} - 10^{-4} M_{\odot}$$

i.e.,
$$\frac{dP}{dm} = \frac{-GM}{4\pi r^4};$$
$$dm = 4\pi r^2 \rho dr$$

Addendum:

2 x 10¹⁹ dyne cm⁻²? 10⁷ K?

Prialnik in his textbook says 2×10^{18} dyne cm⁻²; 2×10^{7} K

I ran a half dozen models with Kepler to check. Found 2 x 10⁷ K is a better temperature for the onset of the runaway. The pressure ranged from 3 x 10¹⁸ to 9 x 10¹⁸ dyne cm⁻² at runaway. The density was around 5 $\times 10^3$ g cm⁻³ and went down as the runaway developed. Mildly degenerate. Burning continued throughout the nova, not just at the beginning.

Runaway is when the rise time for the temperature at the base becomes much shorter than the time for the accreted mass to increase. It is not a degeneracy condition as described in Prialnik's text.

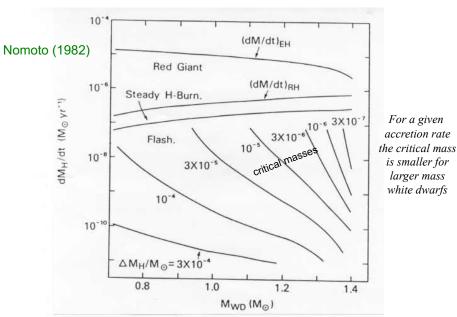
Thermal inertia effects are important at high accretion rates.

Models

$$R_{WD} \approx 8.5 \times 10^{8} \left[1.286 \left(\frac{M_{WD}}{M_{\odot}} \right)^{-2/3} - 0.777 \left(\frac{M_{WD}}{M_{\odot}} \right)^{2/3} \right]^{1/2} cm \qquad R \propto M^{-1/3} cm M$$

Eggleton (1982) as quoted in Politano et al (1990)

This gives a critical mass that decreases rapidly (as $M^{-7/3}$) with mass. Since the recurrence interval is this critical mass divided by the accretion rate, bursts on high mass white dwarfs occur more frequently even though they are rarer by number.



The mass of the accreted hydrogen envelope at the time the hydrogen ignites is a function of the white dwarf mass and accretion rate.

Iben 1982 gives

$$t_{rec} = 570 \text{ yr} \left(\frac{1.5 \times 10^{-8}}{\dot{M}}\right)^{1/3} 10^{-4.38(M_{WD}-1.)} X_{H}^{-1} \\ \times \left[1 - 0.29 \left(\frac{\dot{M}}{1.5 \times 10^{-8}}\right)^{0.3}\right]$$

which could be as low as 6 years for $10^{-7}~M_{\odot}~yr^{-1}$

on a 1.35 $\rm M_{\odot}$ white dwarf.



See Darnley et al (*Nature* 2019 – January 29) for evidence of a nova recurring on time scales of years for millions of years (supershell – 100 pc in diameter – in Andromeda). M31N 2008-12a is the most frequently recurring nova. $M_{crit} \sim 10^{-7} M_{O}$. Authors speculate it could be growing to the Chandraseekhar mass (but presumably NeOMg WD not CO so not SN Ia)

Mass WD	Interval (10 ⁵ yr)	Eve wh
0.60	12.9	the
0.70	7.3	ma
0.80	4.2	The
0.90	2.4	con
1.00	1.2	is e
1.10	0.64	by I
1.20	0.28	eve
1.30	0.09	
1.35	0.04	

Truran and Livio (1986) using Iben (1982) –

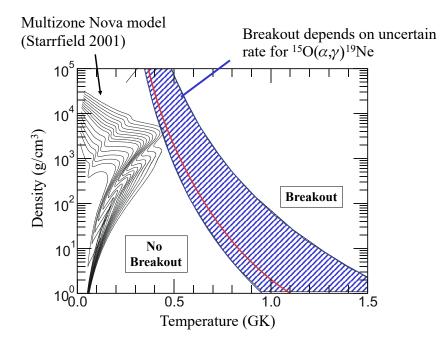
Even though the average mass white dwarf is 0.6 - 0.7 solar masses the most often observed novae have masses around 1.14 solar masses.

These would be white dwarfs composed of Ne, O, and Mg. It is estimated that ~ 1/3 of novae, by number, occur on NeOMg WDs even though they are quite rare.

see also Ritter et al, ApJ, 376, 177, (1991)

Politano et al (1990) in *Physics of Classical* Novae
$$\begin{split} \mathbf{M}_{wD} &= 1.0 \text{ } \mathbf{M}_{\odot} \quad \dot{\mathbf{M}} = 1.\times 10^{-9} \text{ } \mathbf{M}_{\odot} \text{ } y^{-1} \\ R_{wD} &\approx 5500 \text{ km} \quad \mathbf{L}_{wD} = 0.01 \text{ } \mathbf{L}_{\odot} \\ \text{Accreted layer } \Delta \mathbf{R} &\approx 170 \text{ } \text{ km} \\ \mathbf{X}_{H} &= 0.70 \quad \mathbf{X}_{He} = 0.28 \quad \mathbf{X}_{C} = 0.01 \quad \mathbf{X}_{O} = 0.01 \\ \Delta M &\approx \frac{4\pi R^{4} P_{crit}}{GM} = 4 \times 10^{-5} M_{\odot} \\ \rho_{base} &= 2900 \text{ g cm}^{-3} T_{base} = 1.8 \times 10^{7} \text{ K} \quad P_{base} = 9 \times 10^{18} \text{ dyne cm}^{-2} \\ \overline{\rho} &\sim \frac{\Delta M}{4\pi R^{2} \Delta R} \sim 1500 \text{ g cm}^{-3} \\ \text{degeneracy parameter } \eta = 2.7 \end{split}$$

Partially degenerate



Nature of the burning:

Confusing statements exist in the literature. A nova is not a degenerate flash that happens in seconds and then is over (like a SN Ia). The ignition is partly degenerate but actually resembles a thin shell instability more than a nuclear runaway. So long as the radius of the center of mass of the burning layer does not increase dramatically, the pressure at the base stays constant. Some expansion occurs but not enough to put the burning out. At constant P, when density goes down, T goes up.

So the hydrogen continues to burn for a long time, dredging up C and O as it proceeds. Hydrostatic equilibrium maintains the luminosity at near the Eddington value. Matter is lost as a "super-wind", not as a blast wave.

The dredge up of C and O is very important to the energetics and nucleosynthesis

For the beta-limited CNO cycle

$$\varepsilon_{nuc} = 5.9 \times 10^{15} \text{ Z erg g}^{-1} \text{ s}^{-1} \qquad \text{Z} \sim 0.01 - 0.1$$

for M = 10⁻⁵ M_o; Z = 0.01

$$L = \varepsilon_{nuc} M \sim 10^{42} \text{ erg s}^{-1}$$

So the initial power is quite super-Eddington, but that drives convection and expansion until a smaller region is burning and the observed peak $L \sim 10^{38} - 10^{39}$ erg s⁻¹.

The binding energy per gram of material at the white dwarf edge is about

$$\frac{GM}{R} \approx \frac{(6.67E - 8)(2E33)}{5E8} \approx 2 \times 10^{17} \text{ erg gm}^{-1}$$

To eject e.g., 3 x 10⁻⁵ solar masses takes about 10⁴⁶ erg. The kinetic energy (e.g., 1000 km/s) is about 10⁴⁵ The integral of the Eddington luminosity for 10^7 s is also about 10^{45} erg. So the binding energy dominates the energy budget ad the light and kinetic energy are a small fraction of that.

In some cases common envelope effects may also be important. The companion star is inside the nova.

Nucleosynthesis in Novae

Basically ¹⁵N and ¹⁷O

The mass fraction of both in the ejecta is ~ 0.01 , so crudely ...

$$M_{nova}({}^{15}\text{O}) \sim (0.01)(3 \times 10^{-5})(30)(10^{10}) \sim 10^{5} M_{\odot} \qquad \text{Woosley (1986)}$$

$$X_{\text{Pop I}}({}^{15}\text{N}) \sim 10^{5} \underline{/3 \times 10^{10}} \sim 4 \times 10^{-6} \approx \text{ the solar mass fraction}$$

$$\underbrace{\text{approximate Pop I} \qquad \text{of } {}^{15}\text{N and } {}^{17}\text{O in the sun.}$$

material in the Galaxy within solar orbit

Novae also make interesting amounts of ²²Na and ²⁶Al for gamma-ray astronomy

TABLE 2 Heavy-element Mass Fractions in Novae from Optical and Ultraviolet Spectroscopy														
Object	Year	Reference	Н	He	С	Ν	0	Ne	Na-Fe	Z	(Z/Z_{\odot})	$({\rm Ne}/{\rm Ne}_{\odot})$	CNO/Ne-Fe	
Solar		1	0.71	0.27	0.0031	0.001	0.0097	0.0018	0.0034	0.019	1.0	1.0	2.7	
T Aur	1891	2	0.47	0.40		0.079	0.051			0.13	6.8			
RR Pic	1925	3	0.53	0.43	0.0039	0.022	0.0058	0.011		0.043	2.3	6.3	2.9	I I and I alle a
DQ Her	1934	4	0.34	0.095	0.045	0.23	0.29			0.57	30.			H mildly
DQ Her	1934	5	0.27	0.16	0.058	0.29	0.22			0.57	30.			depleted
HR Del	1967	6	0.45	0.48		0.027	0.047	0.0030		0.077	4.1	1.7	25.	uepieleu
V1500 Cyg	1975	7	0.49	0.21	0.070	0.075	0.13	0.023		0.30	16.	13.	12.	
V1500 Cyg	1975	8	0.57	0.27	0.058	0.041	0.050	0.0099		0.16	8.4	5.6	15.	
V1668 Cyg	1978	9	0.45	0.23	0.047	0.14	0.13	0.0068		0.32	17.	3.9	47.	He/H mildly
V1668 Cyg	1978	10	0.45	0.22	0.070	0.14	0.12			0.33	17.			
V693 CrA	1981	11	0.40	0.21	0.004	0.069	0.067	0.023		0.39	21.	128.		enhanced
V693 CrA	1981	12	0.29	0.32	0.046	0.080	0.12	0.17	0.016	0.39	21.	97.	1.3	
V693 CrA	1981	10	0.16	0.18	0.0078	0.14	0.21	0.26	0.030	0.66	35.	148.	1.2	
V1370 Aql	1982	13	0.053	0.088	0.035	0.14	0.051	0.52	0.11	0.86	45.	296.	0.36	CNO
V1370 Aql	1982	10	0.044	0.10	0.050	0.19	0.037	0.56	0.017	0.86	45.	296.	0.48	CINO
GQ Mus	1983	14	0.37	0.39	0.0081	0.13	0.095	0.0023	0.0039	0.2 4	13.	1.2	38.	enhanced
PW Vul	1984	15	0.69	0.25	0.0033	0.049	0.014	0.00066		0.067	3.5	0.38	100.	onnanooa
PW Vul	1984	10	0.47	0.23	0.073	0.14	0.083	0.0040	0.0048	0.30	16.	2.3	34.	
PW Vul	1984	16	0.617	0.247	0.018	0.069	0.0443	0.001	0.0027	0.14	7.7	1.	31.	0
QU Vul	1984	17	0.30	0.60	0.0013	0.018	0.039	0.040	0.0049	0.10	5.3	23.	1.3	Some have very
QU Vul	1984	10	0.33	0.26	0.0095	0.074	0.17	0.086	0.063	0.40	21.	49.	1.7	largo No
QU Vul	1984	18	0.36	0.19		0.071	0.19	0.18	0.0014	0.44	23.	100.	1.4	large Ne
V842 Cen	1986	10	0.41	0.23	0.12	0.21	0.030	0.00090	0.0038	0.36	19.	0.51	77.	
V827 Her	1987	10	0.36	0.29	0.087	0.24	0.016	0.00066	0.0021	0.35	18.	0.38	124.	
QV Vul	1987	10	0.68	0.27		0.010	0.041	0.00099	0.00096	0.053	2.8	0.56	26.	
V2214 Oph	1988	10	0.34	0.26		0.31	0.060	0.017	0.015	0.40	21.	9.7	12.	
V977 Sco	1989	10	0.51	0.39		0.042	0.030	0.026	0.0027	0.10	5.3	15.	2.5	
V433 Set	1989	10	0.49	0.45		0.053	0.0070	0.00014	0.0017	0.062	3.3	0.80	33.	
V351 Pup	1991	19	0.37	0.25	0.0056	0.076	0.19	0.11		0.38	20. 27.	63.	2.4	
V1974 Cyg	1992	18	0.19	0.32		0.085	0.29	0.11 0.037	0.0051	0.49		68.	3.2	
V1974 Cyg V838 Her	1992 1991	20 11	0.30 0.60	0.52 0.31	0.015 0.012	0.023 0.012	0.10 0.004	0.037	0.075	0.18 0.09	9.7 0.11	21. 31.	3.1	

REFERENCES.-(1) Grevesse & Anders 1989; (2) Gallagher et al. 1980; (3) Williams & Gallagher 1979; (4) Williams et al. 1978; (5) Petitjean et al. 1990; (6) Tylenda 1978; (7) Ferland & Shields 1978b; (8) Lance et al. 1988; (9) Stickland et al. 1981; (10) Andreä et al. 1994; (11) Vanlandingham et al. 1997; (12) Williams et al. 1985; (13) Snijders et al. 1987; (14) Morisset & Péquignot 1996; (15) Saizar et al. 1991; (16) Schwarz et al. 1997c; (17) Saizar et al. 1992; (18) Austin et al. 1996; (19) Saizar et al. 1996; (20) Hayward et al. 1996.

Some issues

Burning is not violent enough to give fast ٠ novae unless the accreted layer is significantly enriched with CNO prior to or early during the runaway.

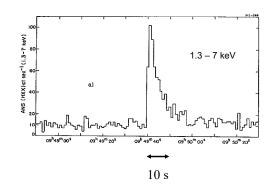
Shear mixing during accretion

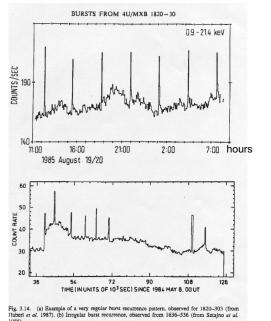
Convective "undershoot" during burst

- CO vs NeO white dwarf
- Making ¹⁵N and ¹⁷O
- Relation to Type Ia supernovae. How to grow M_{WD} when models suggest it is actually shrinking?

Type I X-Ray Bursts

First X-ray burst: 3U 1820-30 (Grindlay et al. 1976) with ANS (Astronomical Netherlands Satellite)

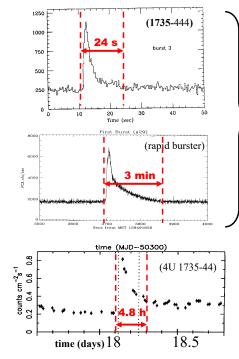




Typical X-ray bursts:

- recurrence: hours-days
- regular or irregular

Frequent and very bright phenomenon !



Normal type I bursts: • duration 10-100 s • ~10³⁹ erg

Superbursts: (discovered 2001, so far 24 seen – Keek et al (2015))

•~10⁴³ erg • rare (every 3.5 yr ?)

Type I X-Ray Bursts (e.g., Strohmayer & Bildsten 2003)

- Burst rise times < 1 s to 10 s
- Burst duration 10's of seconds to minutes (some much longer "superbursts")
- Occur in low mass x-ray binaries
- Persistent luminosity from <0.01 Eddington to 0.2 Eddington (i.e., 10³⁶- 10³⁸ erg s⁻¹)
- Spectrum softens as burst proceeds. Spectrum thermal. A cooling blackbody
- L_{peak} < 4 x 10³⁸ erg s⁻¹. i.e., about Eddington. Evidence for radius expansion in some bursts. T initially 3 keV, decreases to 0.5 keV, then gets hotter again.

- Of 13 known luminous globular cluster x-ray sources, 12 show x-ray bursts. Over 70 total X-ray bursters were known in 2002.
- Distances 4 12 kpc. Two discovered in M31 (Pietsch and Haberl, *A&A*, **430**, L45 (2005).
- Low B-field $< 10^{8-9}$ gauss
- Rapid rotation (at break up? due to accretion?). In transition to becoming ms pulsars?
- Very little mass lost (based upon models). Unimportant to nucleosynthesis

- Back-of-the envelope calculation: $E_{burst} \sim 10^{39} \text{ erg};$ $E_{nuclear} \sim 1 \text{ MeV/nucleon}$ $(\sim 10^{18} \text{ erg/g})$ \Rightarrow fuel $\Delta M \sim 10^{21} \text{ g};$ for $M \sim 10^{-10}$ to $10^{-9} M_{\odot}/\text{yr}$ $\Rightarrow t_{recur} \sim \text{hrs-days}$
- But 1 MeV/nucleon << BE at edge of neutron star (~200 MeV/nucleon)

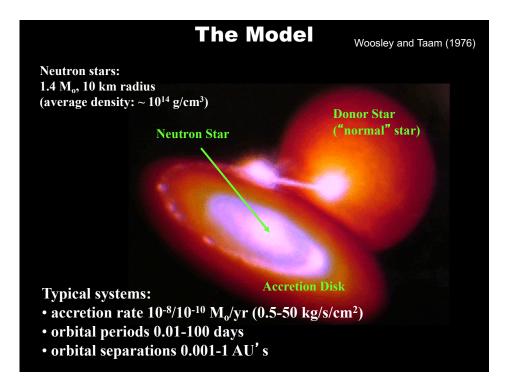
X-ray burst theory predicts three regimes of burning:

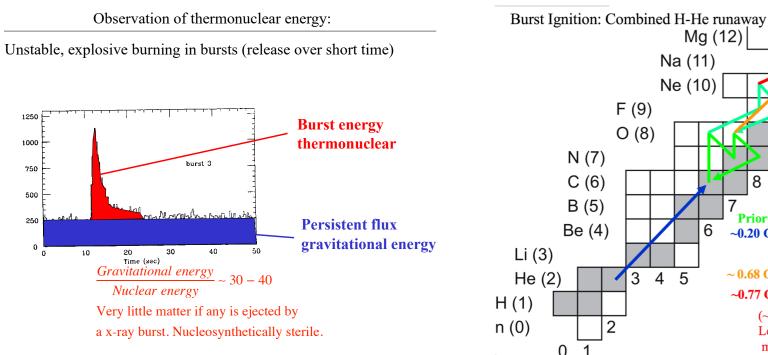
- 1) intermediate accretion rates; $2 \times 10^{-10} M_{\odot} \text{ yr}^{-1} \lesssim \dot{M} \lesssim 4-11 \times 10^{-10} M_{\odot} \text{ yr}^{-1}$: pure He shell ignition after steady H burning
- 2) high accretion rates; $4-11\times 10^{-10}\,M_\odot\,yr^{-1}\lesssim\dot{M}\lesssim 2{\!\!>\!\!\times}\,10^{-8}\,M_\odot\,yr^{-1};$ mixed H/He burning triggered by thermally unstable He ignition
- 3) Accretion rates near Eddington ~ few x 10⁻⁹ carbon fusion powered superbursts. Rare.

During pure helium flashes the fuel is burned rapidly; they last only ~ 5-30 s

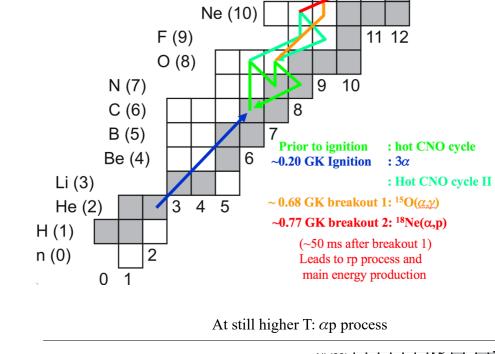
Bursts with unstable mixed H/He burning release their energies on a longer, 10–100 s, timescale, due to the long series of β decays in the rp-process

Superbursts last ~ 1000 s

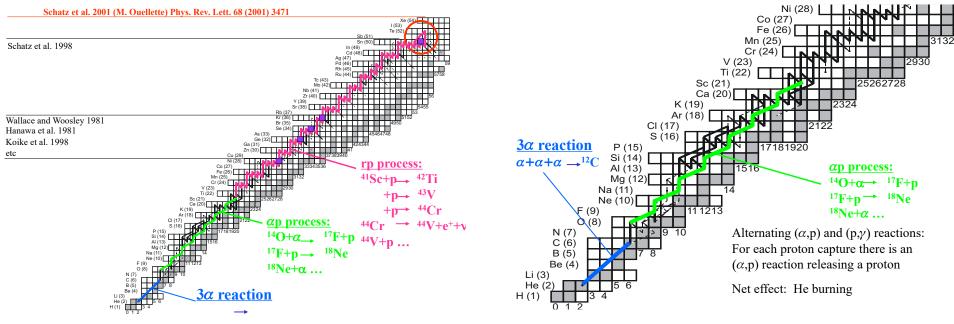


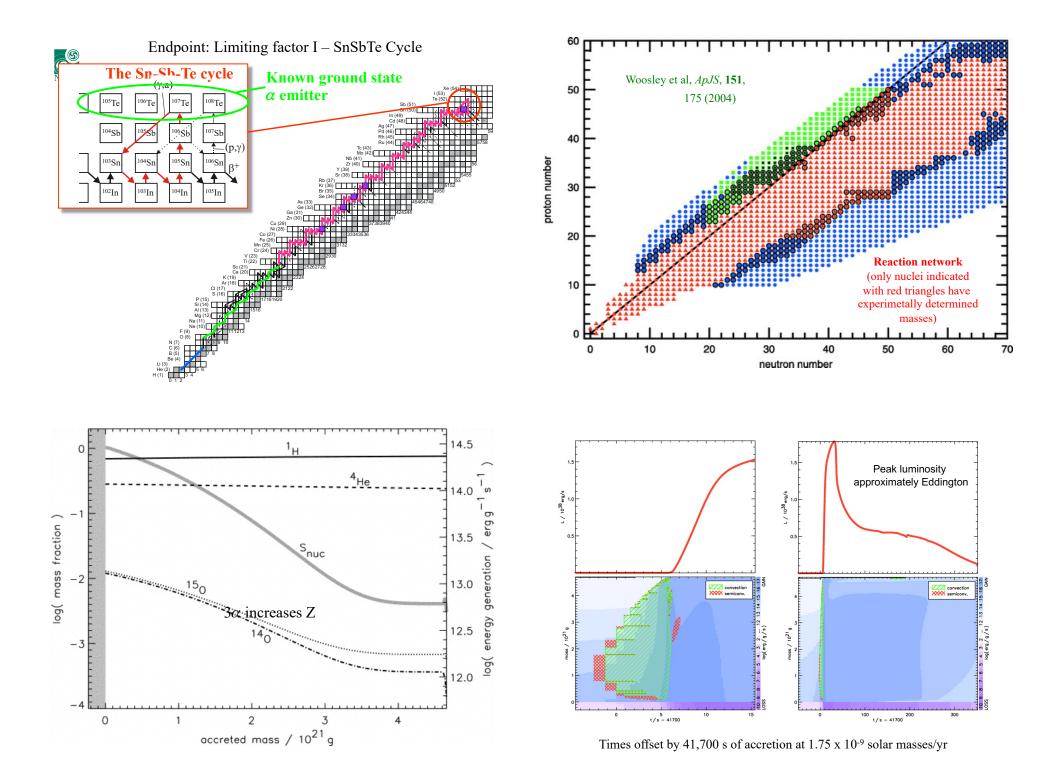


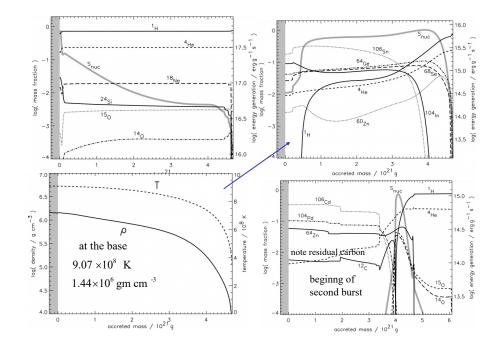
Models: Typical reaction flows

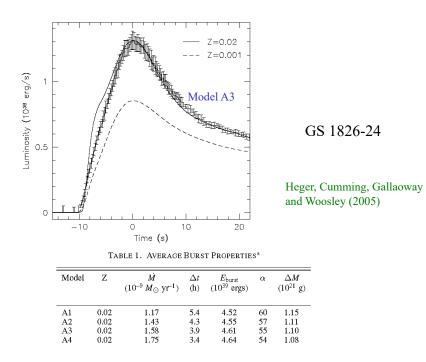


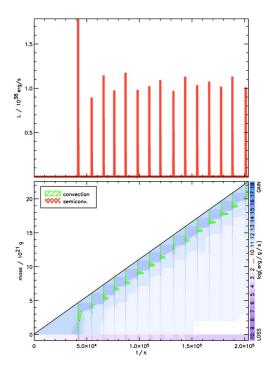
13 14











Fourteen consecutive flashes at about a 4 hours interval.

The first is a start up transient.

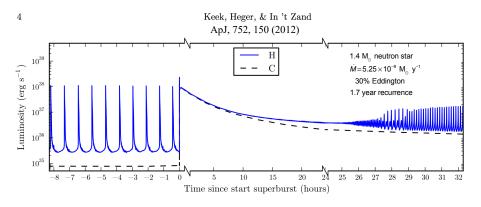
$$\dot{M} = 1.75 \times 10^{-9} M_{\odot} \text{ yr}^{-1}$$

 $Z = Z_{\odot} / 20$

Current Issues:

- Superbursts
- Detailed comparison with an accumulating wealth of observational data, especially time histories of multiple bursts and the effects of thermal inertia
- Large volume of uncertain, yet important reaction rates (FRIB)
- Multi-D models with B fields and rotation spreading of the burning
- Can XRB's be used to obtain neutron star radii, crustal structure, and/or distances

"Superbursts"



About 2 dozen superbursts have been observed. They are thought to be produced by carbon runaways as predicted by Woosley and Taam (1976). The fine structure in the above simulation has not yet been observed Recent 2D simulations from Chris Malone using MAESTRO

http://www.astro.sunysb.edu/cmalone/research/pure_he4_xrb/index.html

XRB models by Alex Heger et al.

http://2sn.org/xrb/movie/